



list



# Une petite histoire autour de la simulation du CND par ondes guidées

une collaboration POEMS-CEA



# OUTLINE

## 1. Overview of guided wave modeling

### 1.1. Context/Motivation

### 1.2. Waveguide and Modal formalism

## 2. Chronology 2006/2024

### 2.1. CIVA evolution

### 2.2. Elastic waveguide

### 2.3. Half Space Matching (HSM)

## 3. Demo

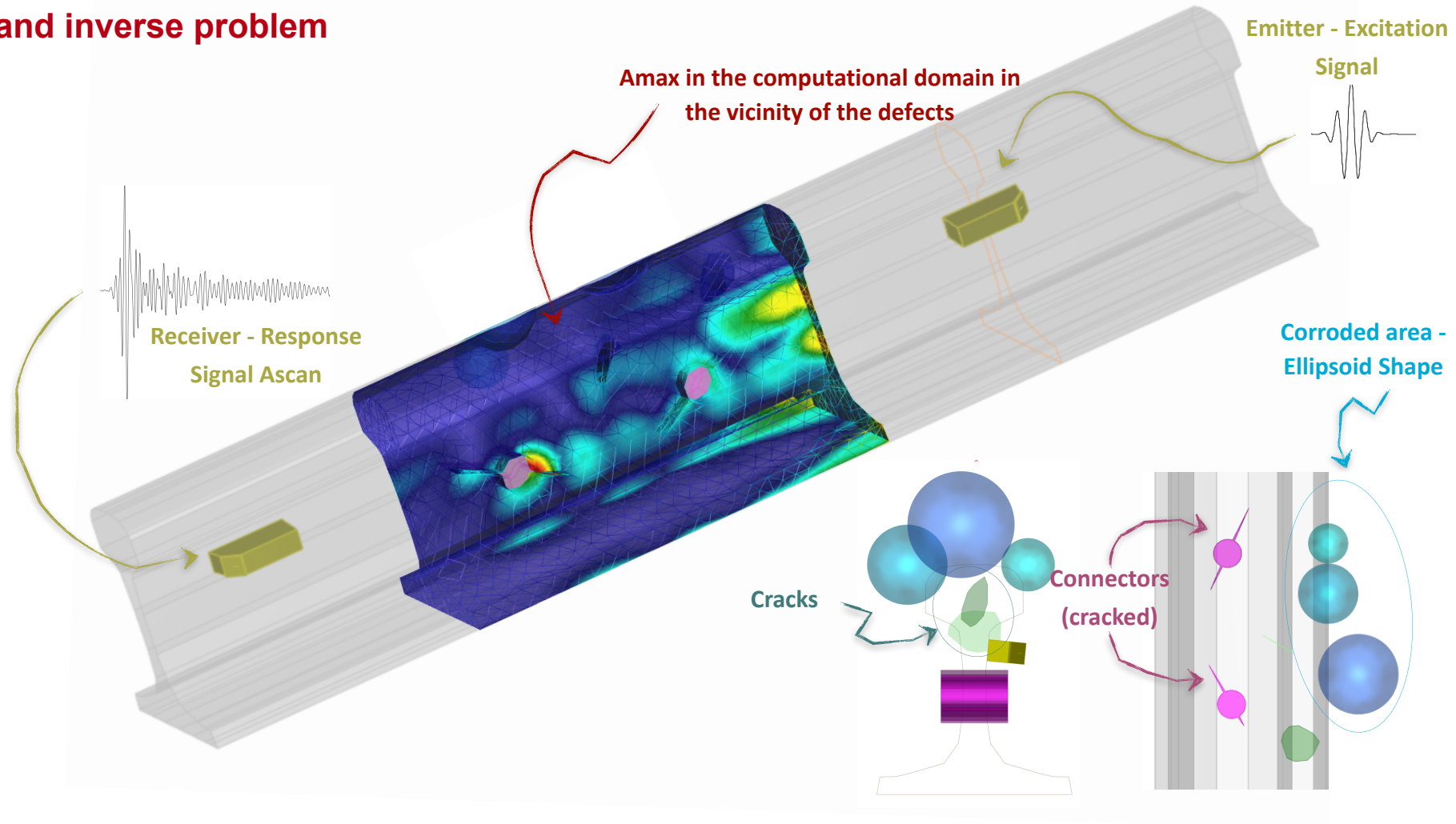


# SIMULATION OF NON DESTRUCTIVE INSPECTION BY GUIDED WAVES

## Context and motivations

Simulate guided waves propagation in a domain containing several localized defects (cracks, corrosion, cavities)

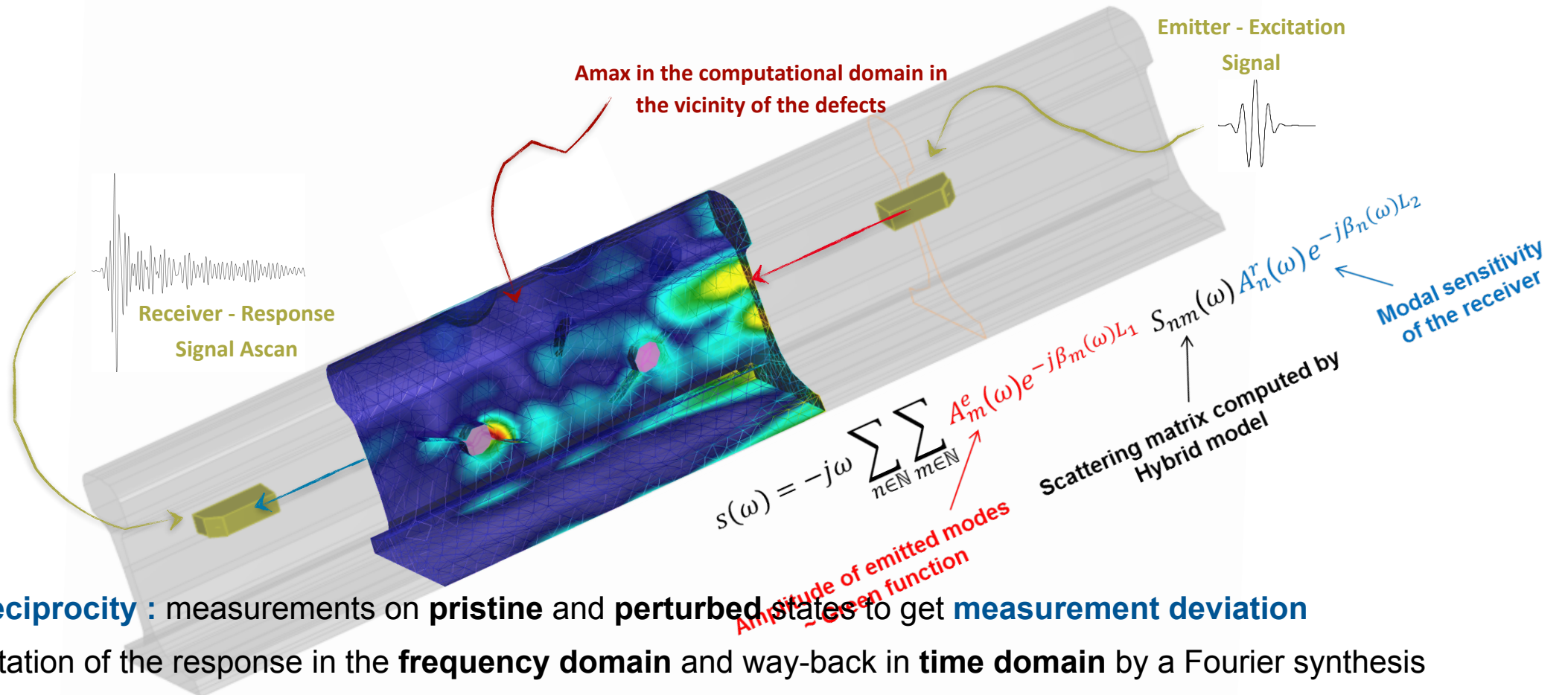
⇒ **direct and inverse problem**



# WAVEGUIDE AND MODAL FORMALISM

## Modal Formalism

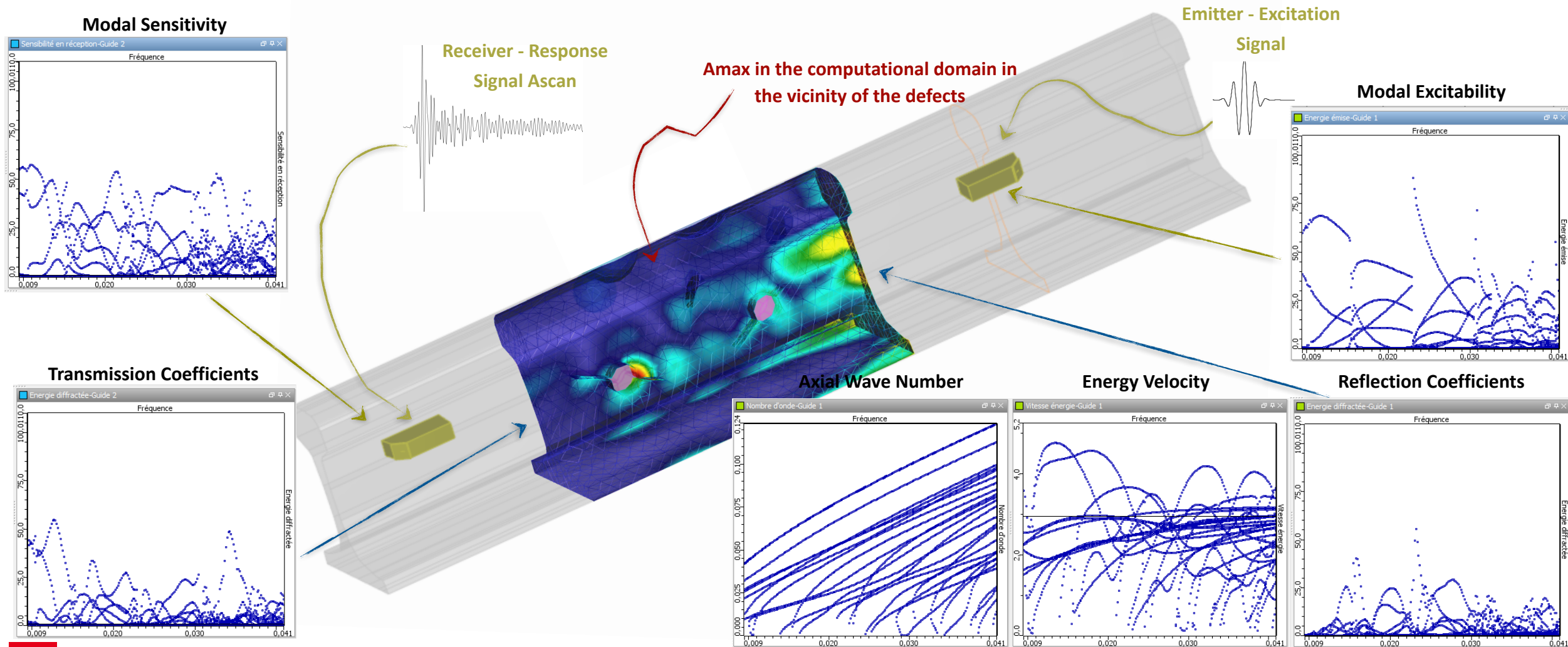
- ▶ The elastodynamic field is represented by a **superposition of modes** at a given frequency  $\omega$



- ▶ **Auld reciprocity** : measurements on **pristine** and **perturbed** states to get **measurement deviation**
- ▶ Computation of the response in the **frequency domain** and way-back in **time domain** by a Fourier synthesis

# WAVEGUIDE AND MODAL FORMALISM

Dispersion curves for the representation of all modal quantities over a frequency range



# 3 MODULES TO UNDERSTAND AND SIMULATE THE PHYSIC OF GUIDED WAVES



## Modes Computation

- ▶ Determination of the modes propagating in the structure in the frequency domain
- ▶ Modal characteristics (phase/energy velocity, wave number, attenuation...) represented in the form of dispersion curves

## Field Computation

- ▶ Determination of the elastodynamic field radiated by a source in different sections of the structure
- ▶ Modal Excitability of the source (dispersion curves)

## Inspection Simulation

- ▶ Determination of the time signal received by the receiver
- ▶ Modal conversions related to the perturbations/defects of the structure (energy dispersion curves)

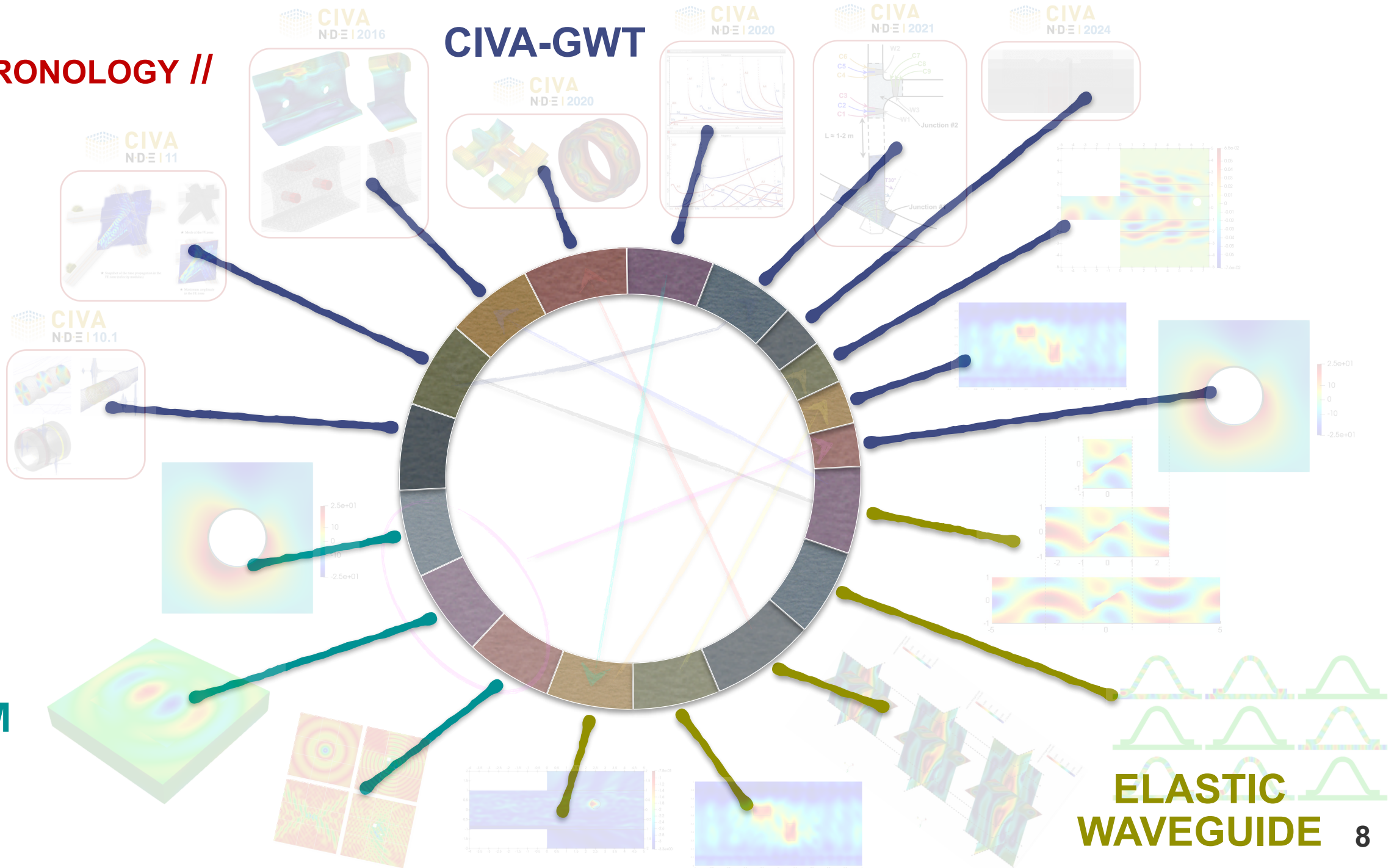
# OUTLINE

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# CHRONOLOGY //

# CIVA-GWT

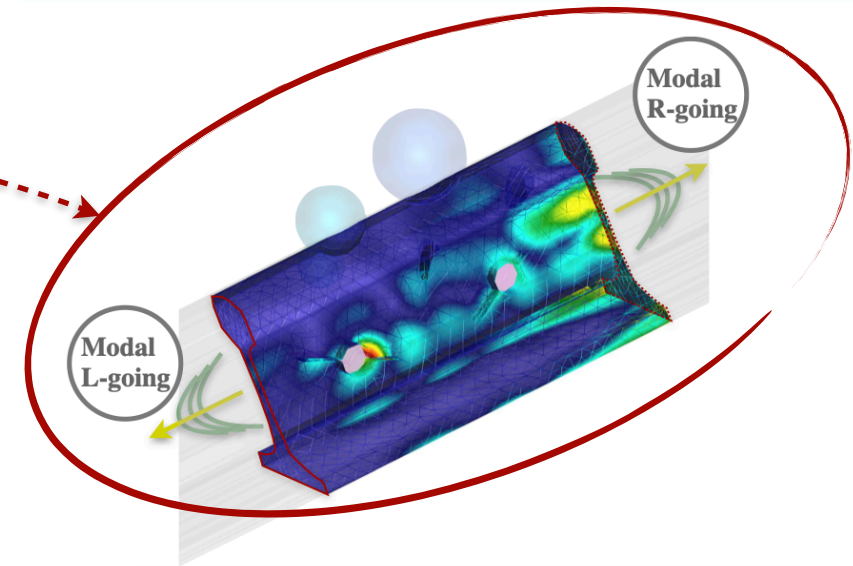
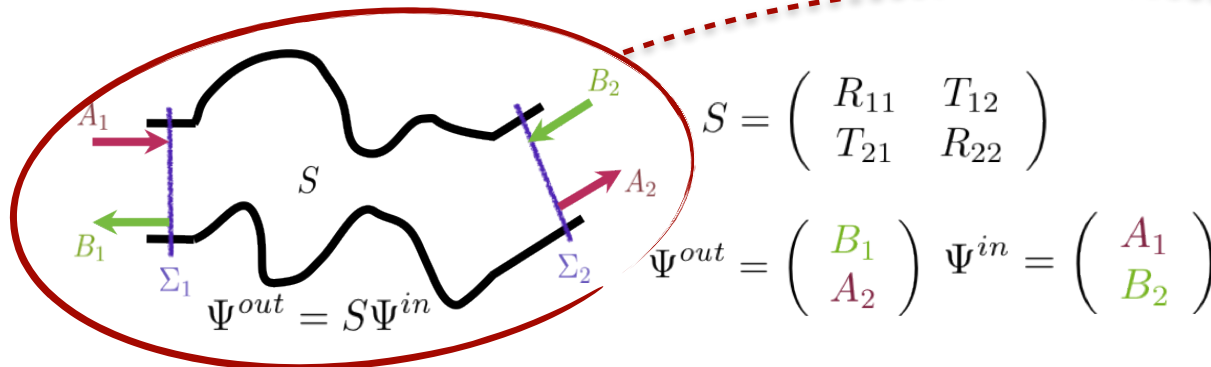
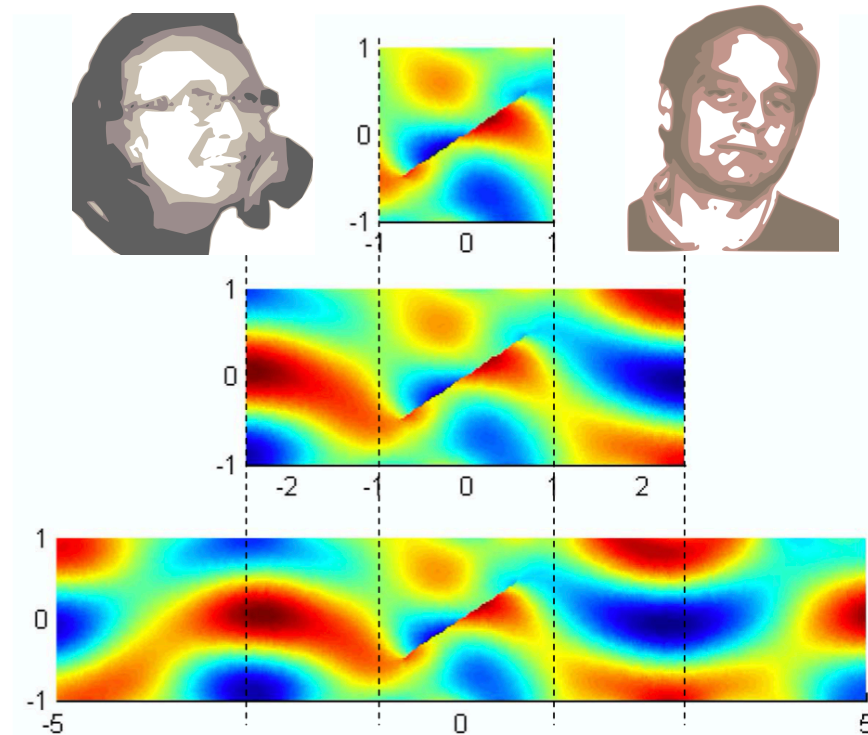


# SCATTERING IN ELASTIC WAVEGUIDE : PART 1

## Transparent Boundary Conditions (TBC) in elastic waveguide

V. Baronian, A-S. Bonnet-Ben Dhia and E. Lunéville, **TBC for the harmonic diffraction problem in an elastic waveguide** (2010)

- ▶ **Coupling FE/Modal representations, XY formalism  $\Rightarrow$  YtoX operator** (generalization of DtN map), arbitrary localized perturbation
- ▶ **Code : MELINA**
- ▶ **Exact Condition** (No spurious reflection) - **Non local** TBC (lost of sparsity)
- ▶ **Orthotropic** medium (orthogonality « Fraser »)
- ▶ Gives the **scattering matrix** : Modes conversions and sensitivity toward the defect are known



A. Maurel, V. Pagneux, **Lamb wave propagation in inhomogeneous elastic waveguide** (2002)

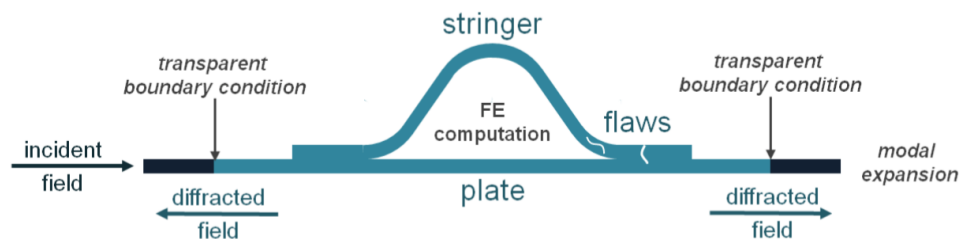
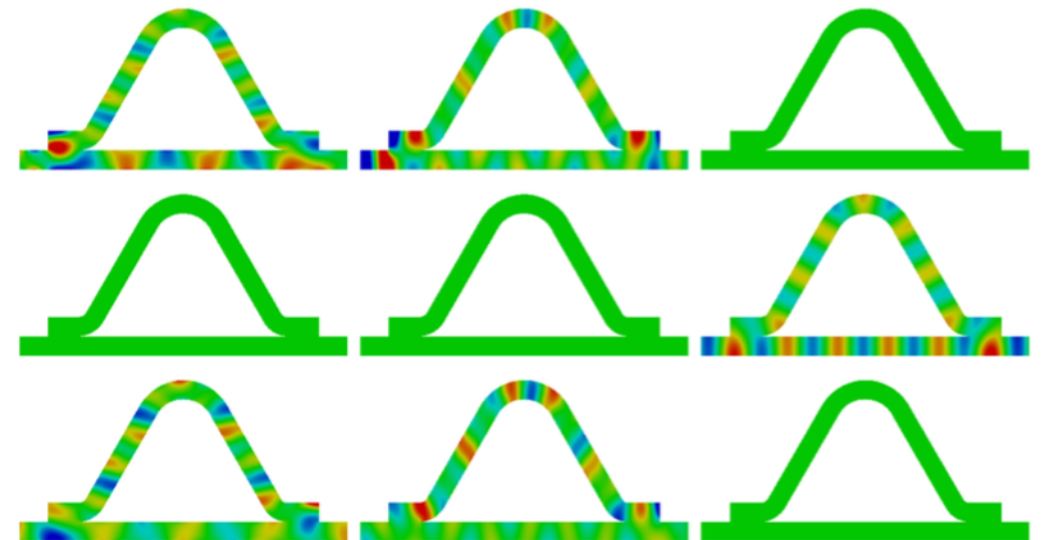
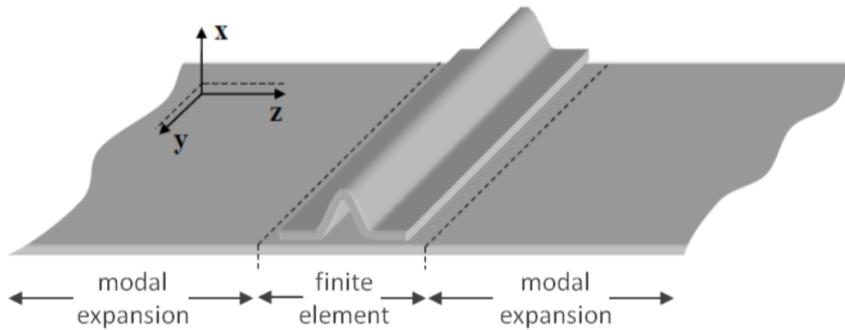
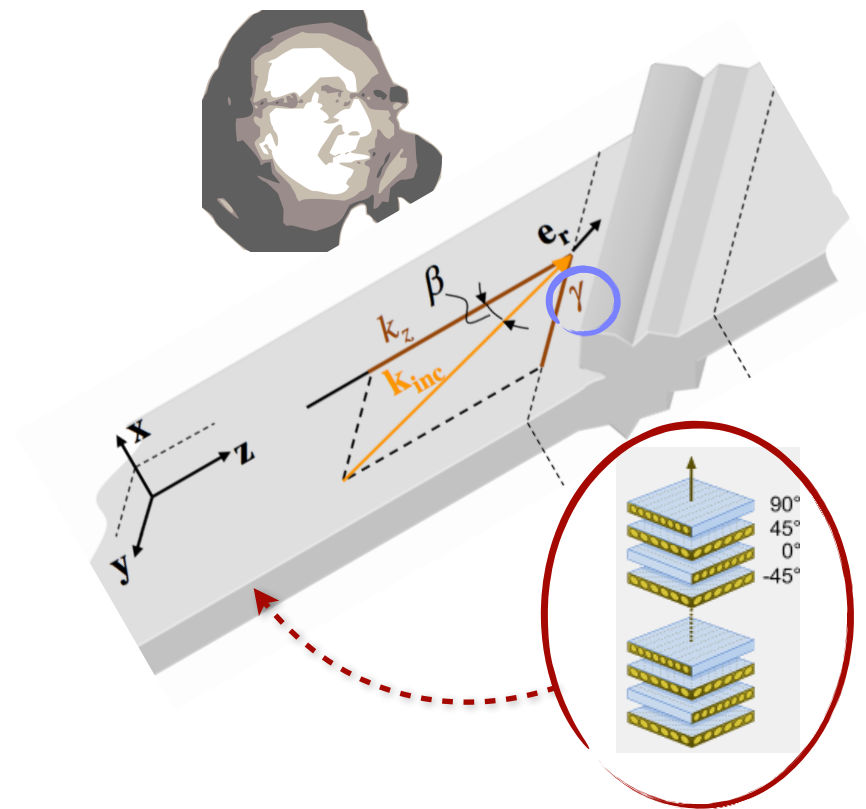
V. Pagneux, A. Maurel, **Scattering matrix properties with evanescent modes for waveguides in fluids and solids** (2004)

# SCATTERING IN ELASTIC WAVEGUIDE : PART 2

TBC for 2D elastic waveguide with obliquely incident wave (L. Taupin - 2008/2011)

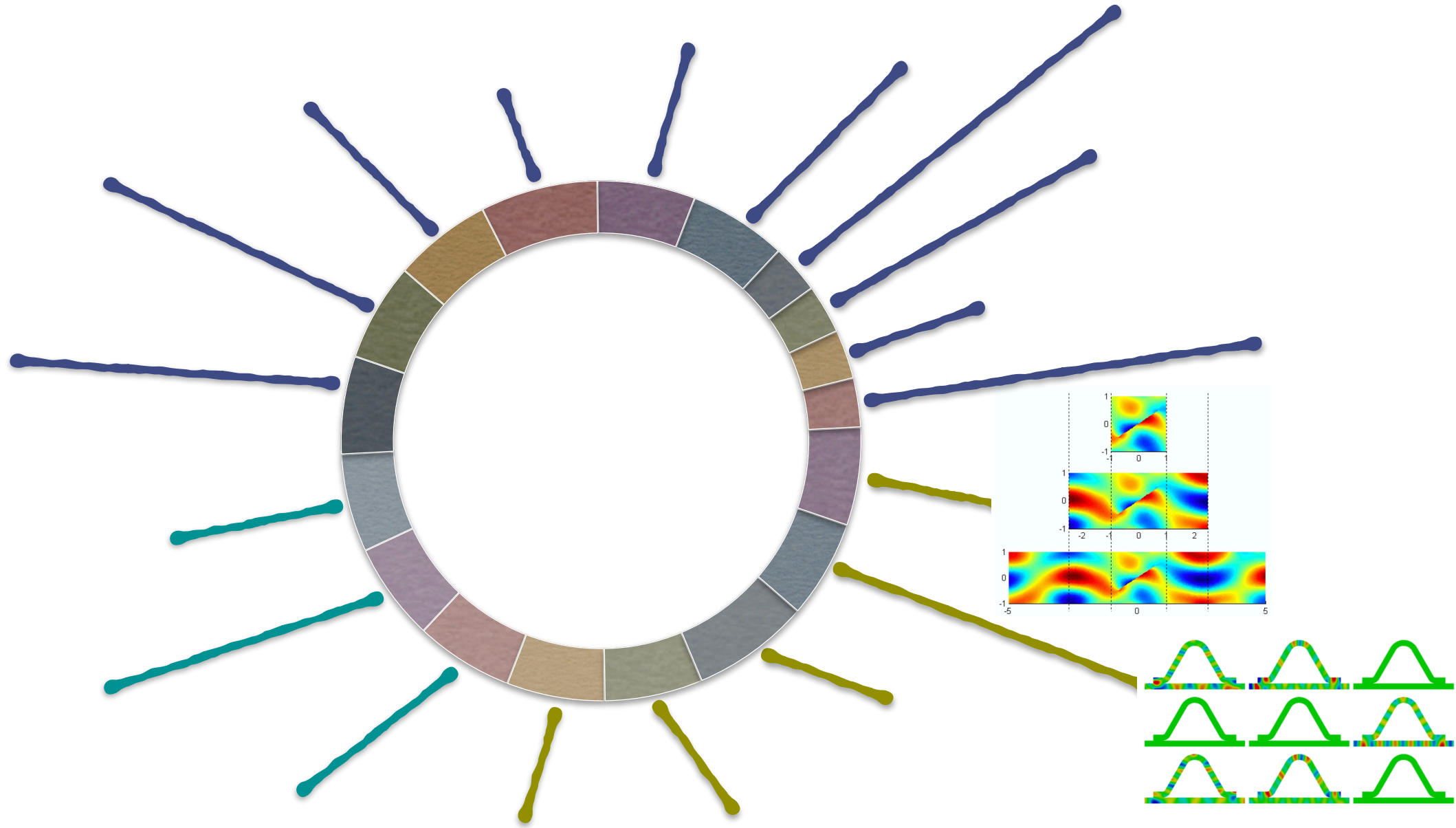
L. Taupin, A. Lhémy, V. Baronian, A-S. Bonnet-Ben Dhia, **Scattering of obliquely incident guided waves by a stiffener bonded to a plate** (2011)

- ▶ Coupling FE/Modal representations, **XY formalism**  $\Rightarrow$  **YtoX operator**
- ▶ Code : **MELINA**  $\Rightarrow$  **XLIFE++**
- ▶ **Linear flaw** (translational invariance)
- ▶ **Anisotropic** medium (lost of orthogonality « Fraser »)





# CHRONOLOGY //



# CHRONOLOGY OF CIVA : THE BEGINNING (2012)

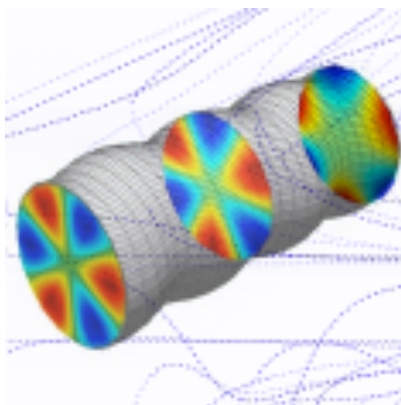
Development of 3 modules (Modes/Beam/Inspection) to simulate propagation in elastic waveguide

K. Jezzine, *Approche modale pour la simulation globale de contrôles non destructifs par ondes guidées* (2006)

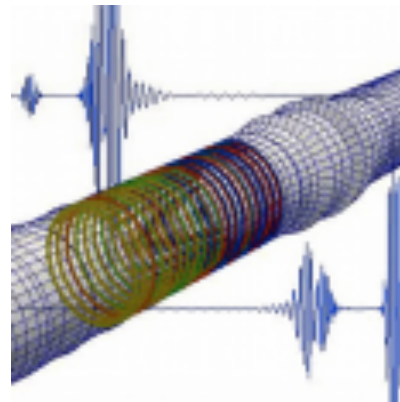
- ▶ **Geometry** : 2D cartesian and axisymmetric
- ▶ **Flaws** : vertical crack only
- ▶ **Numerical methods** : **SAFE** (modes/beam computation), **Modes Matching** (modes interaction) and **Modal synthesis** (time domain)
- ▶ **Isotropic material**
- ▶ **Contribution** : K. Jezzine (2006)

$$s(\omega) = -j\omega \sum_{n \in \mathbb{N}} \sum_{m \in \mathbb{N}} A_m^e(\omega) e^{-j\beta_m(\omega)L_1} S_{nm}(\omega) A_n^r(\omega) e^{-j\beta_n(\omega)L_2}$$

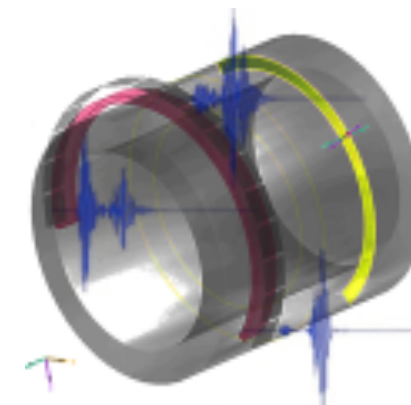
MODES COMPUTATION



BEAM COMPUTATION

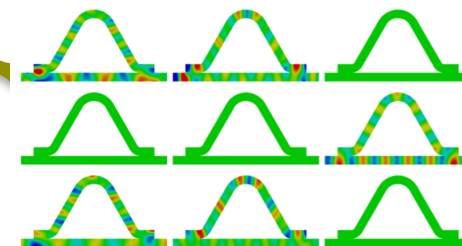
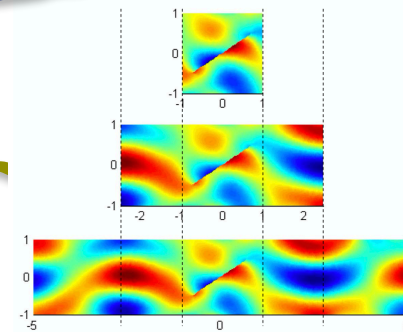
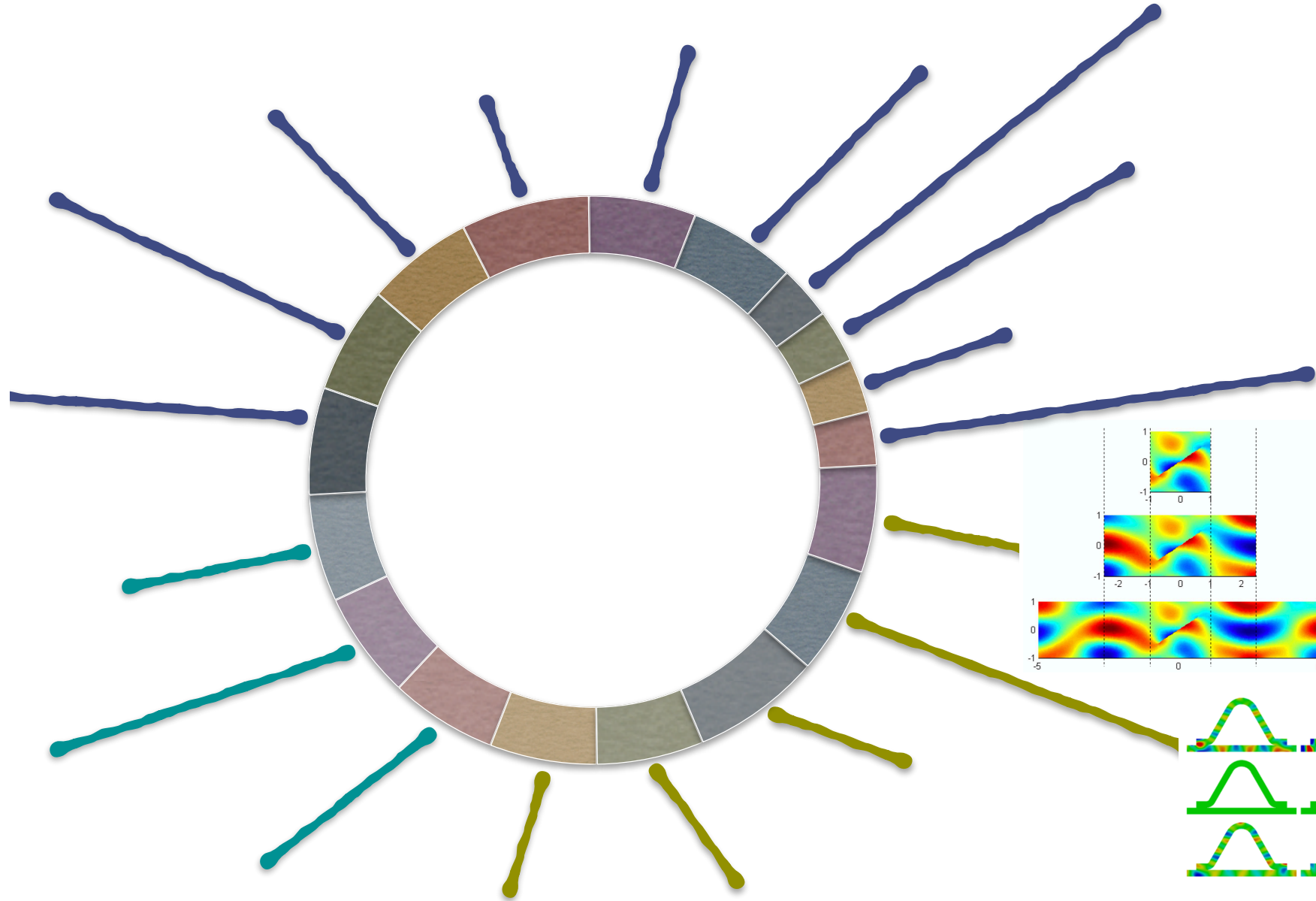
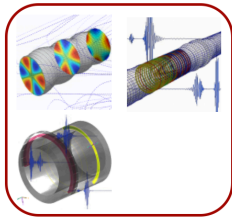


INSPECTION SIMULATION



# CHRONOLOGY //

CIVA  
NDE | 10.1

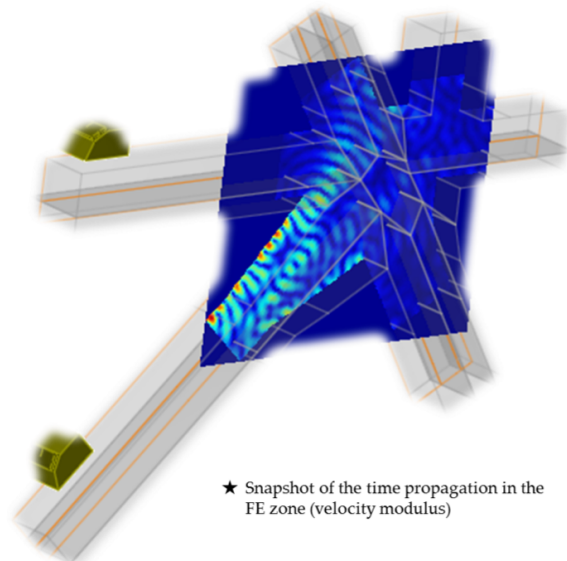


# CHRONOLOGY OF CIVA : YTOX PART 1 (2014 : +5 YEARS...)

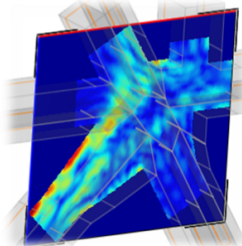
## 1st implementation of YtoX method / automatic 2D meshing

C. Geuzaine, J-F. Remacle, **Gmsh: a three-dimensional finite element mesh generator with built-in pre- and post- processing facilities** (2009)

- ▶ **Geometry : 2D cartesian and axisymmetric specimens for modes interaction**
- ▶ **Flaws : arbitrary perturbations**
- ▶ **Numerical methods : 2D Hybrid FE/Modal coupling** (modes interaction)
- ▶ **Isotropic material**
- ▶ **Contribution : K. Jezzine (2006) - V. Baronian (2009) - GMSH (2D mesh)**

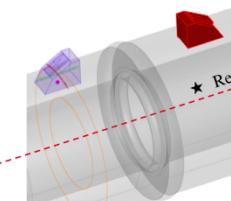
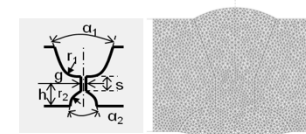


★ Mesh of the FE zone

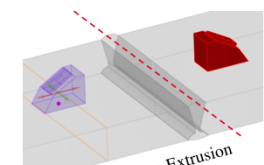


★ Maximum amplitude in the FE zone

### • Weld

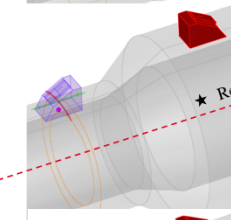
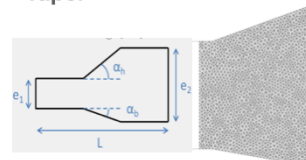


★ Revolution

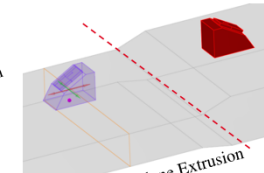


★ Plane Extrusion

### • Taper

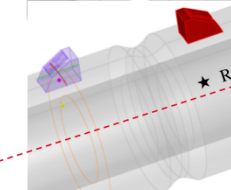
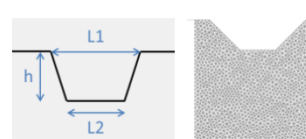


★ Revolution

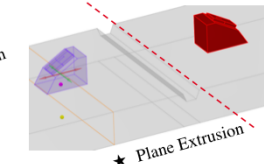


★ Plane Extrusion

### • Groove

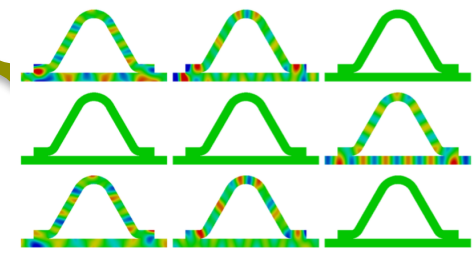
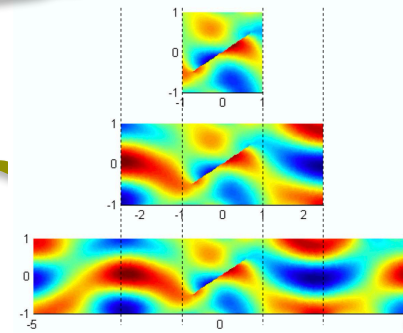
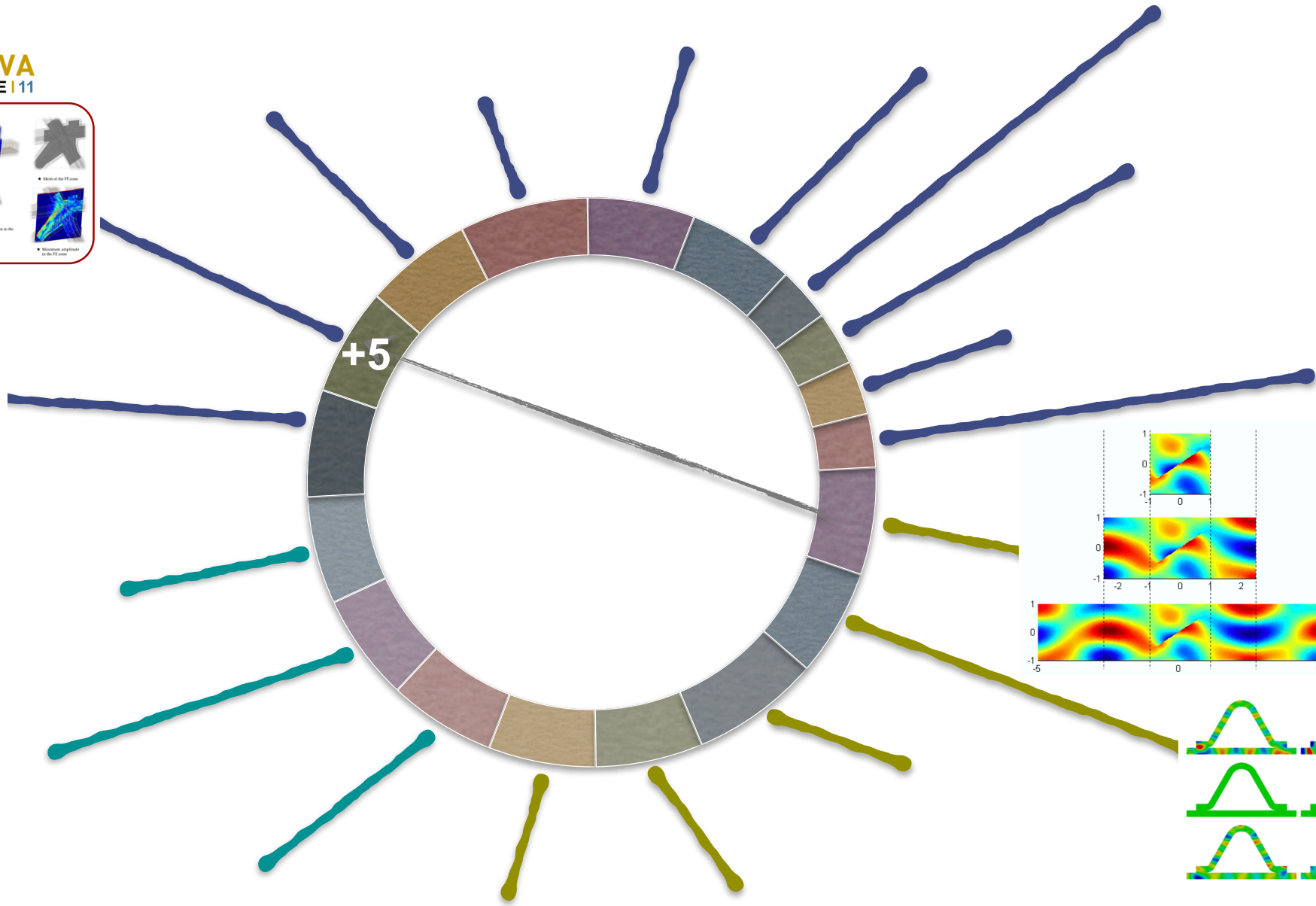
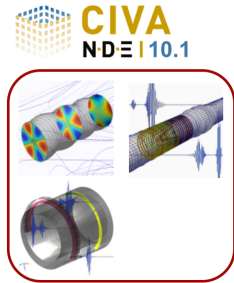
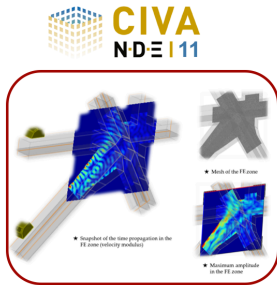


★ Revolution



★ Plane Extrusion

# CHRONOLOGY //



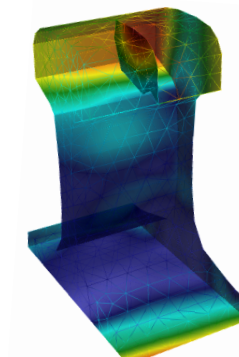
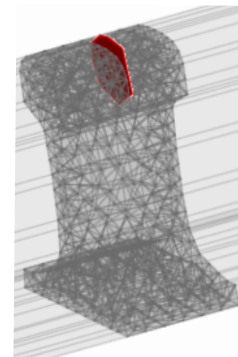
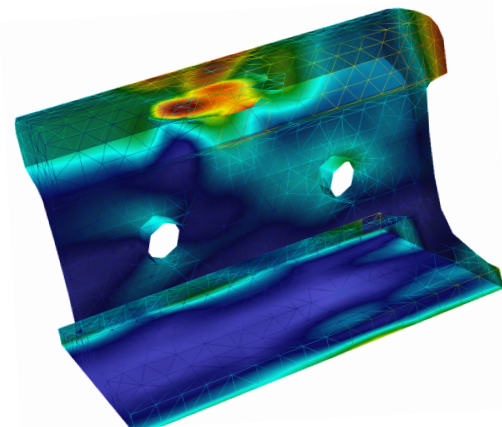
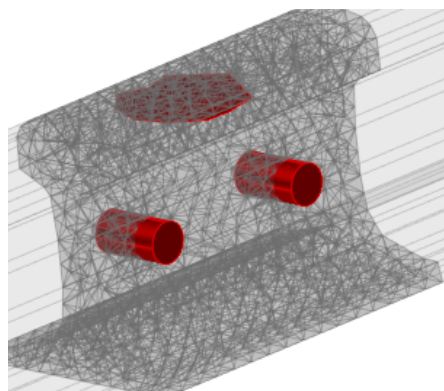
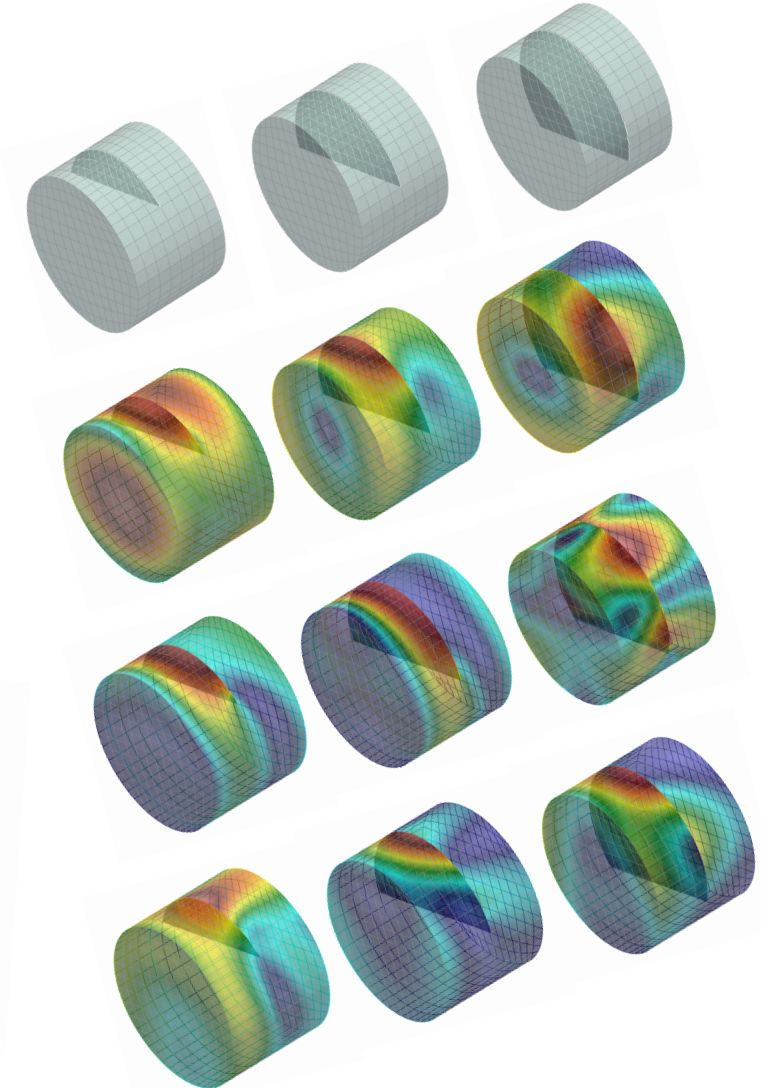


# CHRONOLOGY OF CIVA : Y2X PART 2 (2016 : +2 YEARS...)

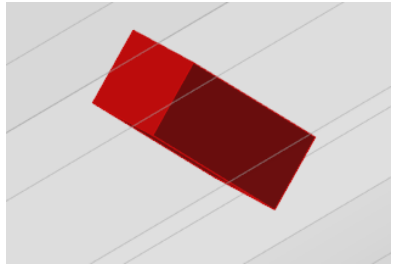
## 2nd implementation of YtoX method / automatic 3D meshing

C. Geuzaine, J-F. Remacle, **Gmsh: a three-dimensional finite element mesh generator with built-in pre- and post- processing facilities** (2009)

- ▶ **Geometry : 3D cylinder of arbitrary cross section for modes interaction**
- ▶ **Flaws : arbitrary perturbations (complex surface crack, cavities)**
- ▶ **Numerical methods : 3D Hybrid FE/Modal coupling (modes interaction)**
- ▶ **Isotropic material**
- ▶ **Contribution : K. Jezzine (2006) - V. Baronian (2009) - GMSH (3D mesh)**



# FEATURED FLAWS



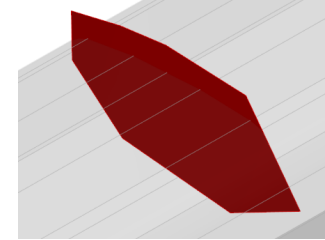
*Rectangular block*



*Rectangular crack*



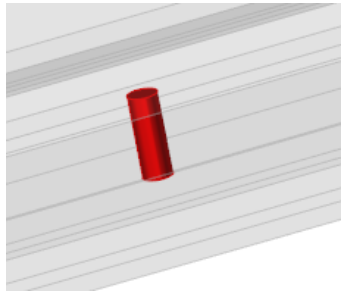
*Semi elliptical crack*



*CAD-contoured crack*



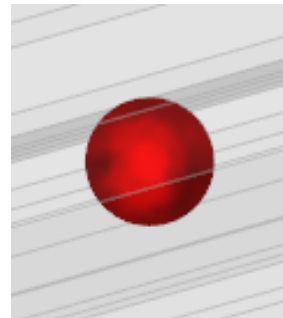
*Multi-faceted defect*



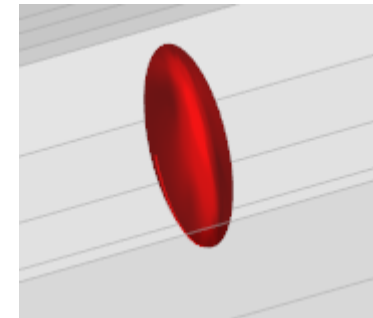
*Flat bottom hole*



*Hemispherical bottom hole*



*Spherical*



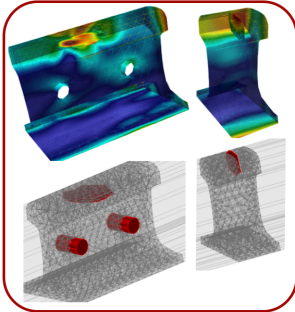
*Ellipsoidal*



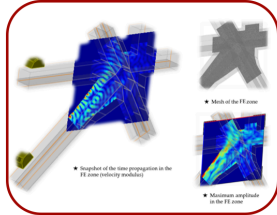
*Branched defect*

# CHRONOLOGY //

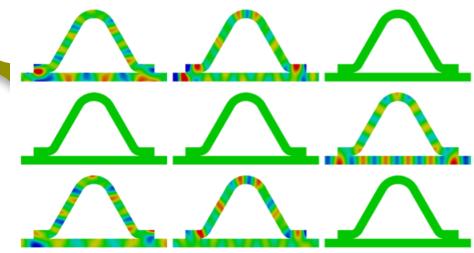
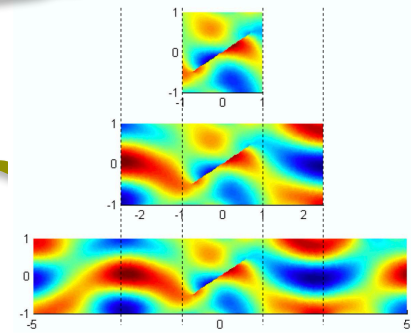
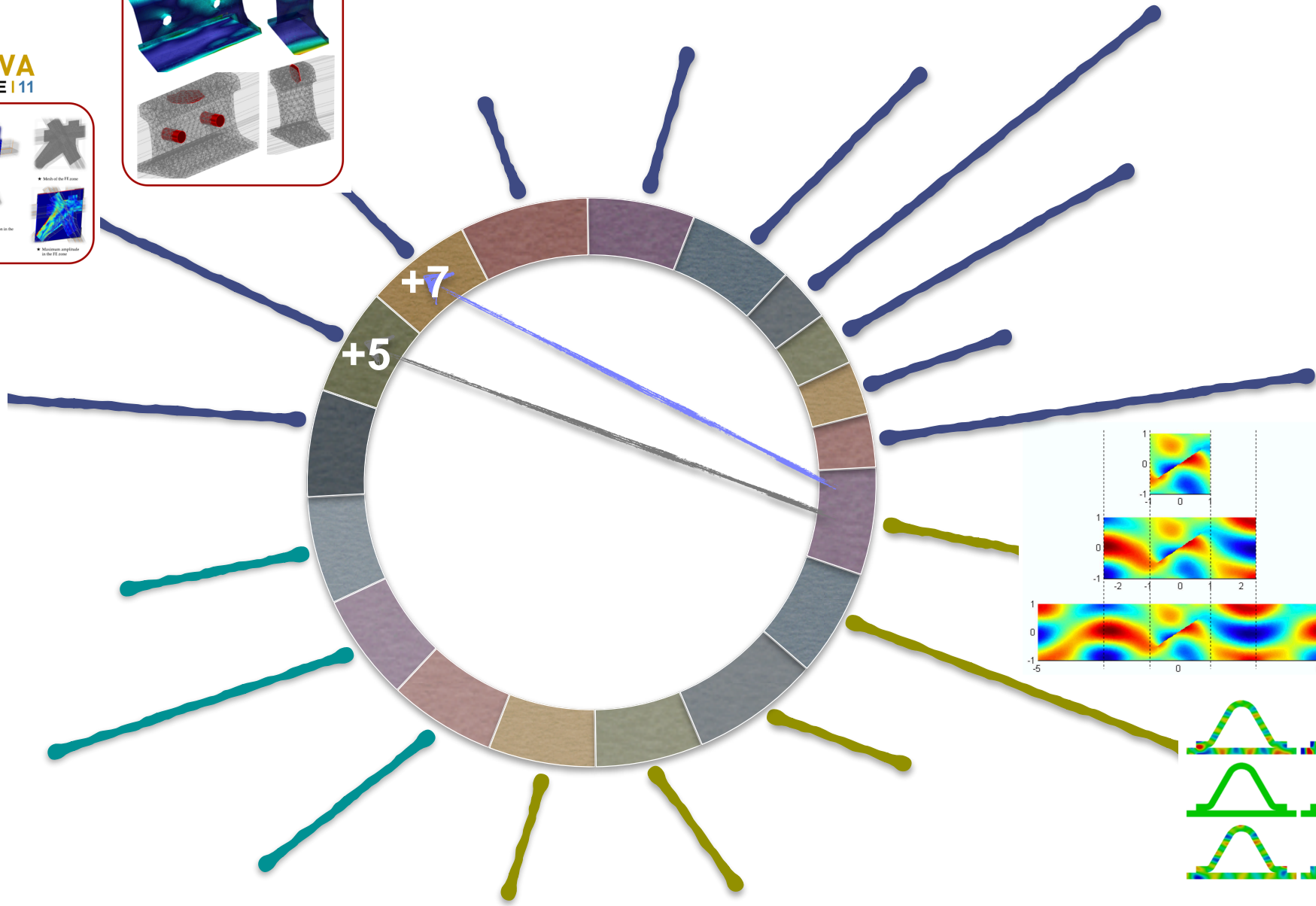
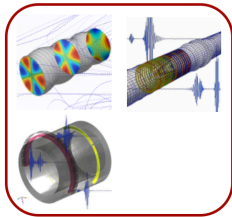
CIVA  
NDE | 2016



CIVA  
NDE | 11



CIVA  
NDE | 10.1



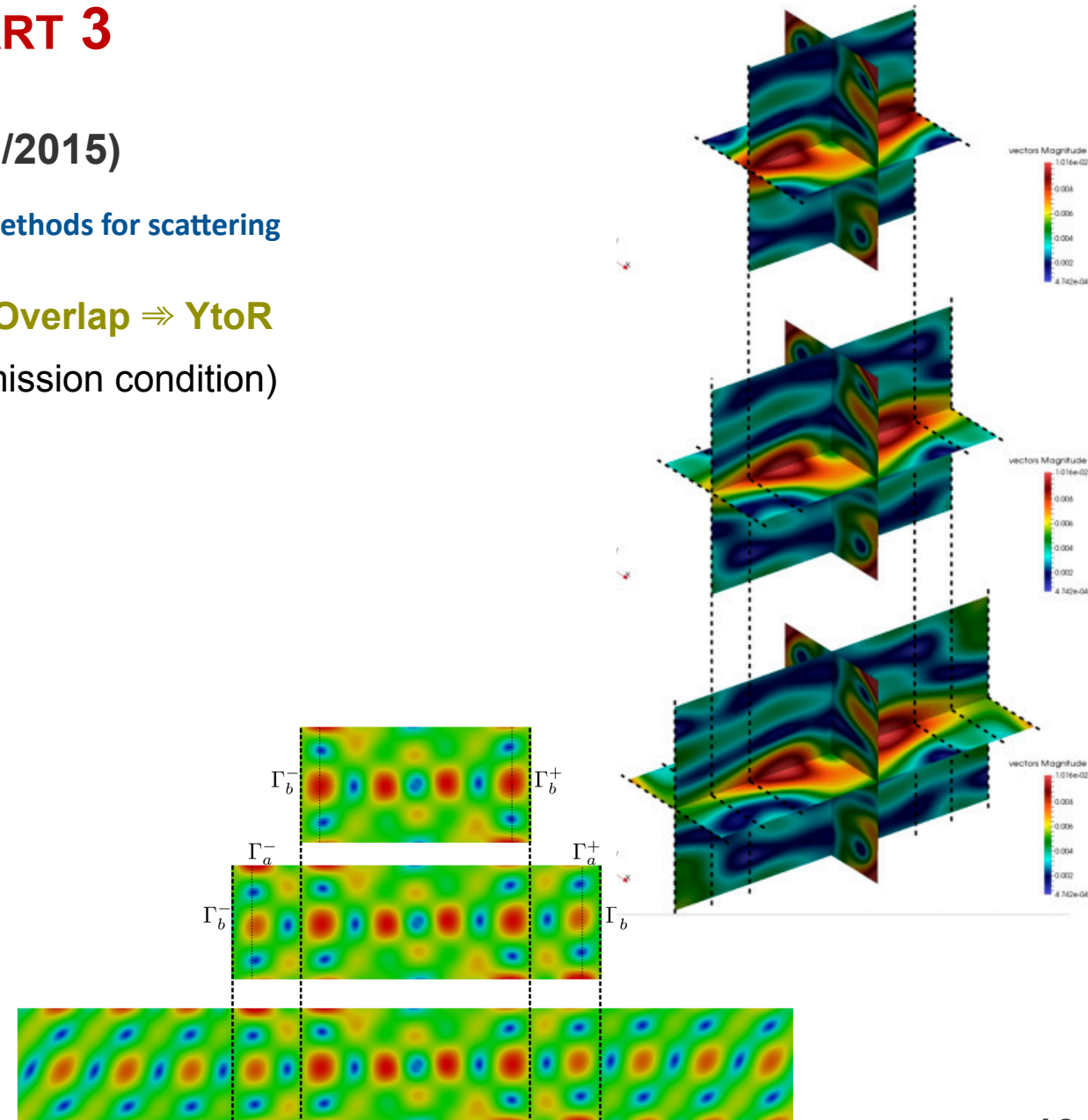
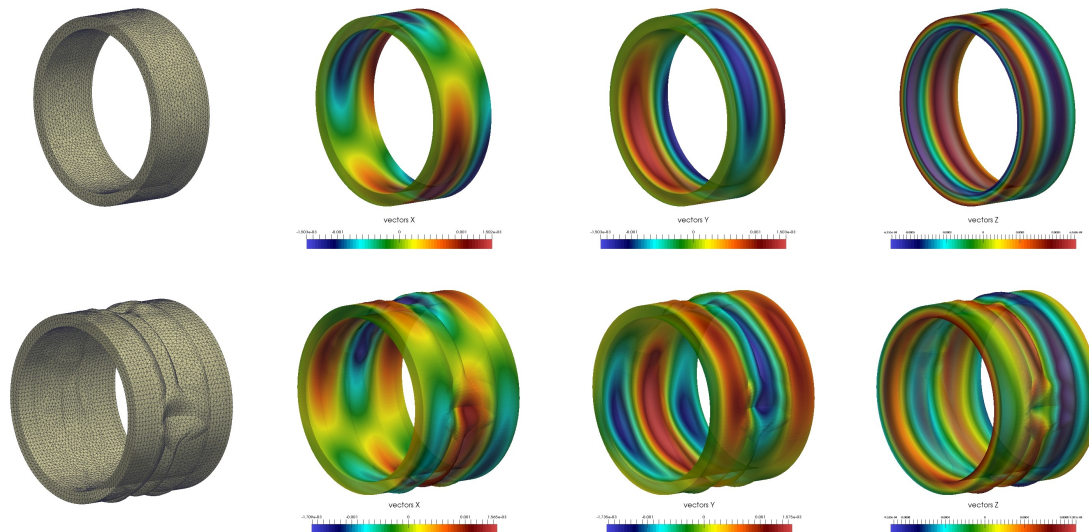


# SCATTERING IN ELASTIC WAVEGUIDE : PART 3

## New TBC in elastic waveguide (A. Tonnoir - 2011/2015)

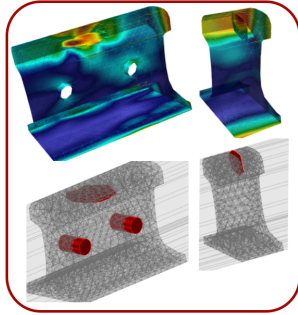
V. Baronian, A-S. Bonnet-Ben Dhia, S. Fliss and A. Tonnoir, **Iterative methods for scattering problems in unbounded anisotropic waveguides** (2016)

- ▶ Coupling FE/Modal representations, **XY formalism**, **Overlap**  $\Rightarrow$  **YtoR operator & OtoR operator** (modal « Outgoing » transmission condition)
- ▶ Iterative solver **GMRES**, reduction of memory cost
- ▶ Code : **Antoine**, **Prototype CEA**
- ▶ **Anisotropic** medium

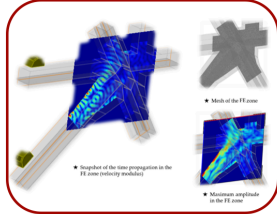


# CHRONOLOGY //

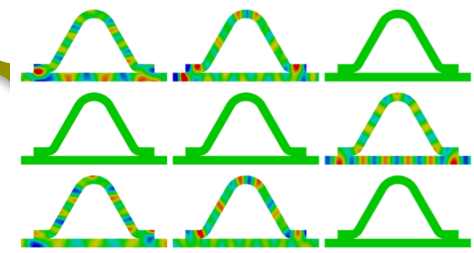
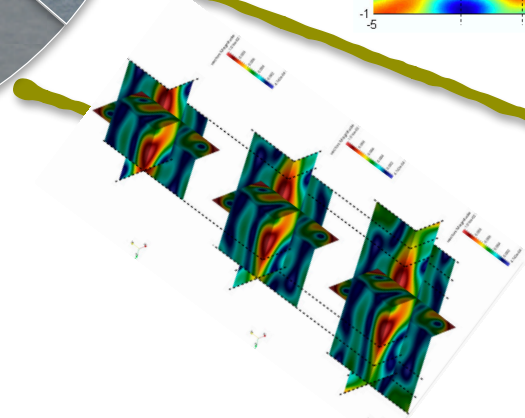
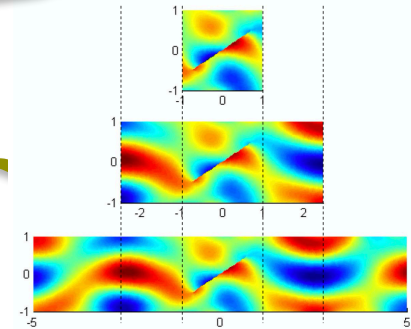
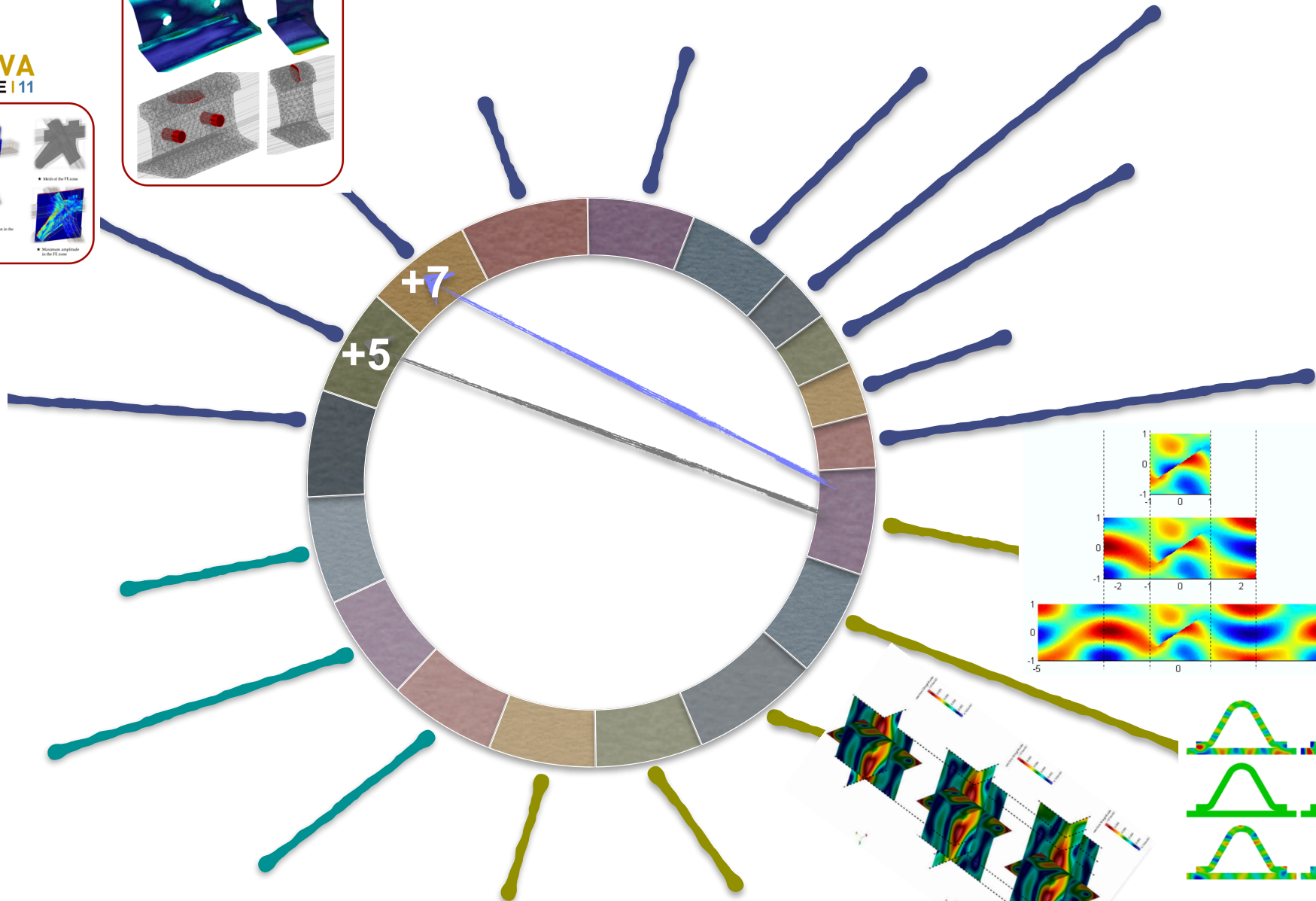
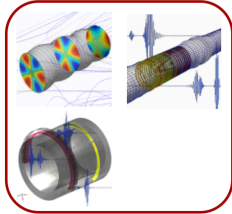
CIVA  
NDE | 2016



CIVA  
NDE | 11



CIVA  
NDE | 10.1

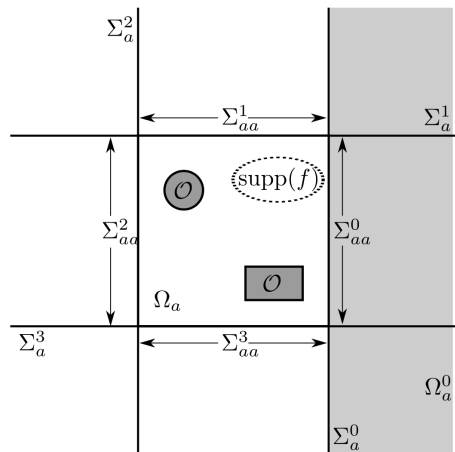


# HALF SPACE MATCHING (HSM) METHOD : PART 1

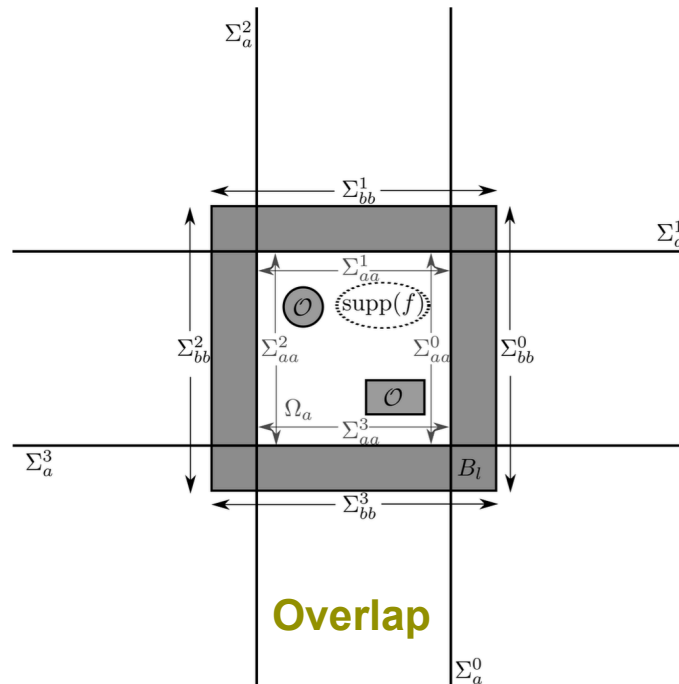
## Transparent boundary conditions for 2D acoustic/elastic media (A. Tonnoir - 2011/2015)

A-S. Bonnet-Ben Dhia, S. Fliss and A. Tonnoir, **The Halfspace Matching Method : a new method to solve scattering problem in infinite media** (2018)

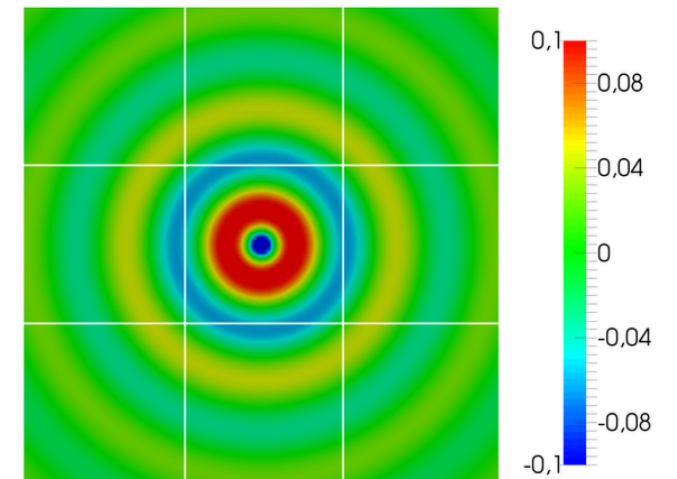
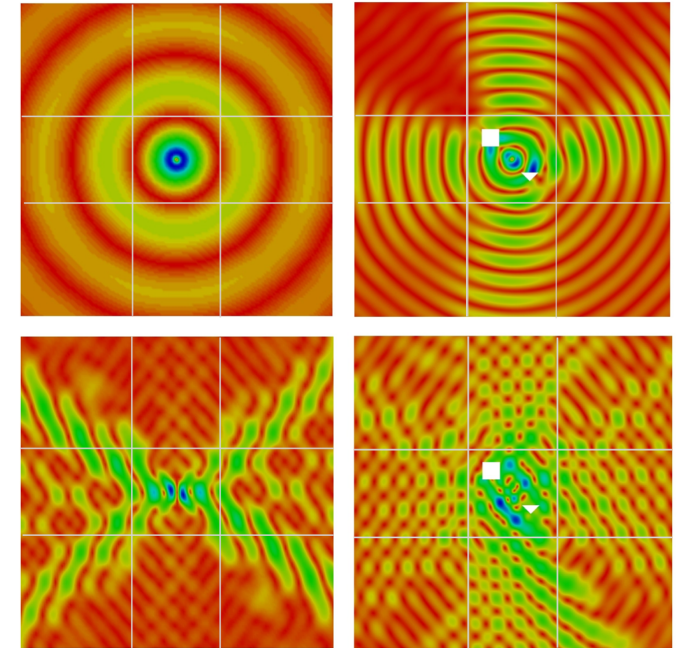
- ▶ **Geometry : 2D acoustic/elastic (no modes)**
- ▶ **Multi-domain formulation, Compatibility relations, integral operators**
- ▶ **Iterative solver GMRES**, reduction of memory cost
- ▶ **Code : Antoine**
- ▶ **Anisotropic medium**



No Overlap



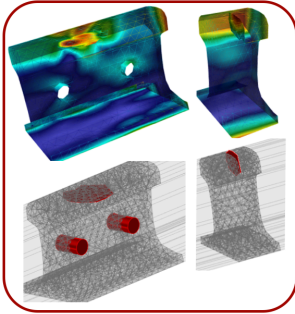
Overlap



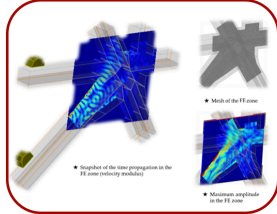


# CHRONOLOGY //

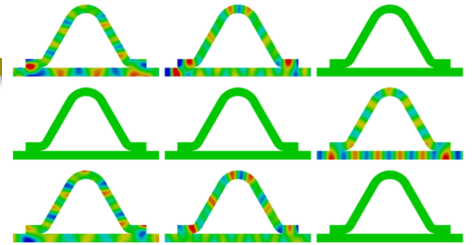
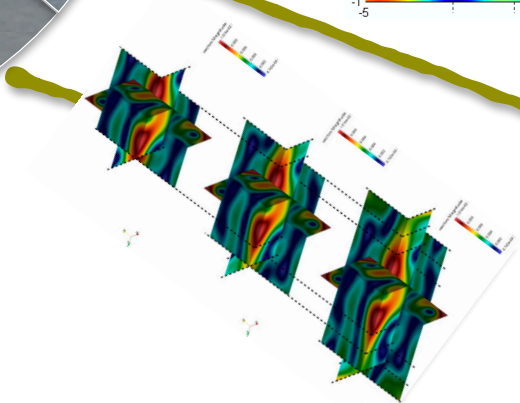
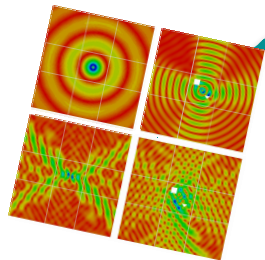
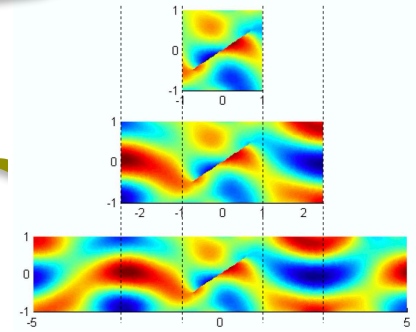
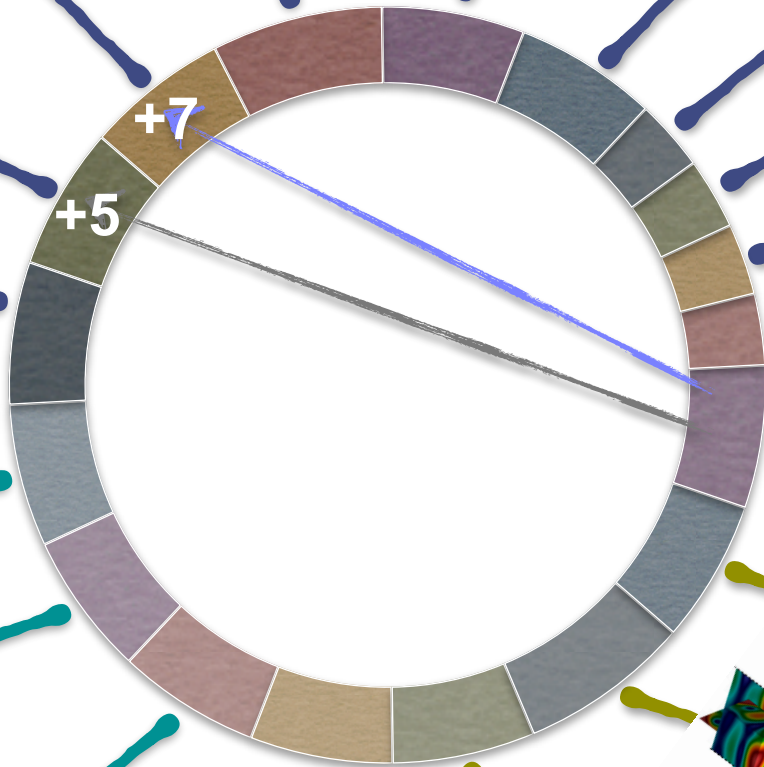
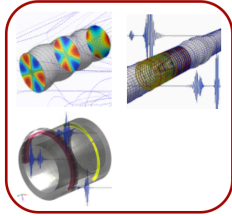
CIVA  
NDE | 2016



CIVA  
NDE | 11



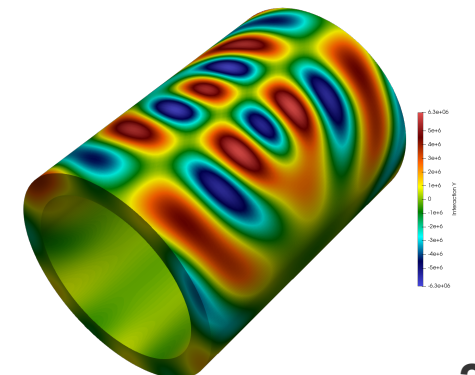
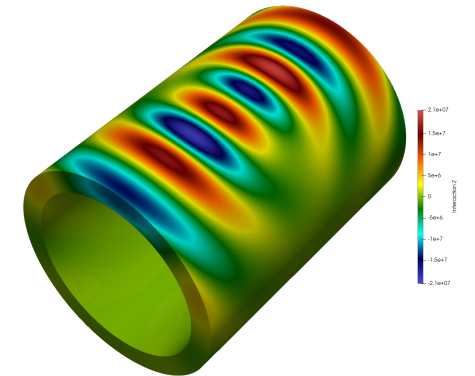
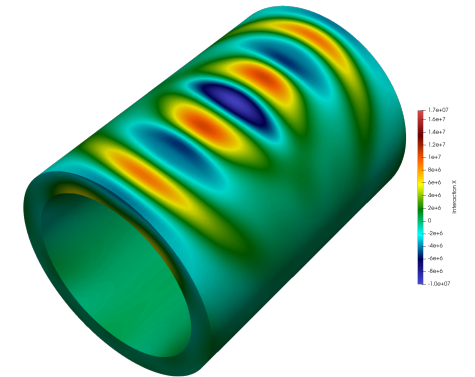
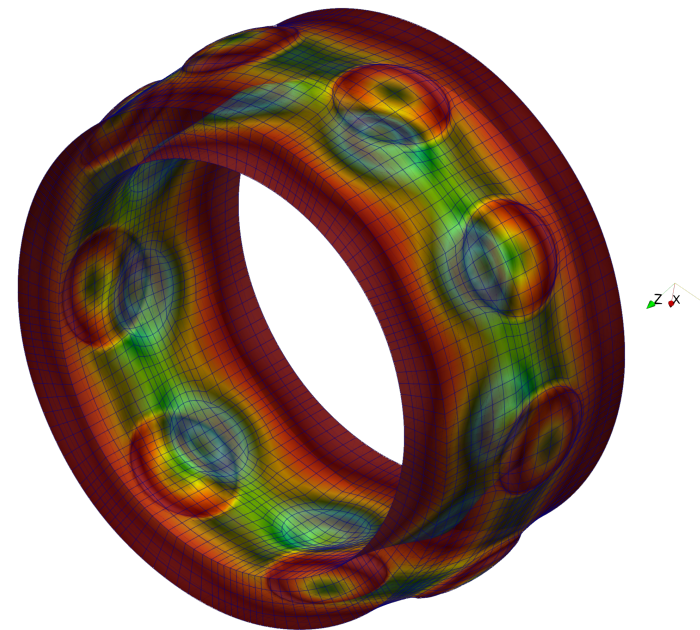
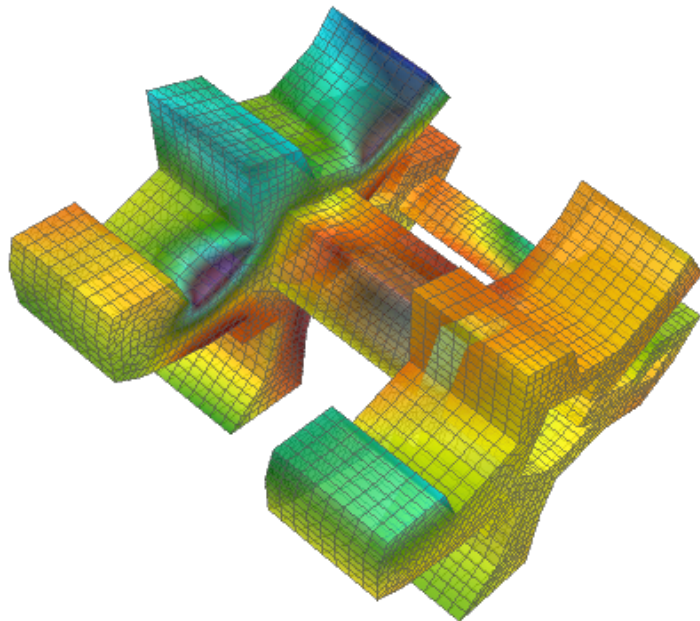
CIVA  
NDE | 10.1



# CHRONOLOGY OF CIVA : OTOR & ITERATIVE SOLVER (2020)

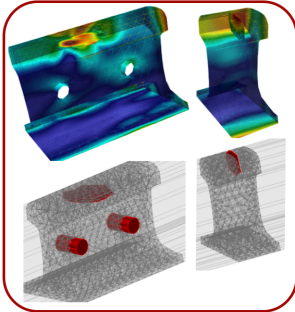
## Implementation of OtoR operator

- ▶ **Geometry** : 3D elastic waveguide
- ▶ **Flaws/Sources** : arbitrary perturbations, complex sources (EMAT, multi-arrays)
- ▶ **Overlap**  $\Rightarrow$  **YtoR operator & OtoR operator** (modal « Outgoing » transmission condition)
- ▶ **Iterative solver GMRES**, reduction of memory cost
- ▶ **Anisotropic material**

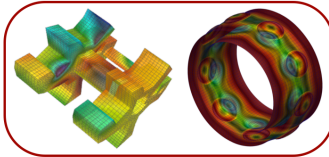


# CHRONOLOGY //

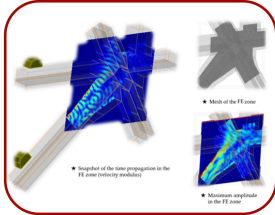
CIVA  
NDE | 2016



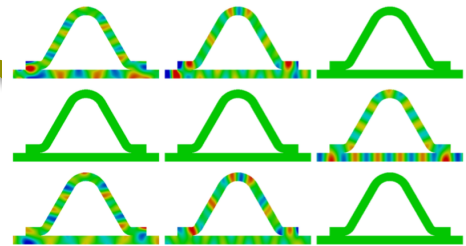
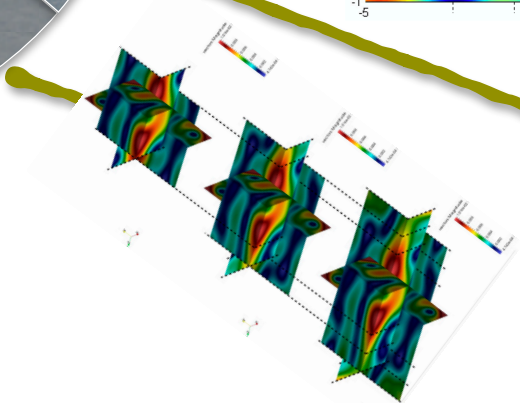
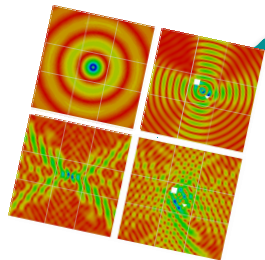
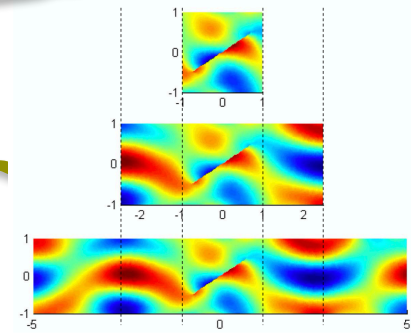
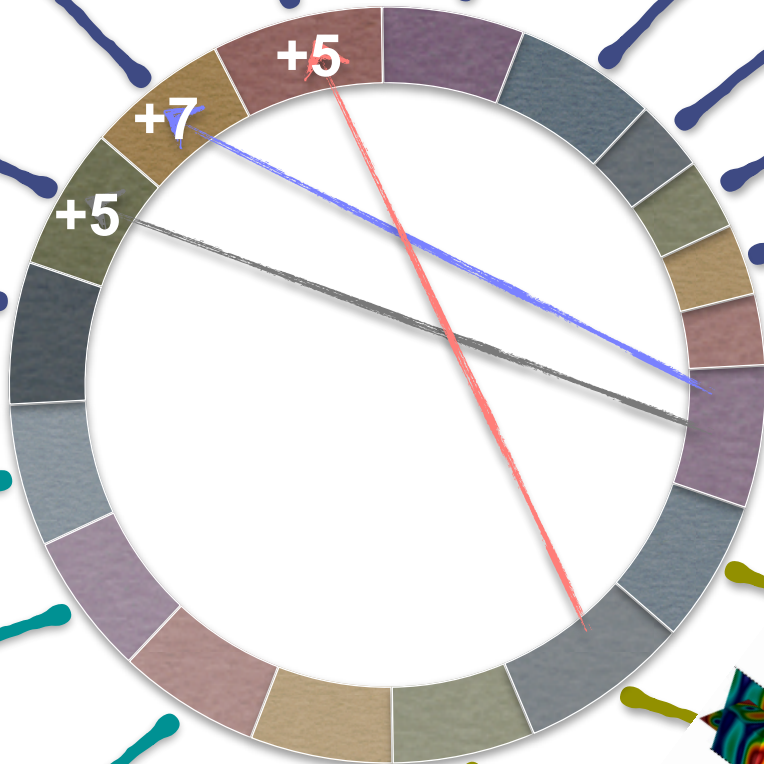
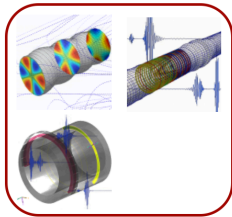
CIVA  
NDE | 2020



CIVA  
NDE | 11



CIVA  
NDE | 10.1

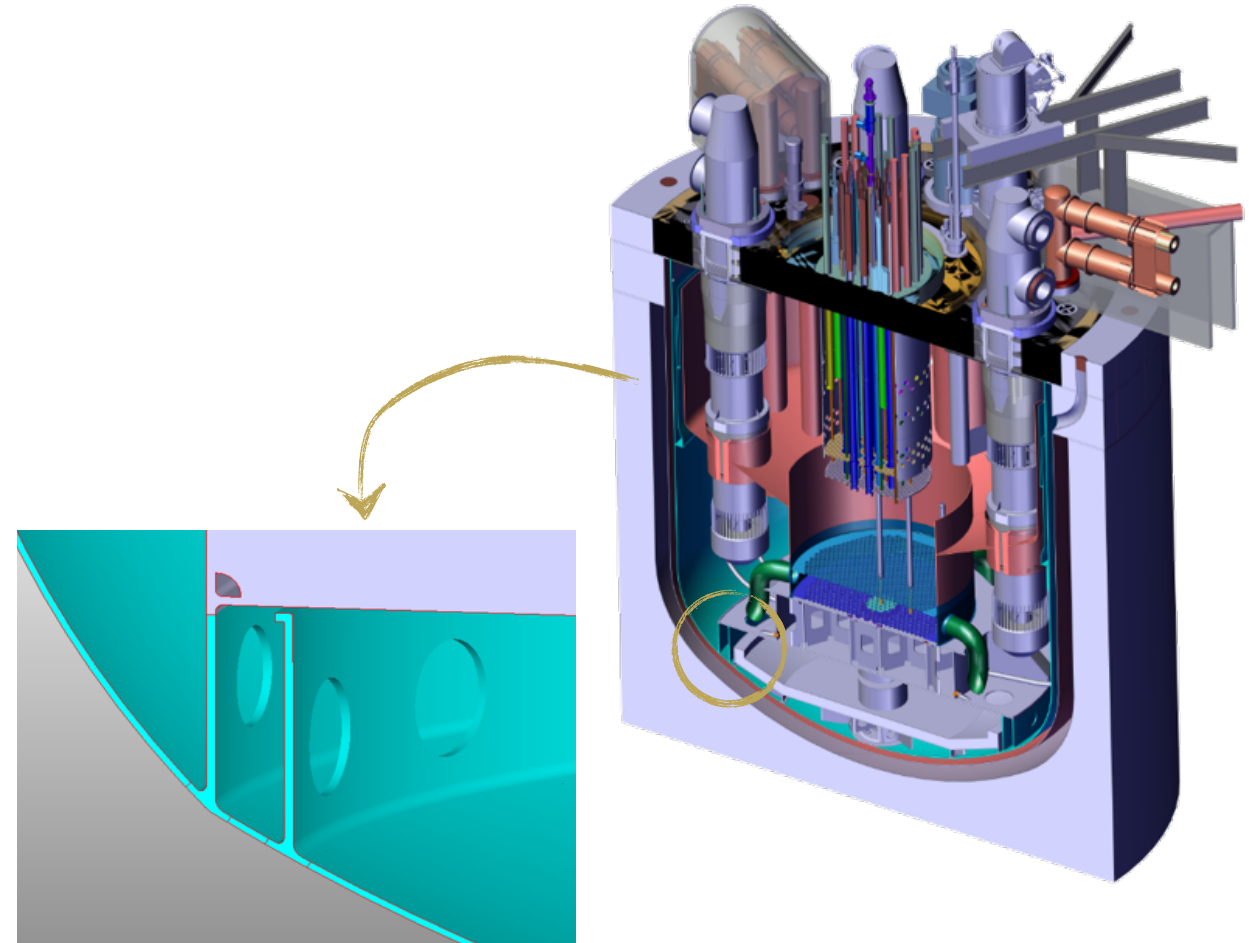
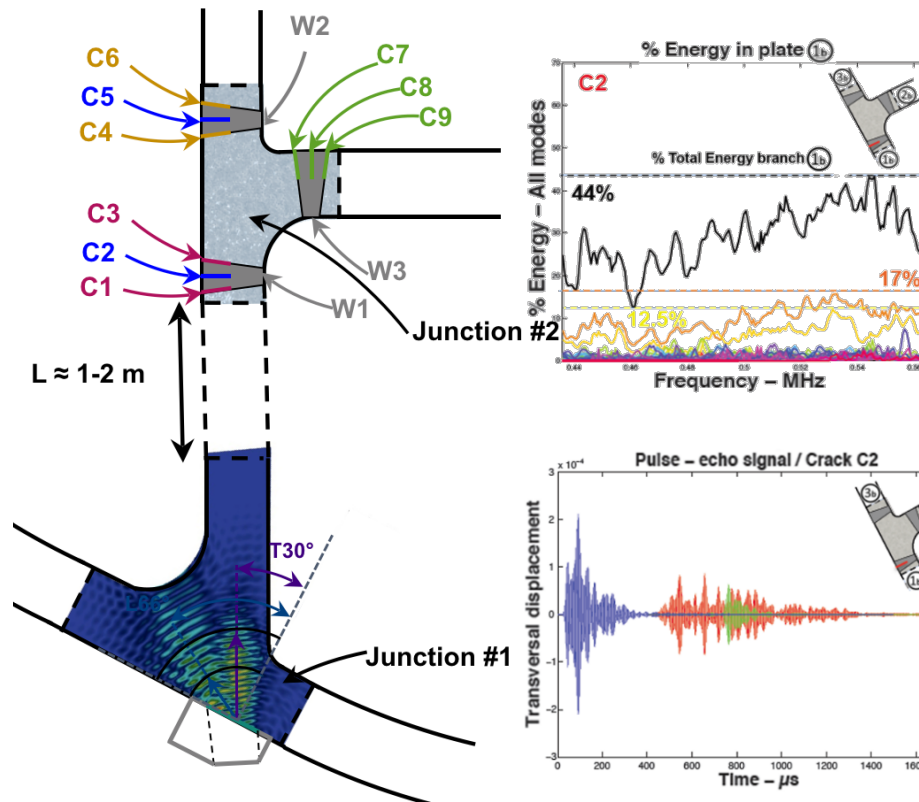




# CHRONOLOGY OF CIVA : MULTI-BOX

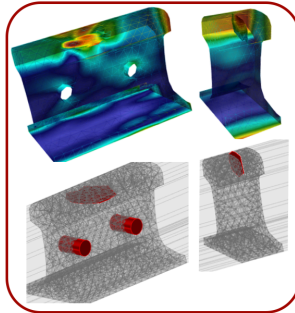
Implementation of the multi-box architecture to combine several FE/Modal box computation

- ▶ Geometry : 3D elastic waveguide
- ▶ Flaws/Sources : arbitrary perturbations,

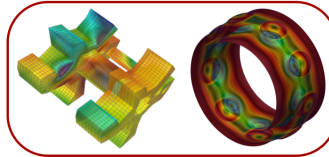


# CHRONOLOGY //

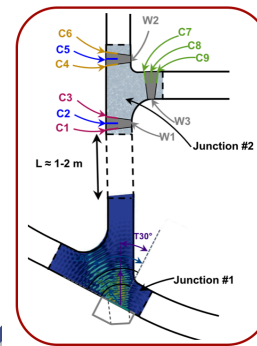
CIVA  
NDE | 2016



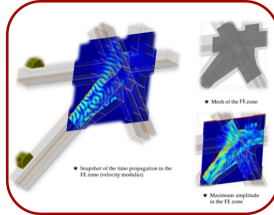
CIVA  
NDE | 2020



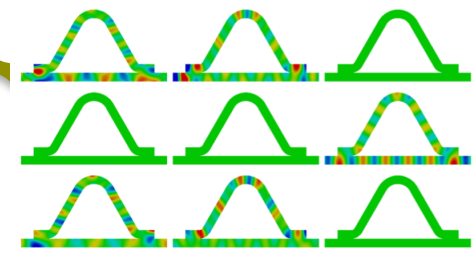
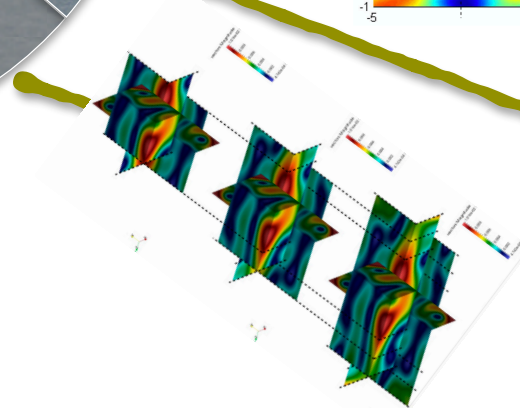
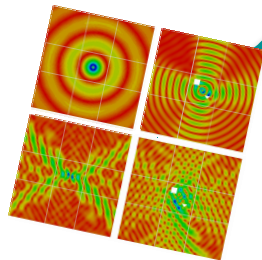
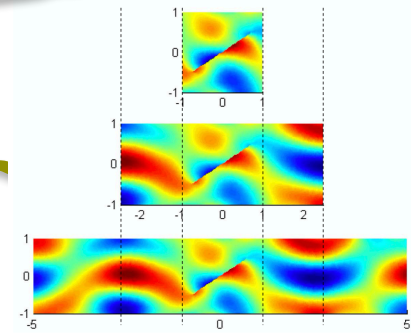
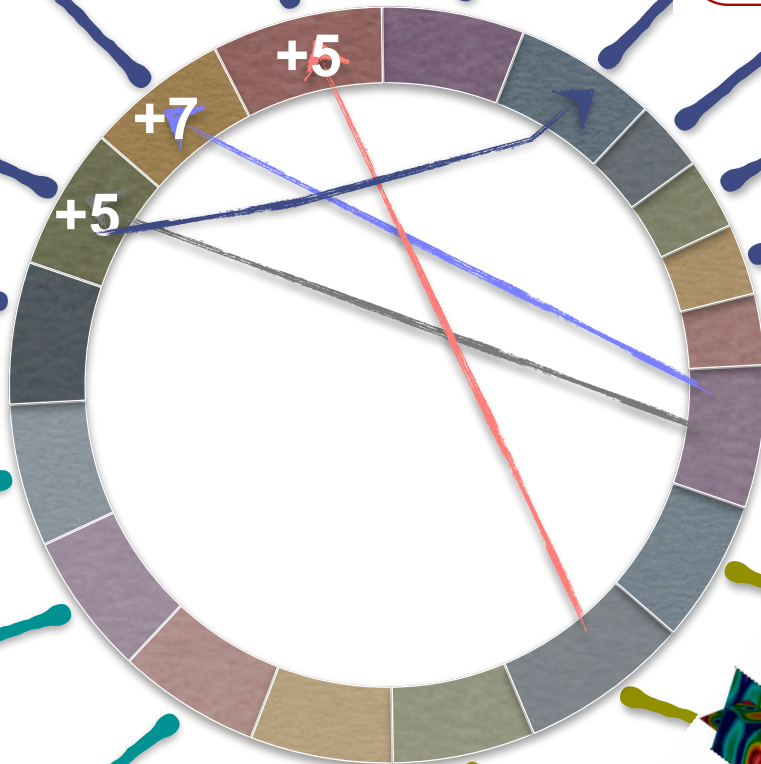
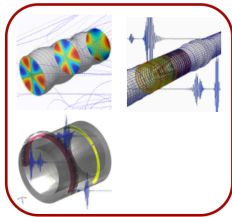
CIVA  
NDE | 2021



CIVA  
NDE | 11



CIVA  
NDE | 10.1



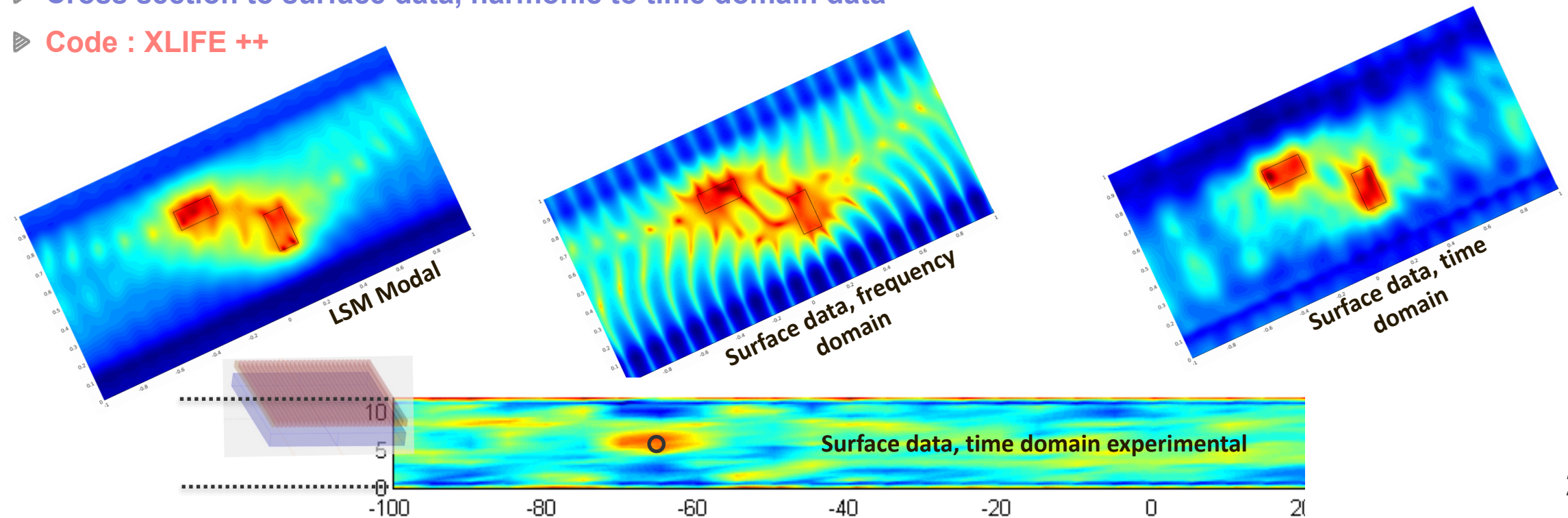


# DEFECT IMAGING IN ELASTIC WAVEGUIDE : PART 1

## Linear Sampling method for imaging defect in elastic waveguide (A. Recoquillay - 2015/2018)

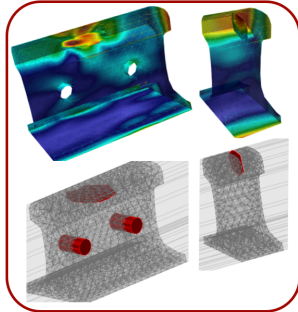
L. Bourgeois, B. Chapuis, A. Recoquillay, V. Baronian, [Linear Sampling Method applied to Non Destructive Testing of an elastic waveguide : theory, numerics and experiments](#) (2018)

- ▶ **Geometry : 2D/3D elastic waveguide**
- ▶ **Flaws : cracks and surface/core defect type**
- ▶ **YX formalism  $\Rightarrow$  YtoX operator** to get the scattering matrix coefficients (direct problem)
- ▶ **Cross section to surface data, harmonic to time domain data**
- ▶ **Code : XLIFE ++**

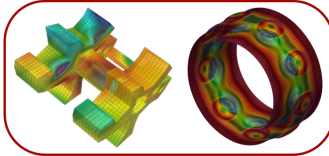


# CHRONOLOGY //

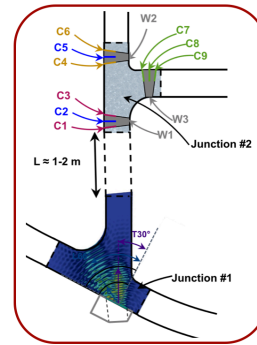
CIVA  
NDE | 2016



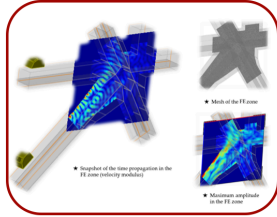
CIVA  
NDE | 2020



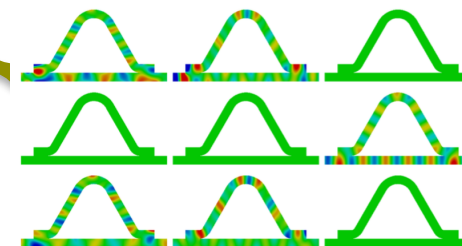
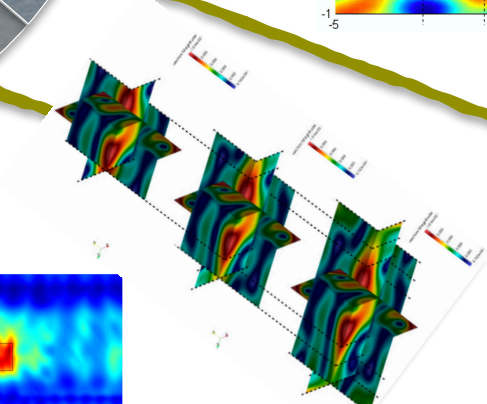
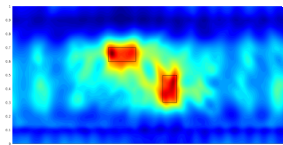
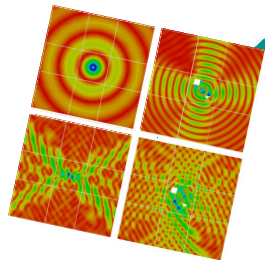
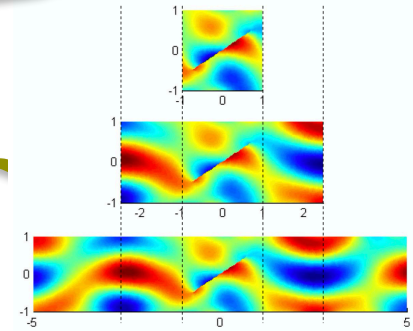
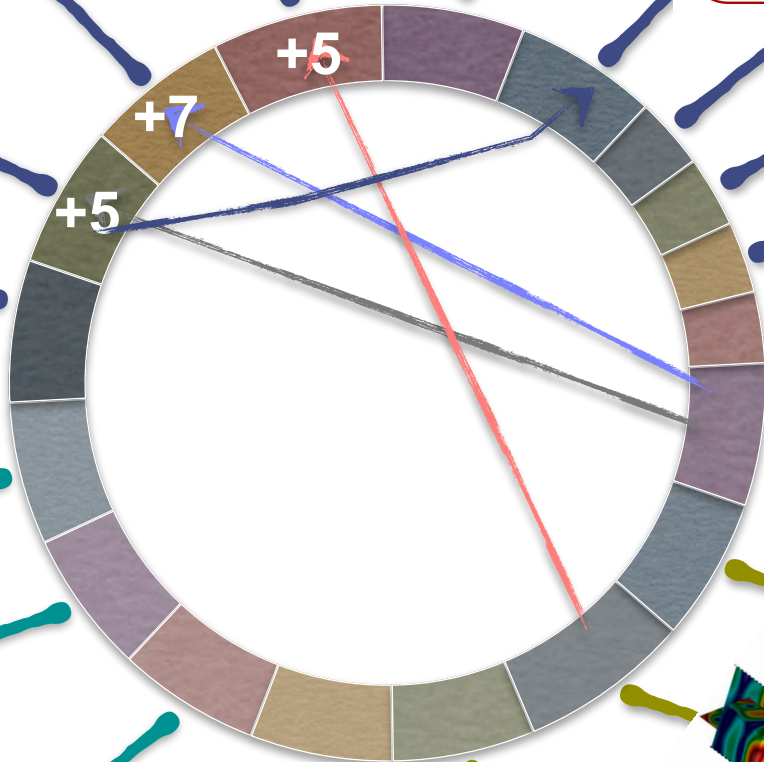
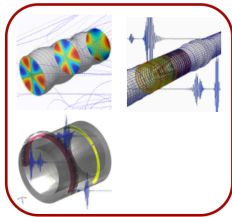
CIVA  
NDE | 2021



CIVA  
NDE | 11



CIVA  
NDE | 10.1



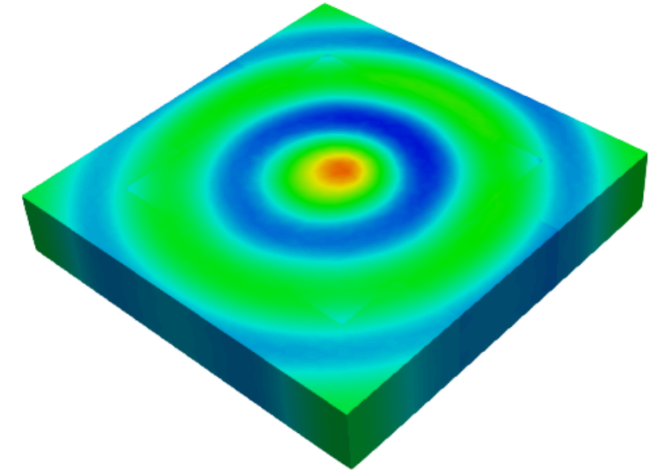
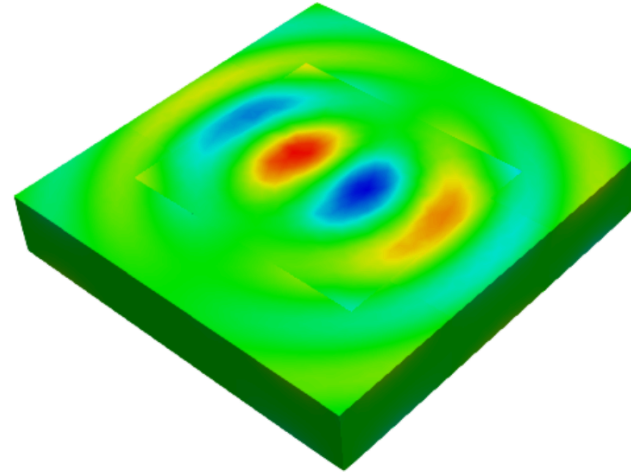
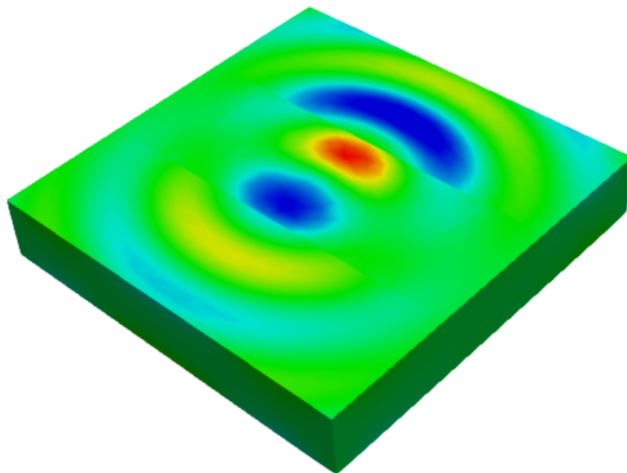
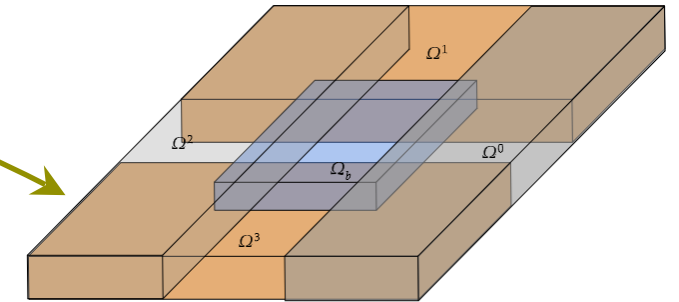
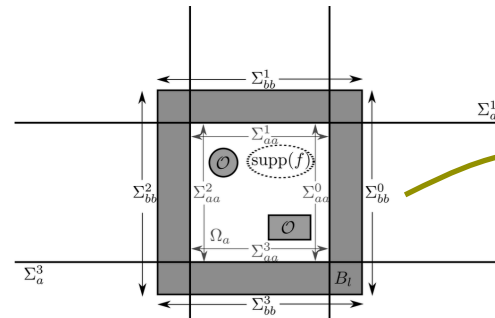
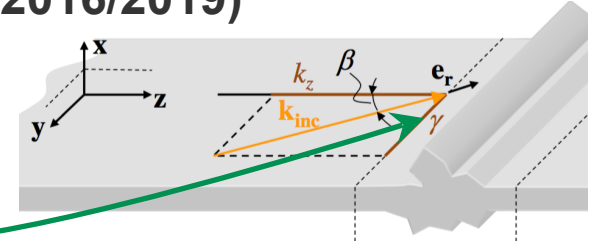
# HALF SPACE MATCHING (HSM) METHOD : PART 2

## Transparent boundary conditions for 3D elastic plate (Y. Tjandrawidjaja - 2016/2019)

Y. Tjandrawidjaja, *Some contributions to the analysis of the Half-Space Matching Method for scattering problems and extension to 3D elastic plates* (2019)

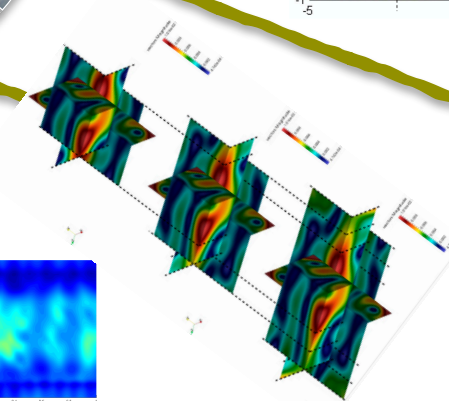
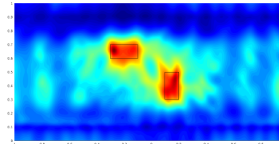
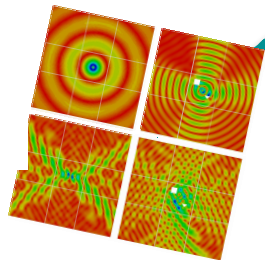
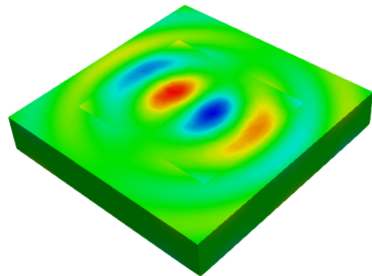
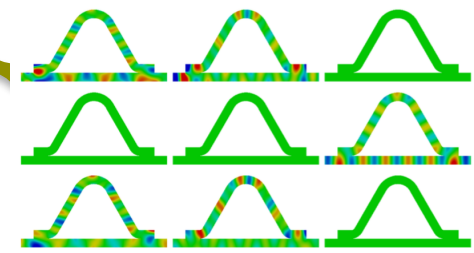
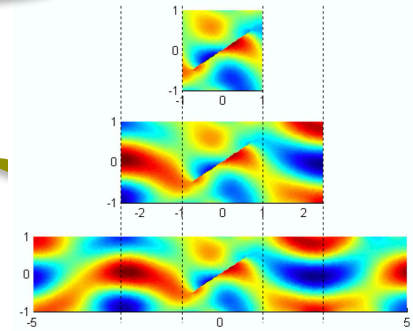
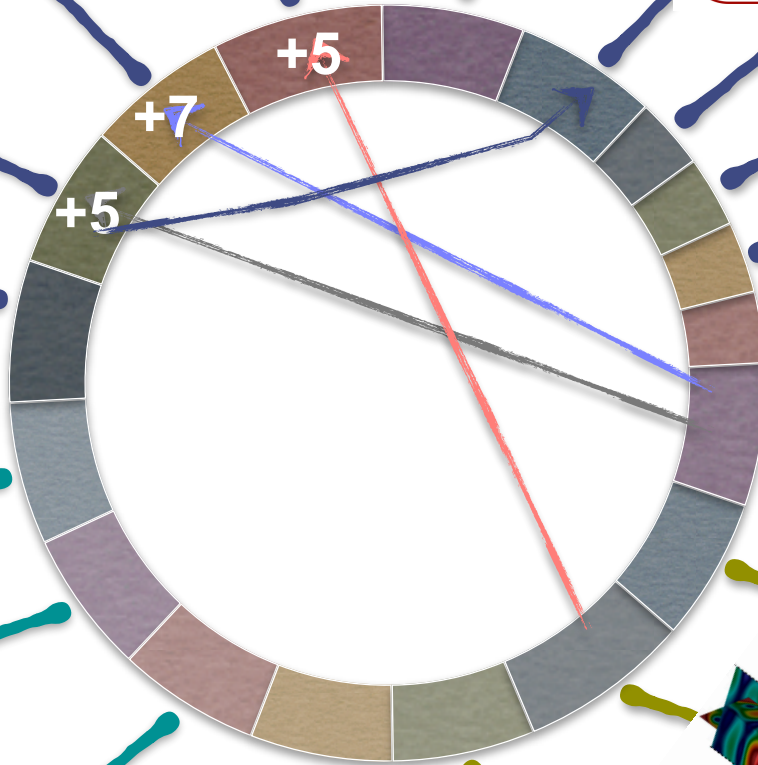
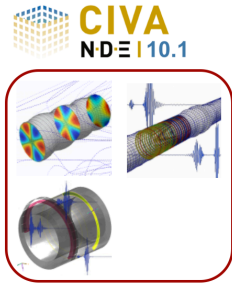
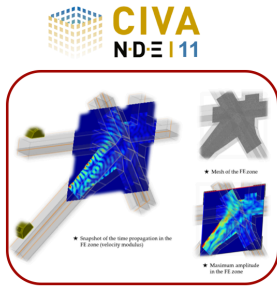
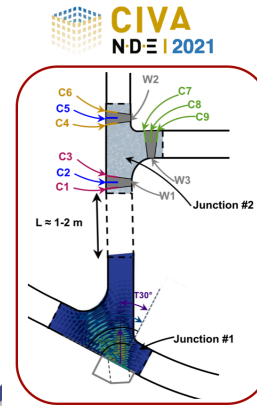
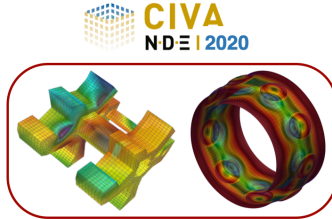
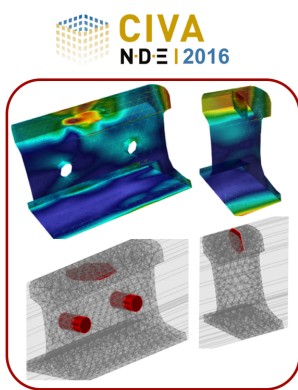
- ▶ **Geometry : 3D elastic plate (modes are back :  $\xi$  modes)**
- ▶ **Multi-domain & Multi-trace formulations, Compatibility relations, integral operators, Fourier transform,  $\xi$  modes (bi-orthonality)**

- ▶ **Direct solver**, high memory cost
- ▶ **Code : XLIFE++**
- ▶ **Anisotropic medium**





# CHRONOLOGY //



## Implementation of a mixed formulation for coupled Fluid/Structure waveguide

- ▶ **Geometry : 2D cartesian and axisymmetric specimens**
- ▶ **Numerical methods : SAFE-PML method**
- ▶ **Isotropic material**

### ▶ Equation in fluid medium

$$\Delta\Phi + \frac{\omega^2}{c_f^2}\Phi = 0 \quad \text{dans } \Omega_f,$$

$$p = -\rho_f \frac{\partial\Phi}{\partial t} = -i\omega\rho_f\Phi \quad \text{et} \quad \mathbf{v} = i\omega\mathbf{u}.$$

### ▶ Equation in solid medium

$$-\text{div } \sigma(\mathbf{u}) - \omega^2\rho_s\mathbf{u} = 0 \quad \text{dans } \Omega_s = S \times \mathbb{R},$$

### ▶ Continuity relation

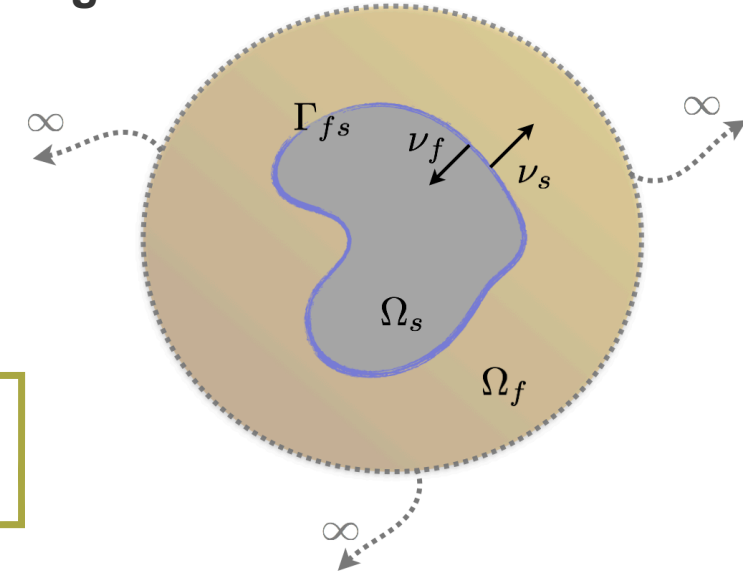
$$\begin{cases} \sigma(\mathbf{u}) \cdot \nu_s = -p\nu_s & \text{sur } \Gamma_{fs}, \\ \mathbf{v} \cdot \nu_s = \nabla\Phi \cdot \nu_s & \text{sur } \Gamma_{fs}, \end{cases}$$

### ▶ Mixed Variational formulation

$$\begin{cases} \int_{\Omega_s} \sigma(\mathbf{u}) : \varepsilon(\tilde{\mathbf{u}}) - \int_{\Omega_s} \rho_s \omega^2 \mathbf{u} \tilde{\mathbf{u}} - \int_{\Gamma_{fs}} i\omega\rho_f(\tilde{\mathbf{u}} \cdot \nu_s)\Phi = 0 \\ \int_{\Omega_f} \rho_f \nabla\Phi \nabla\tilde{\Phi} - \int_{\Omega_f} \rho_f \frac{\omega^2}{c_f^2} \Phi \tilde{\Phi} - \int_{\Gamma_{fs}} i\omega\rho_f(\mathbf{u} \cdot \nu_f)\tilde{\Phi} = 0 \end{cases}$$

### ▶ Modes expression

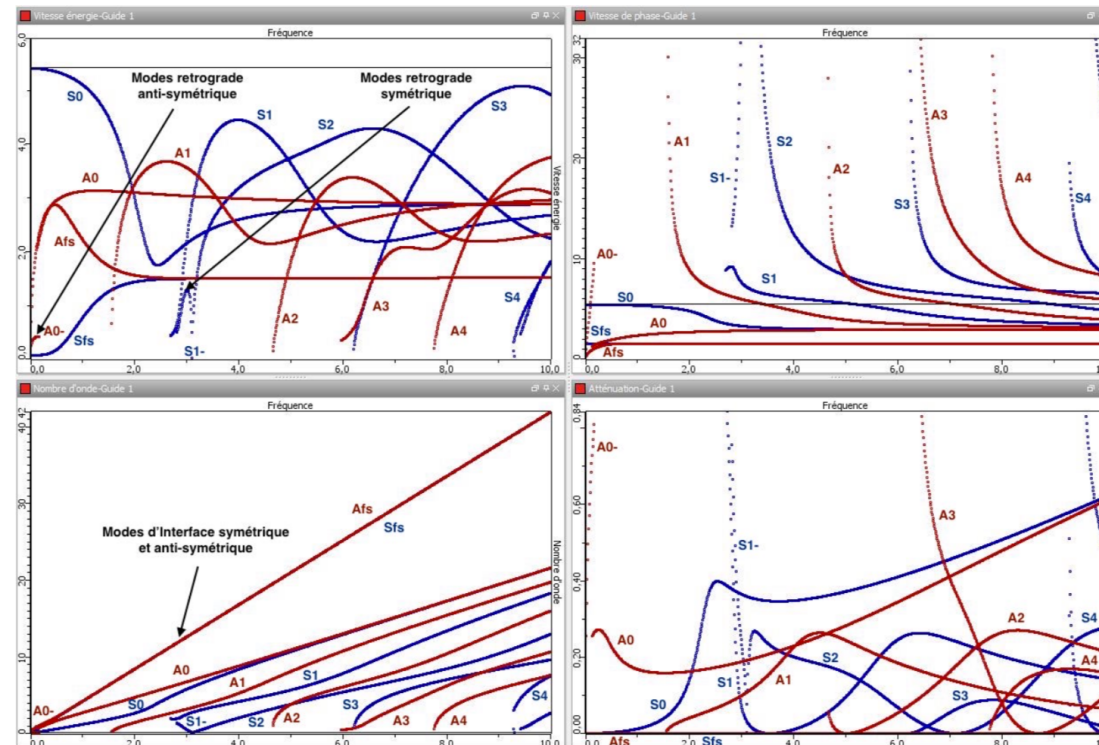
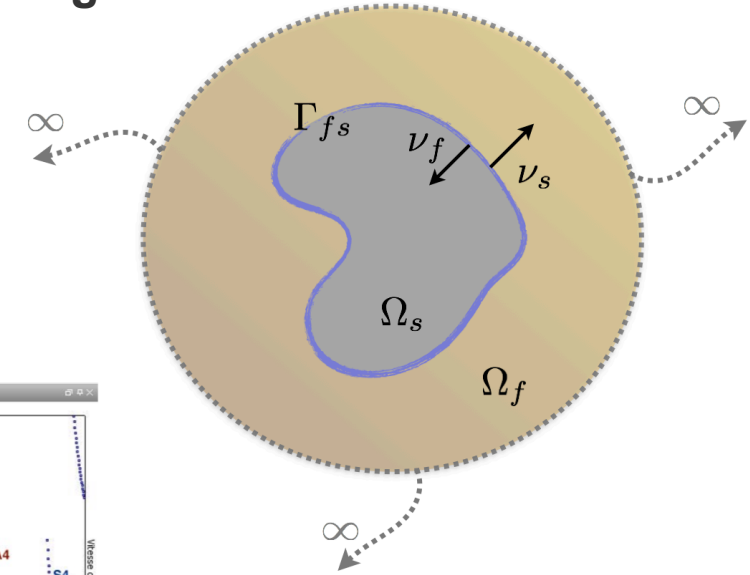
$$\begin{pmatrix} \mathbf{u}(\mathbf{x}_s, z) \\ \Phi(\mathbf{x}_s, z) \end{pmatrix} = \begin{pmatrix} \mathbf{u}(\mathbf{x}_s) \\ \Phi(\mathbf{x}_s) \end{pmatrix} e^{-i\beta z},$$



# CHRONOLOGY OF CIVA : MODES IN SUBMERGED WAVEGUIDE (2020)

Implementation of a mixed formulation for coupled Fluid/Structure waveguide

- ▶ **Geometry** : 2D cartesian and axisymmetric specimens
- ▶ **Numerical methods** : SAFE-PML method
- ▶ **Isotropic material**
- ▶ **Difficulty** : wrong approximation Scholte and Q-Scholte modes with PML



# CHRONOLOGY OF CIVA : BOUNDED FLUID/STRUCTURE WAVEGUIDE (2021/2024)

- D2 = TDF ext
- D3 = FPS int
- D4 = FPS ext
- Ldg = lame de gaz

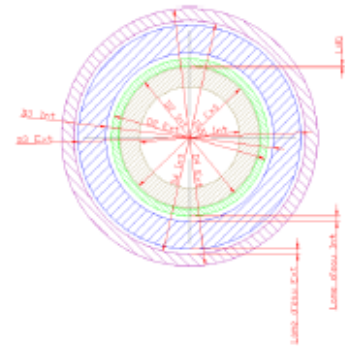
Section C-C = *TDFi Partie basse – PFM*

Section D-D = *TDFi Partie basse*

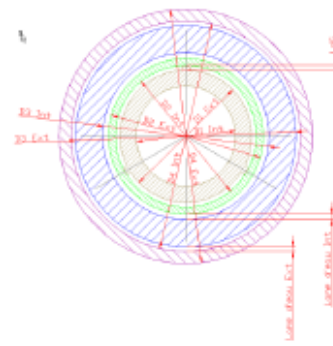
Section F-F = *TDFi Partie Haute*

Section G-G = *TDFi Partie Supérieure*

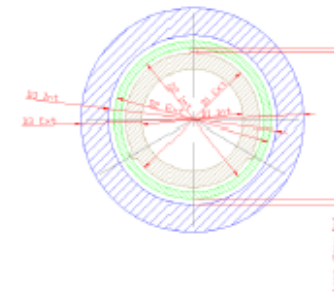
SECTION C - C (Plan de flux moyen)



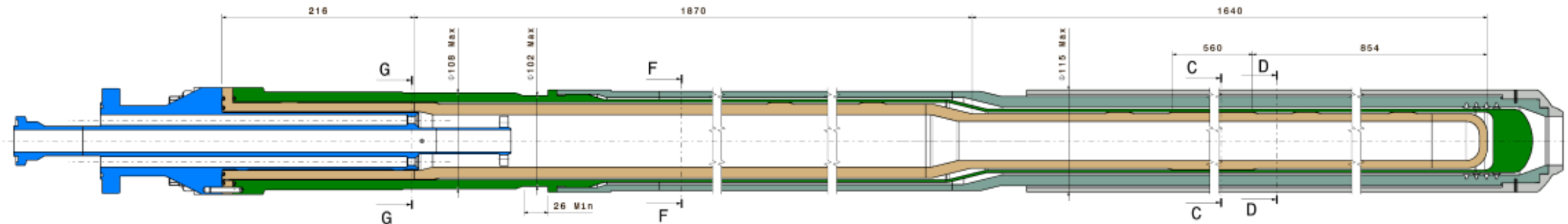
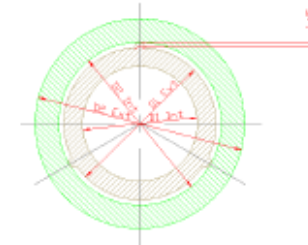
SECTION D - D



SECTION F - F



SECTION G - G



# CHRONOLOGY OF CIVA : BOUNDED FLUID/STRUCTURE WAVEGUIDE (2021/2024)

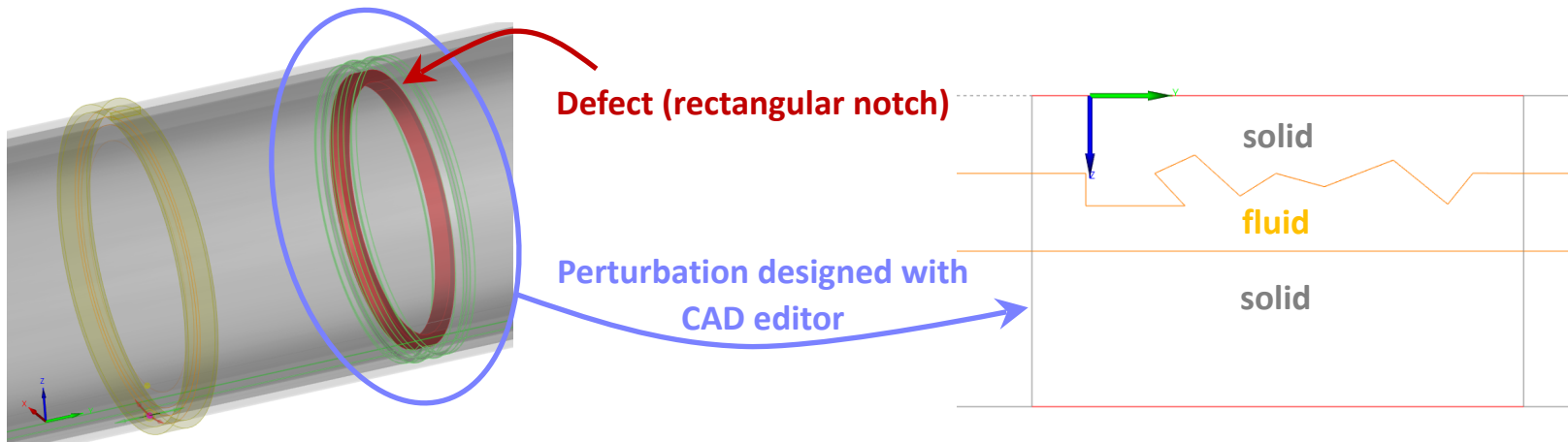
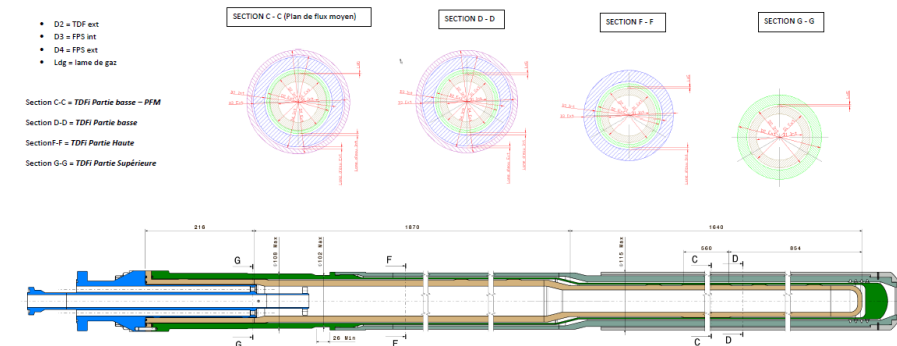
## Implementation of YtoX method for coupled F/S waveguide

- ▶ **Geometry** : 2D cartesian and axisymmetric specimens for modes interaction
- ▶ **Flaws** : arbitrary perturbations/interface irregularity
- ▶ **Extension of XY formalism** (valid for **elastic** and **acoustic** waveguide)

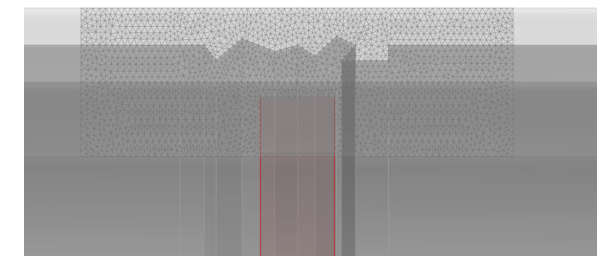
V. Pagneux, A. Maurel, **Scattering matrix properties with evanescent modes for waveguides in fluids and solids** (2004)

...to coupled F/S with bounded cross section

- ▶ **Fraser's bi-orthogonality still valid** :  $(X_{sf}, Y_{sf}) = (X_s, Y_s) + (X_f, Y_f)$

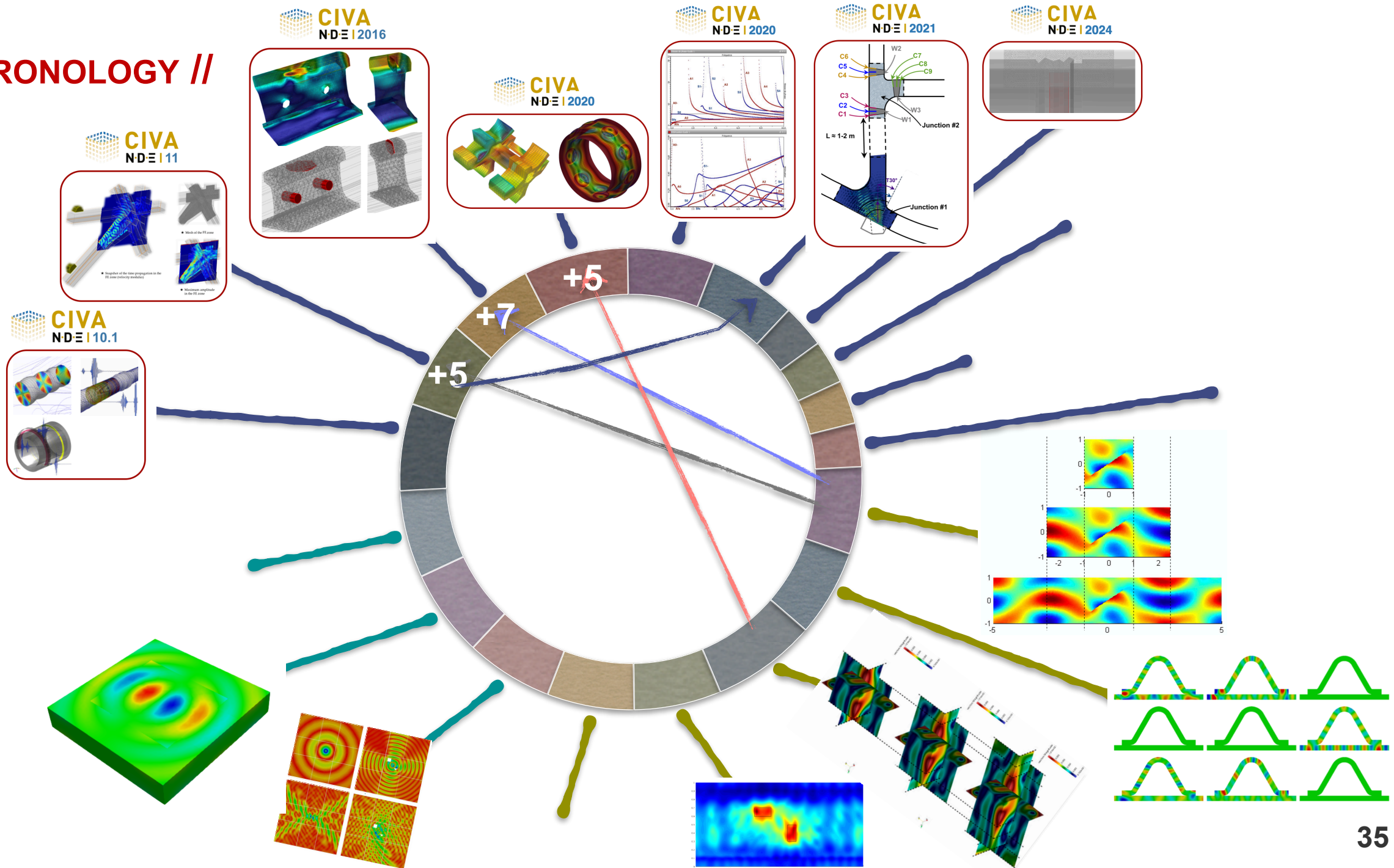


Mesh of the computational domain





# CHRONOLOGY //

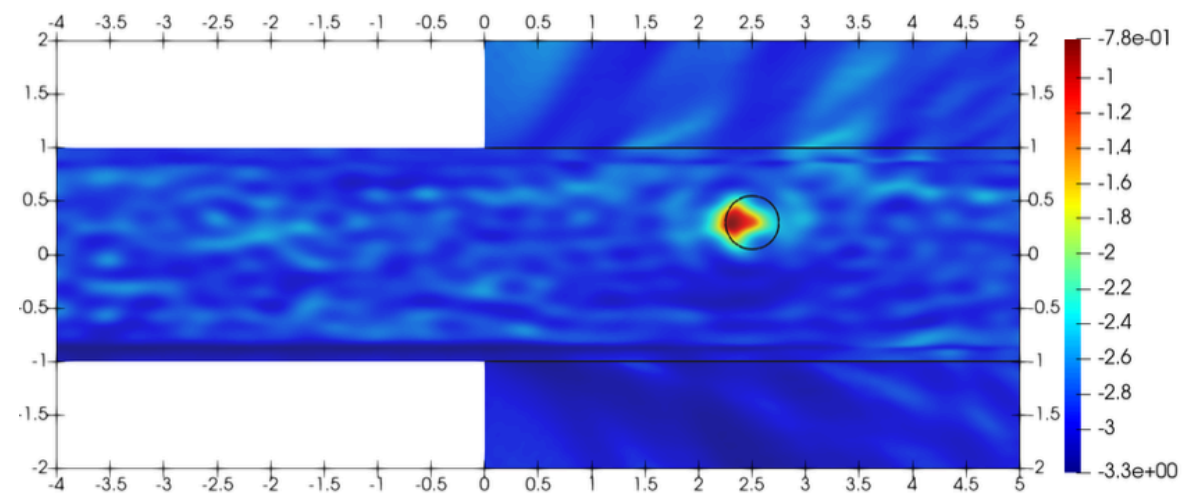
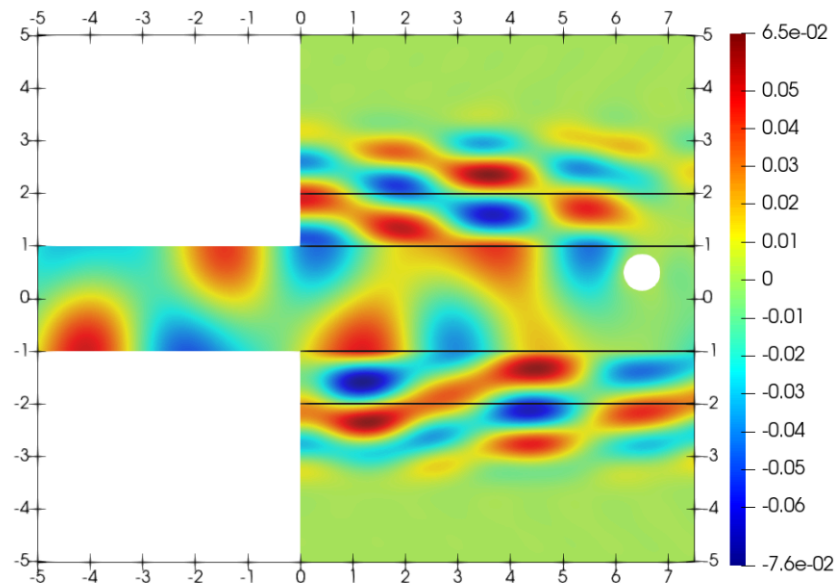


# DEFECT IMAGING IN ELASTIC WAVEGUIDE : PART 2

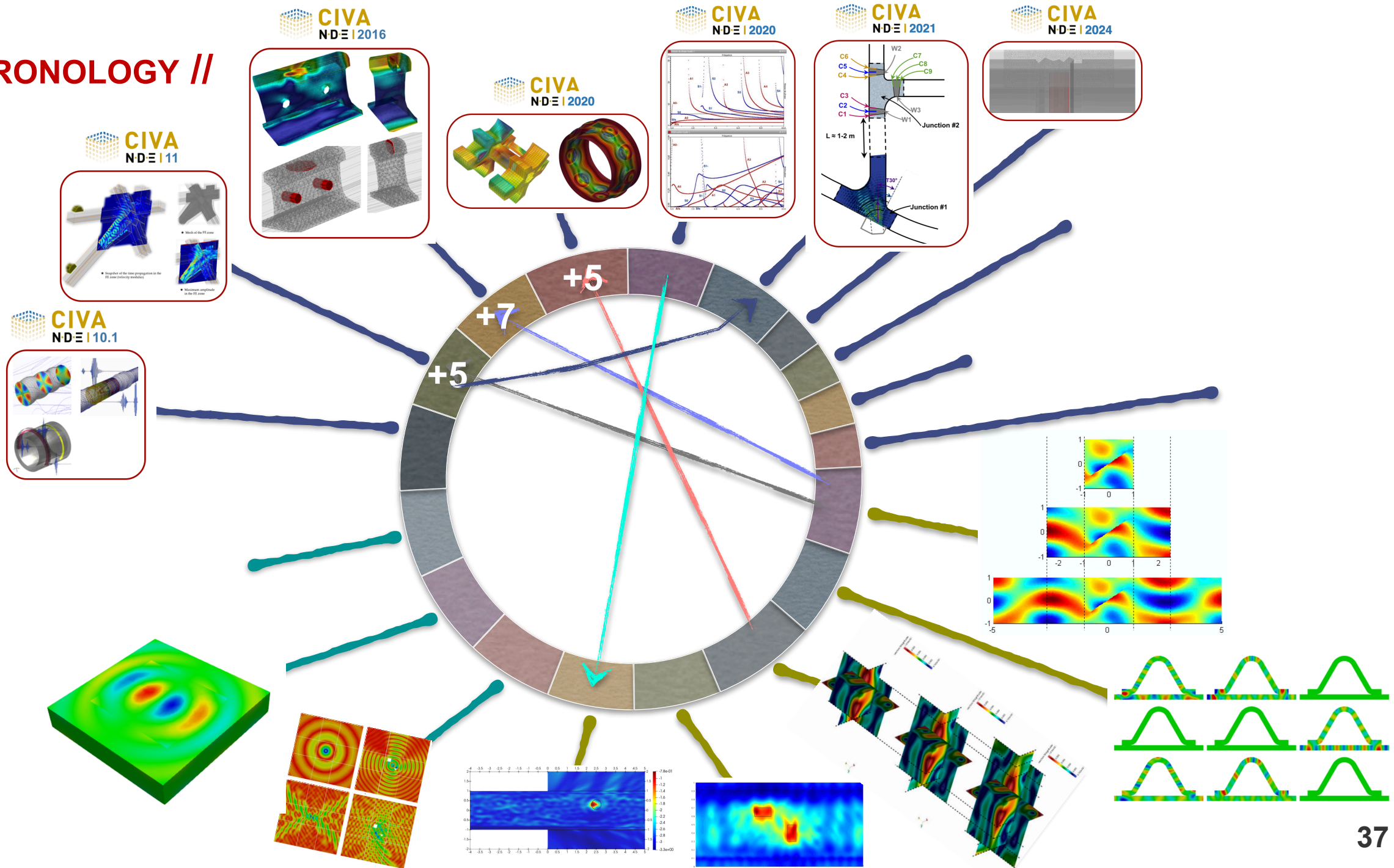
## Linear Sampling method for imaging partially submerged elastic waveguide (J-F. Fritsch - 2019/2023)

J. F. Fritsch, *Propagation des ondes dans les guides partiellement enfouis : résolution du problème direct et imagerie par méthode de type échantillonnage* (2023)

- ▶ **Geometry : 2D/3D elastic waveguide**
- ▶ **Flaws : surface/core defect type in solid part**
- ▶ **XY formalism for submerged waveguide**  $\Rightarrow$  **YtoX operator with PML**, direct and inverse scattering problem
- ▶ **Cross section to surface data, harmonic data**
- ▶ **Code : XLIFE ++**



# CHRONOLOGY //

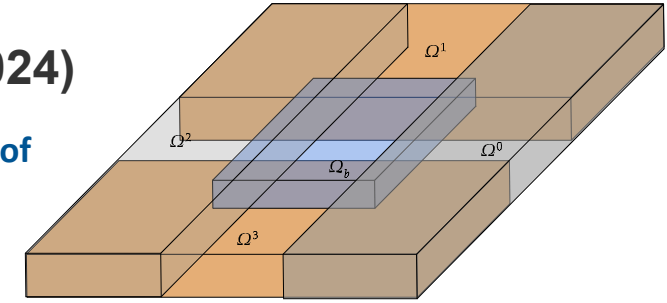




# HALF SPACE MATCHING (HSM) METHOD : PART 3

## Transparent boundary conditions for 3D elastic plate (A. Allouko 2020/2024)

A. Allouko, Hybrid modal - finite elements modeling for ultrasonic testing of an elastic plate. Treatment of oscillating integrals of the HSM method (2024)

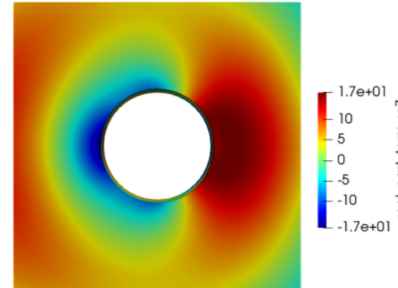


- ▶ **Geometry : 3D elastic plate (modes are back :  $\xi$  modes)**
- ▶ **Multi-domain & Multi-trace formulations, Compatibility relations, integral operators,  $\xi$  modes,**  
Fourier transform

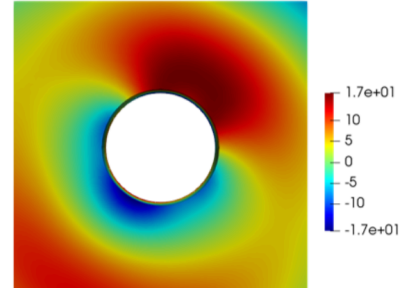
- ▶ **Direct solver,** high memory cost

- ▶ **Code : XLIFE++**

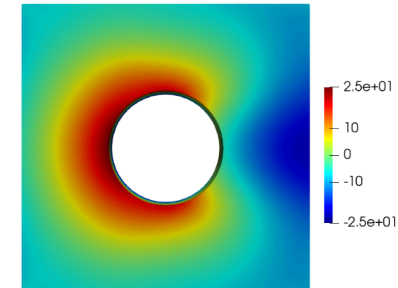
- ▶ **Anisotropic medium**



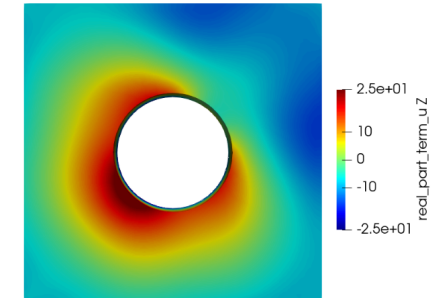
(a)  $\theta = 0^\circ$



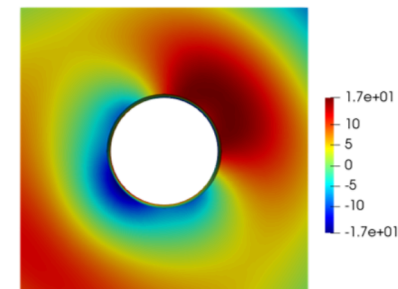
(b)  $\theta = 40^\circ$



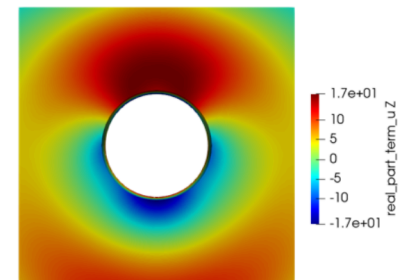
(a)  $\theta = 0^\circ$



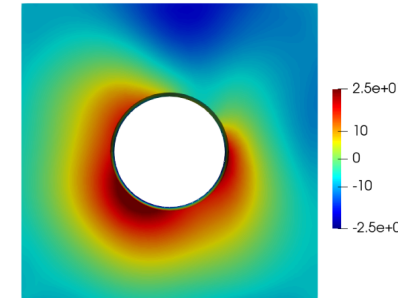
(b)  $\theta = 40^\circ$



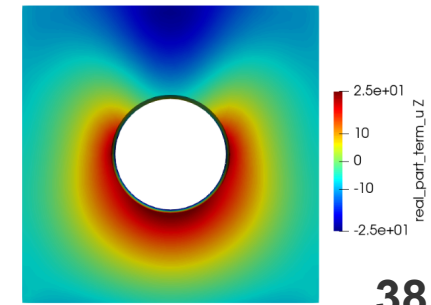
(b)  $\theta = 60^\circ$



(c)  $\theta = 90^\circ$

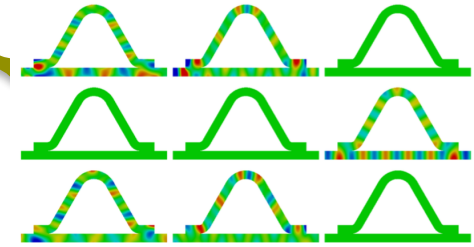
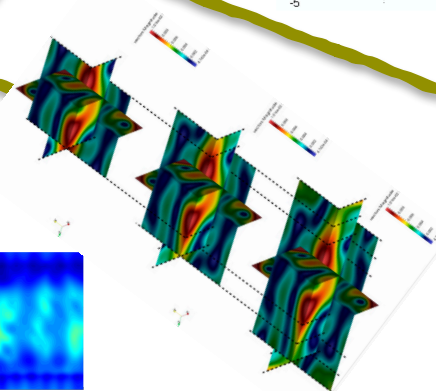
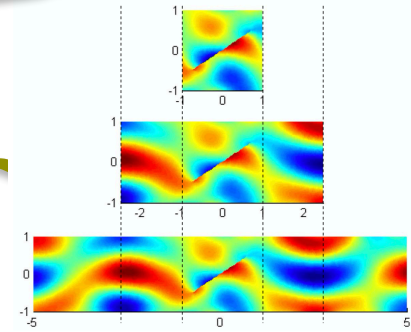
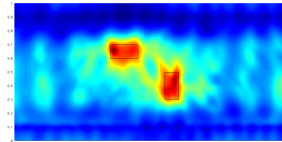
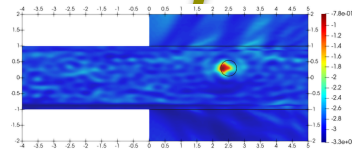
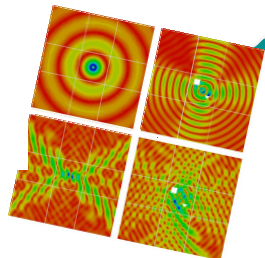
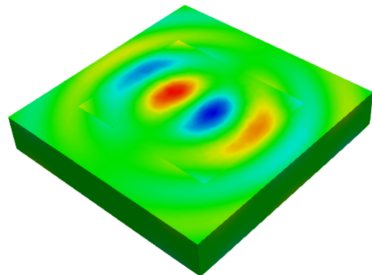
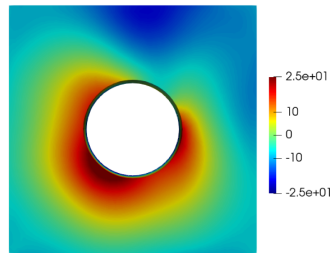
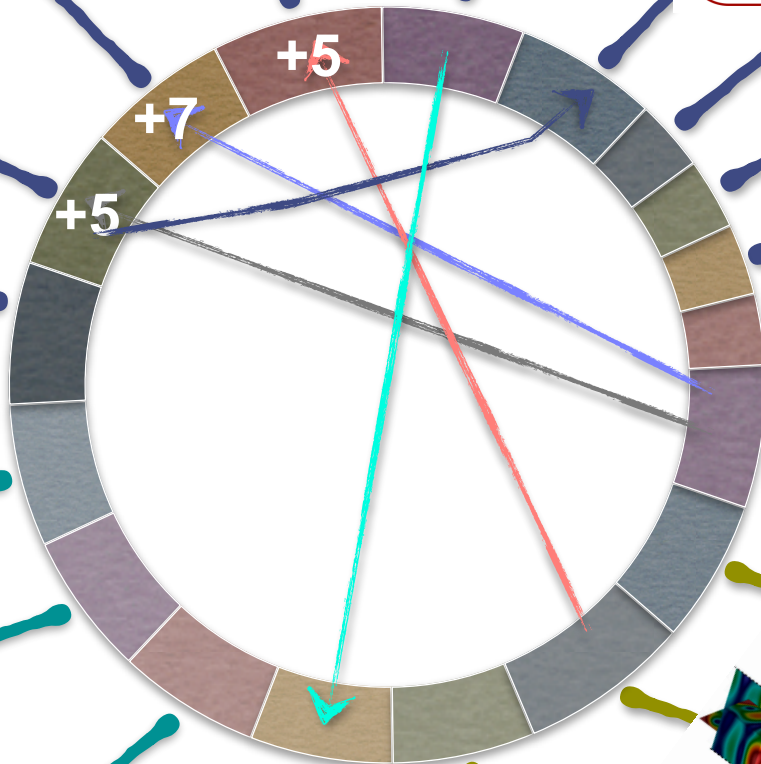
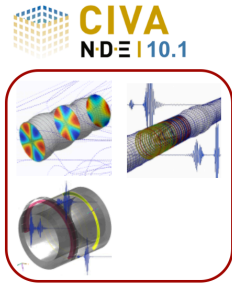
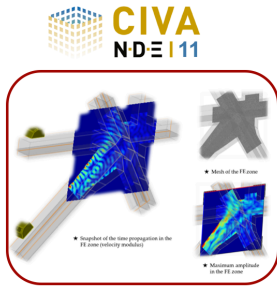
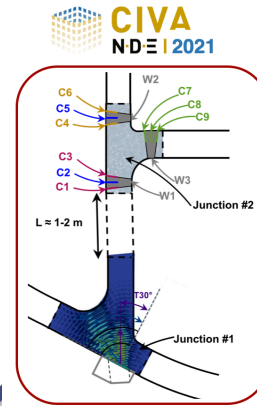
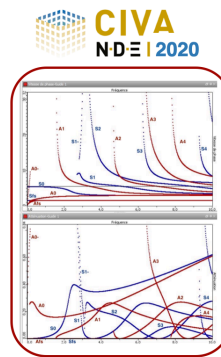
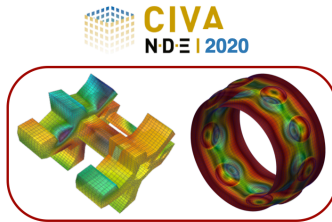
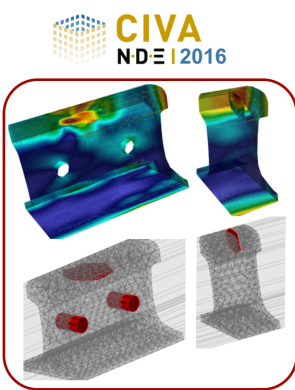


(b)  $\theta = 60^\circ$



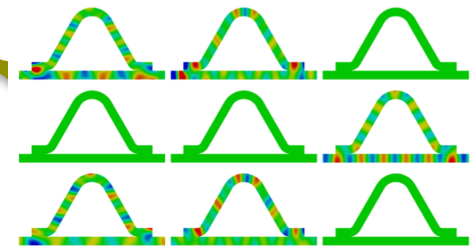
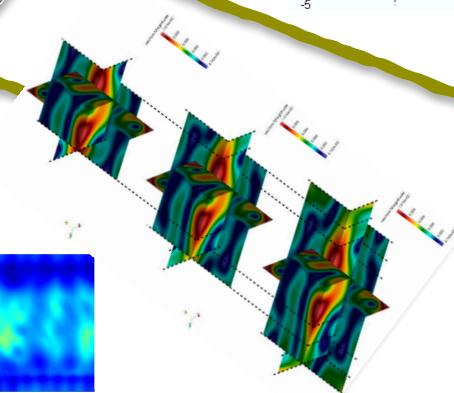
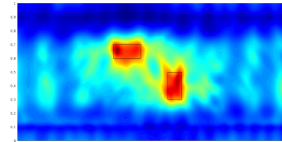
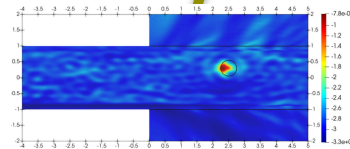
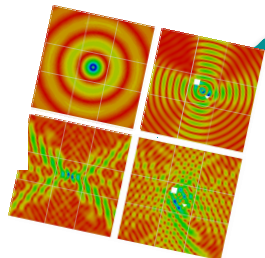
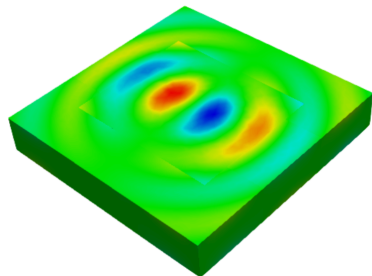
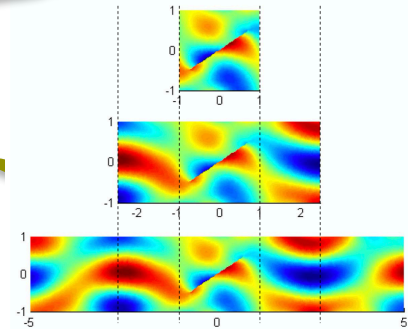
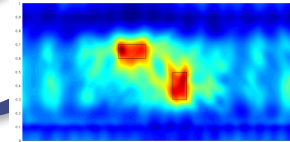
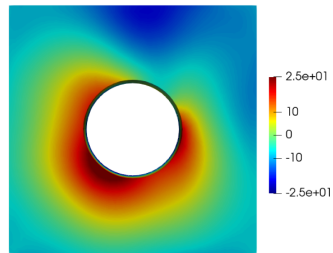
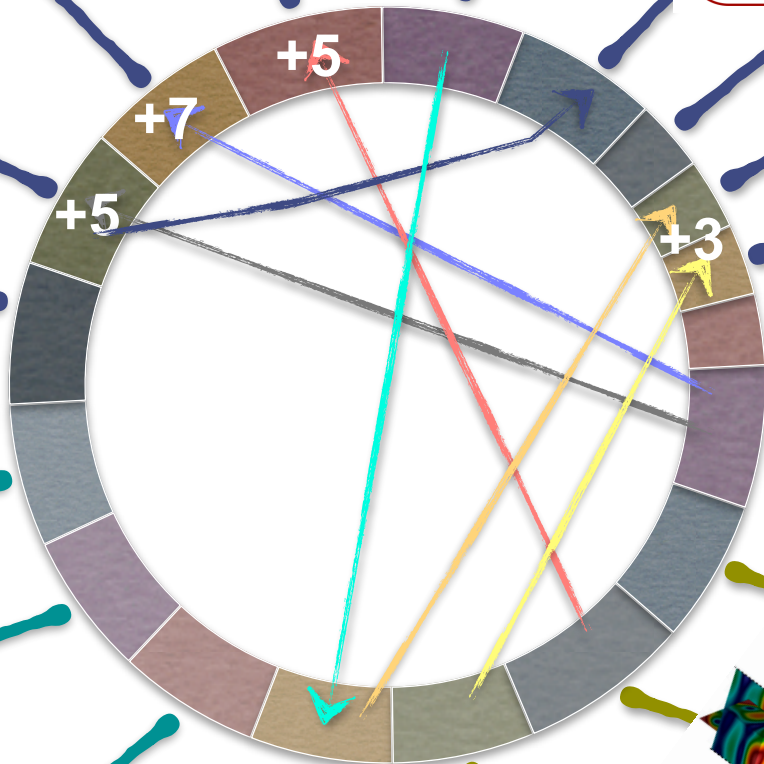
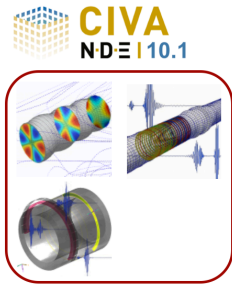
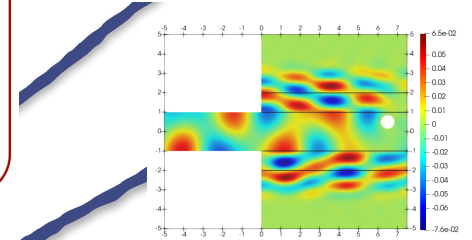
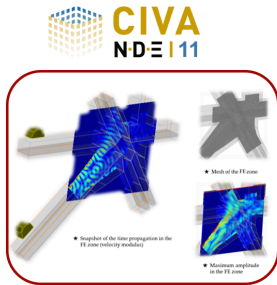
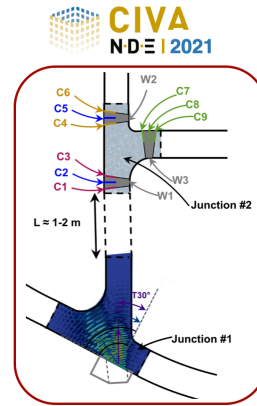
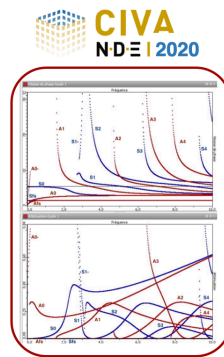
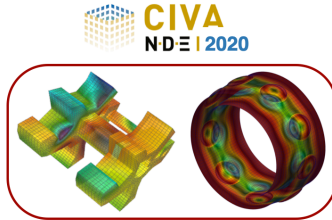
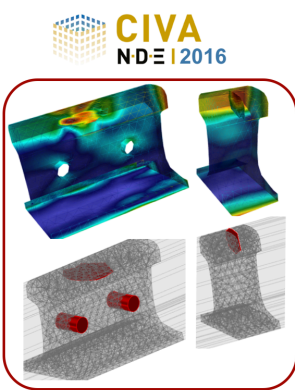
(c)  $\theta = 90^\circ$

# CHRONOLOGY //

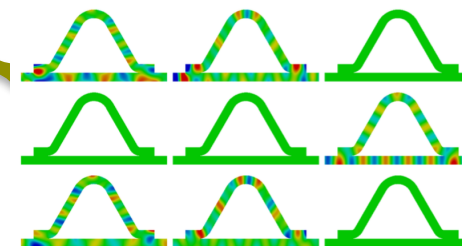
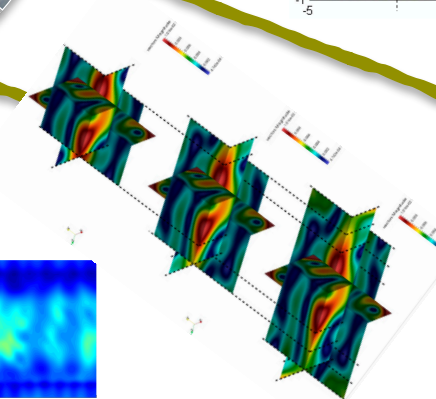
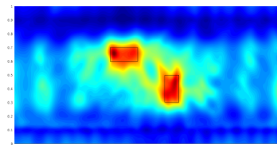
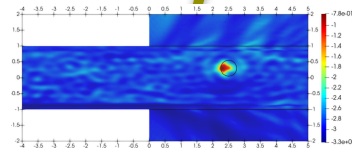
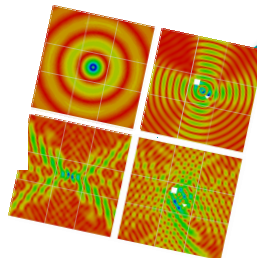
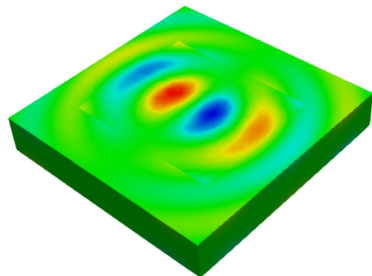
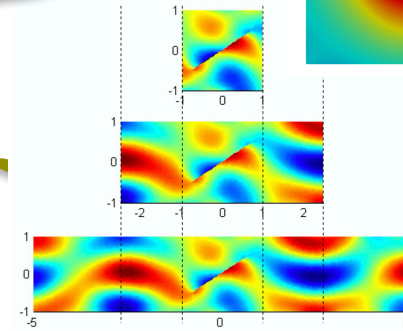
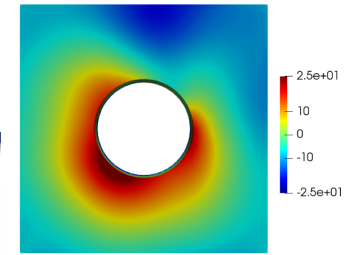
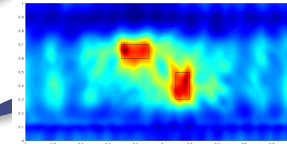
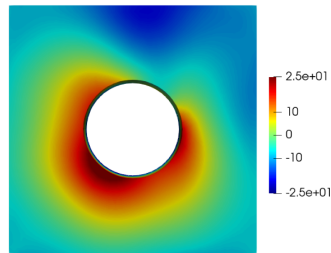
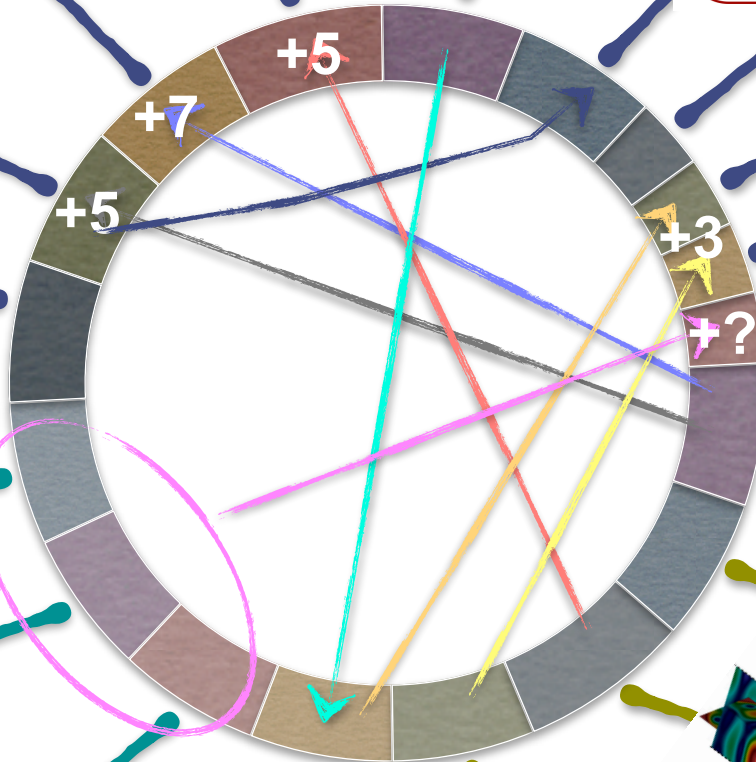
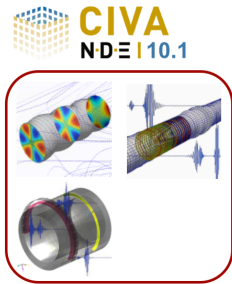
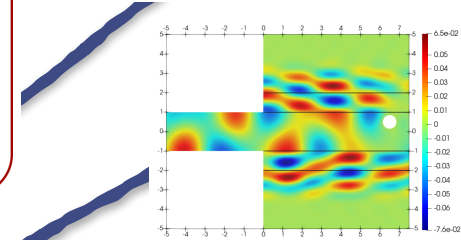
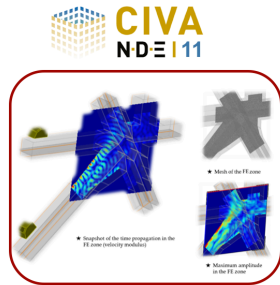
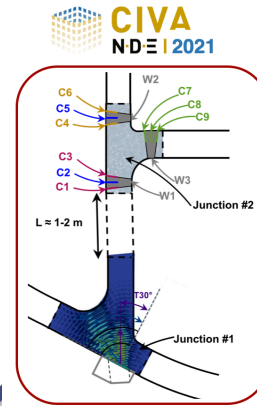
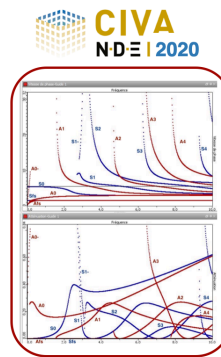
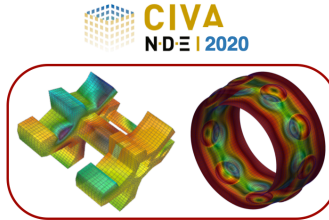
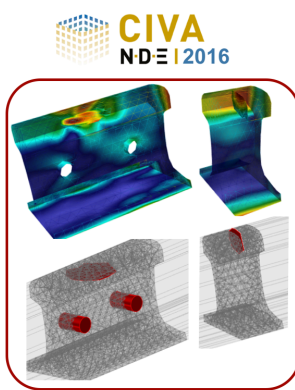




# CHRONOLOGY //



# CHRONOLOGY //



# OUTLINE

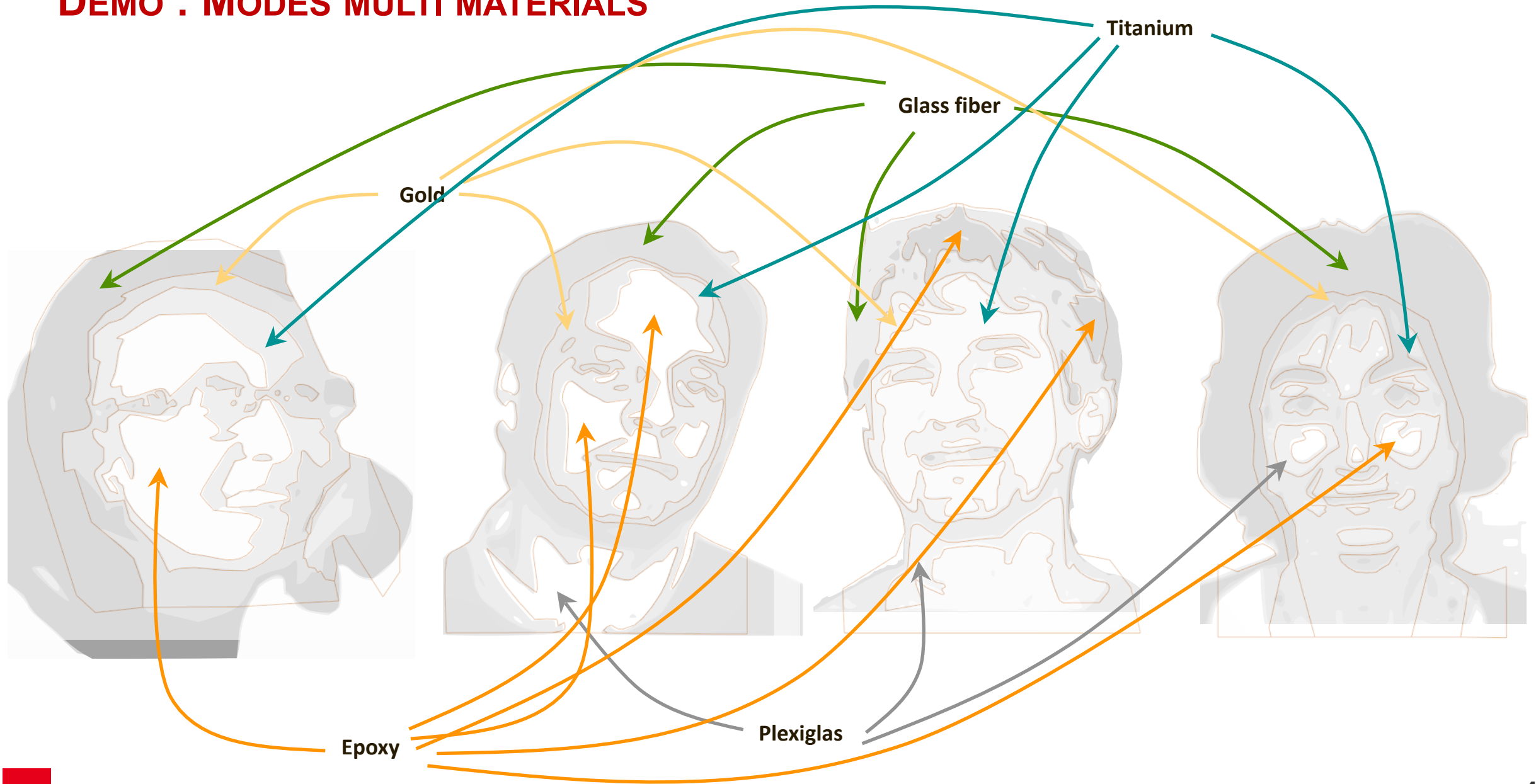
1. Overview of guided wave modeling
  - 1.1. Context/Motivation
  - 1.2. Waveguide and Modal formalism
  
2. Chronology 2006/2024
  - 2.1. CIVA evolution
  - 2.2. Elastic waveguide
  - 2.3. Half Space Matching (HSM)
  
3. Demo

## DEMO : MODES



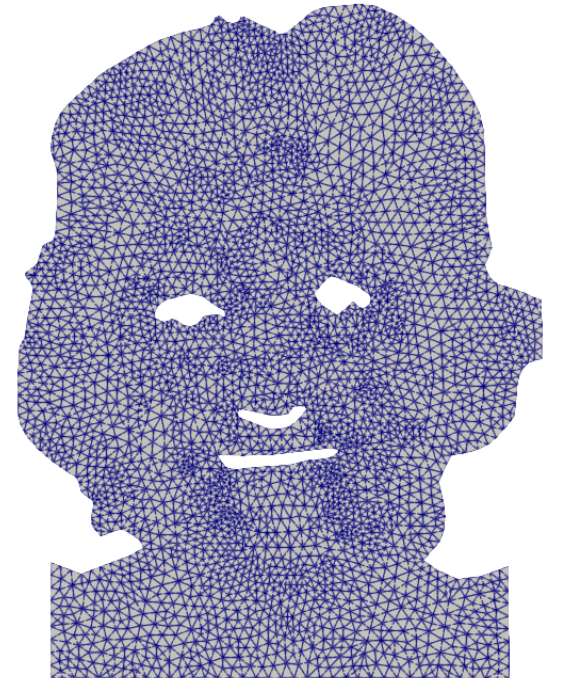
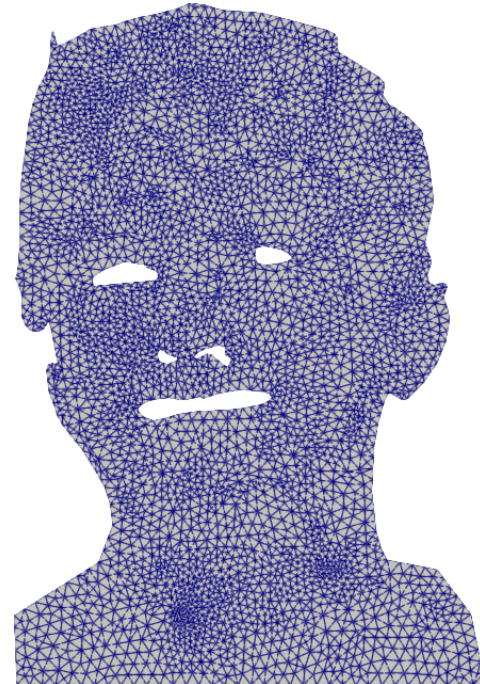
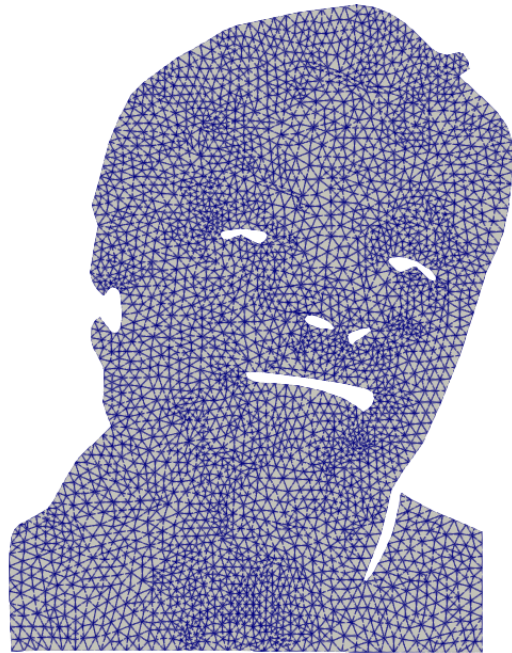
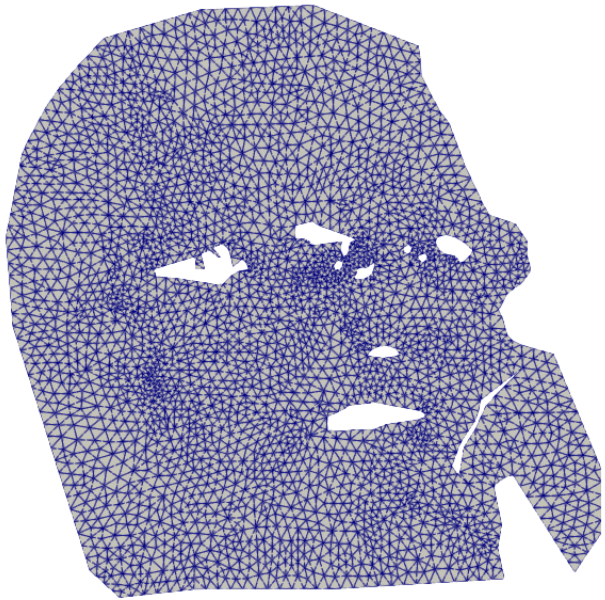


# DEMO : MODES MULTI MATERIALS



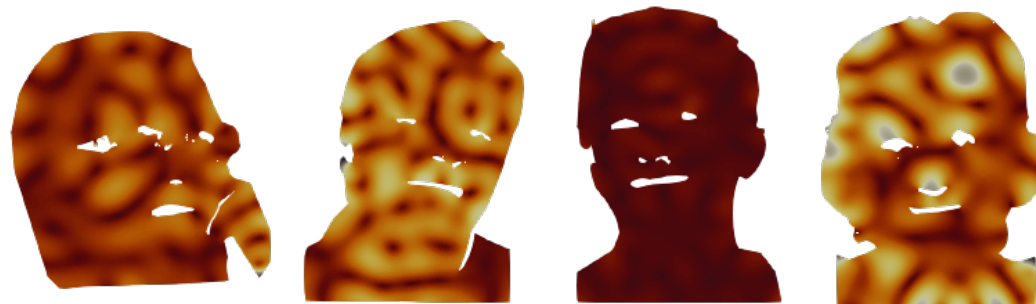


# DEMO : MODES

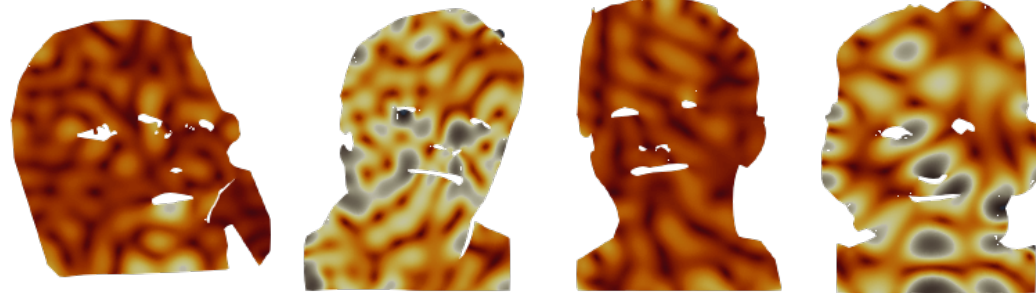


# DEMO : JO MODES

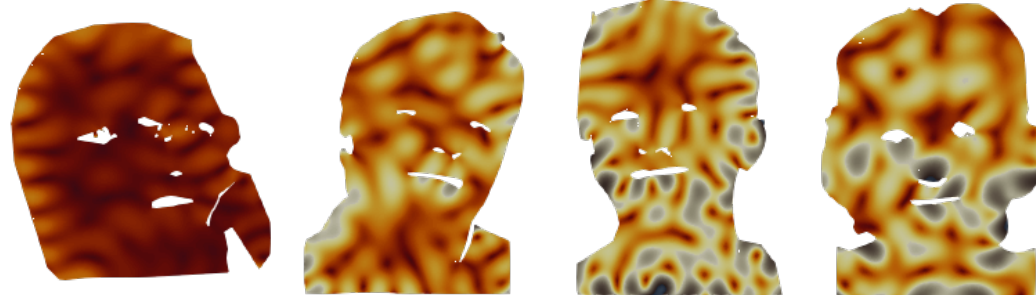
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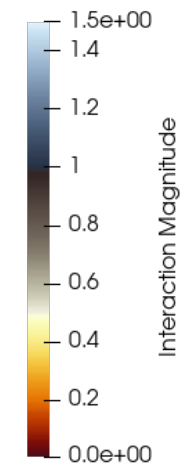
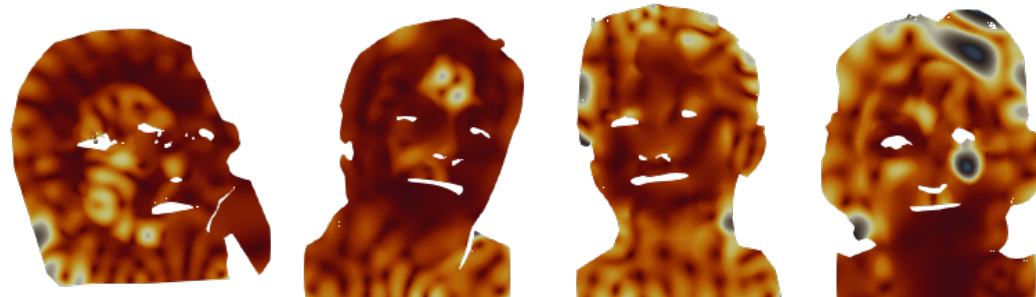
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Gold: 99



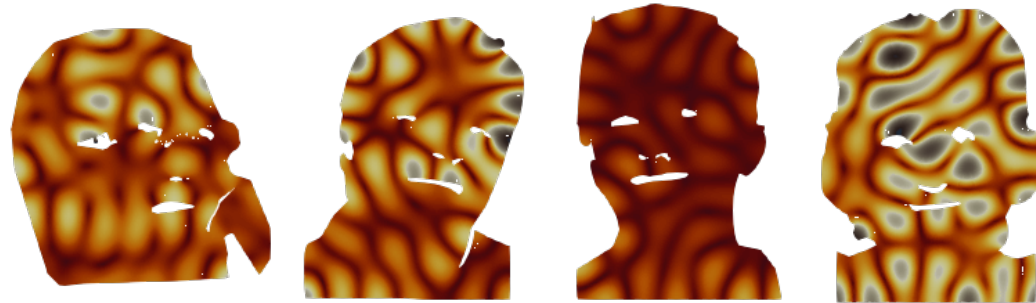
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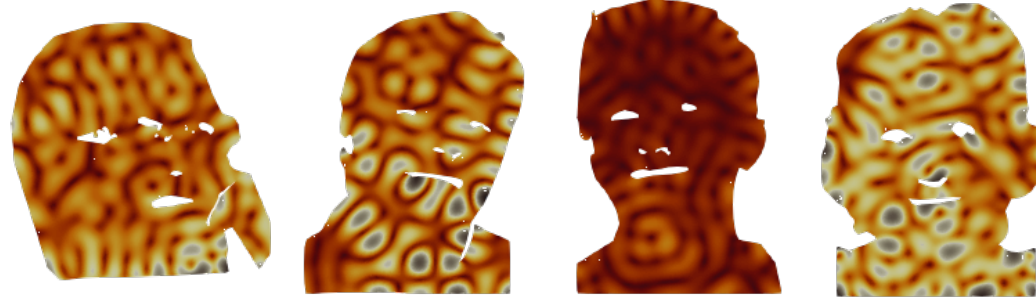


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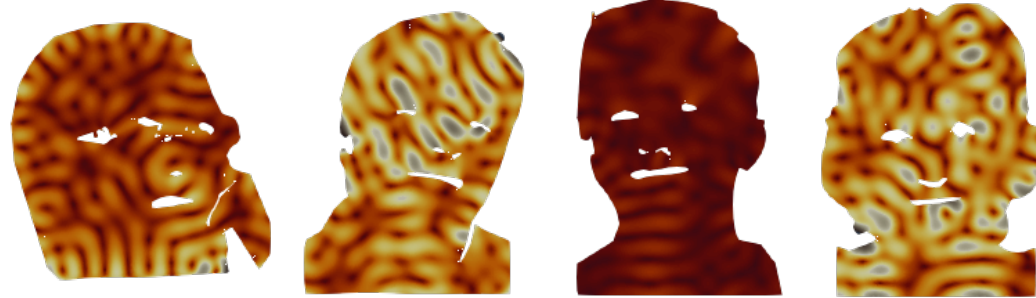
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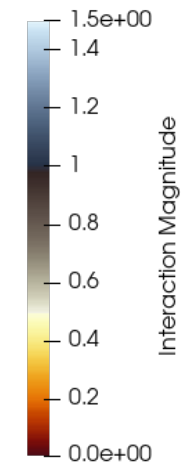
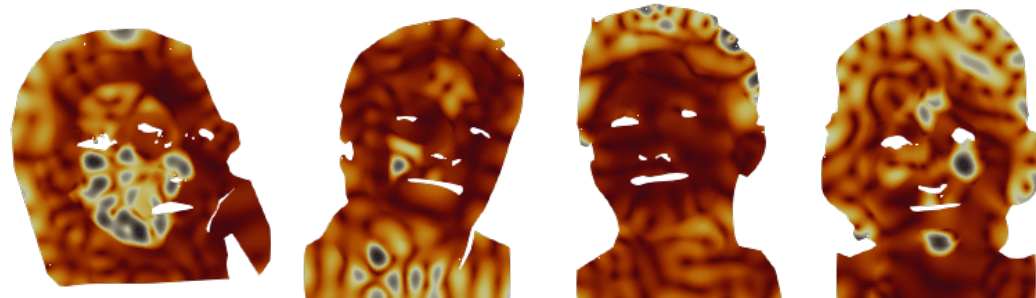
Silver: 200



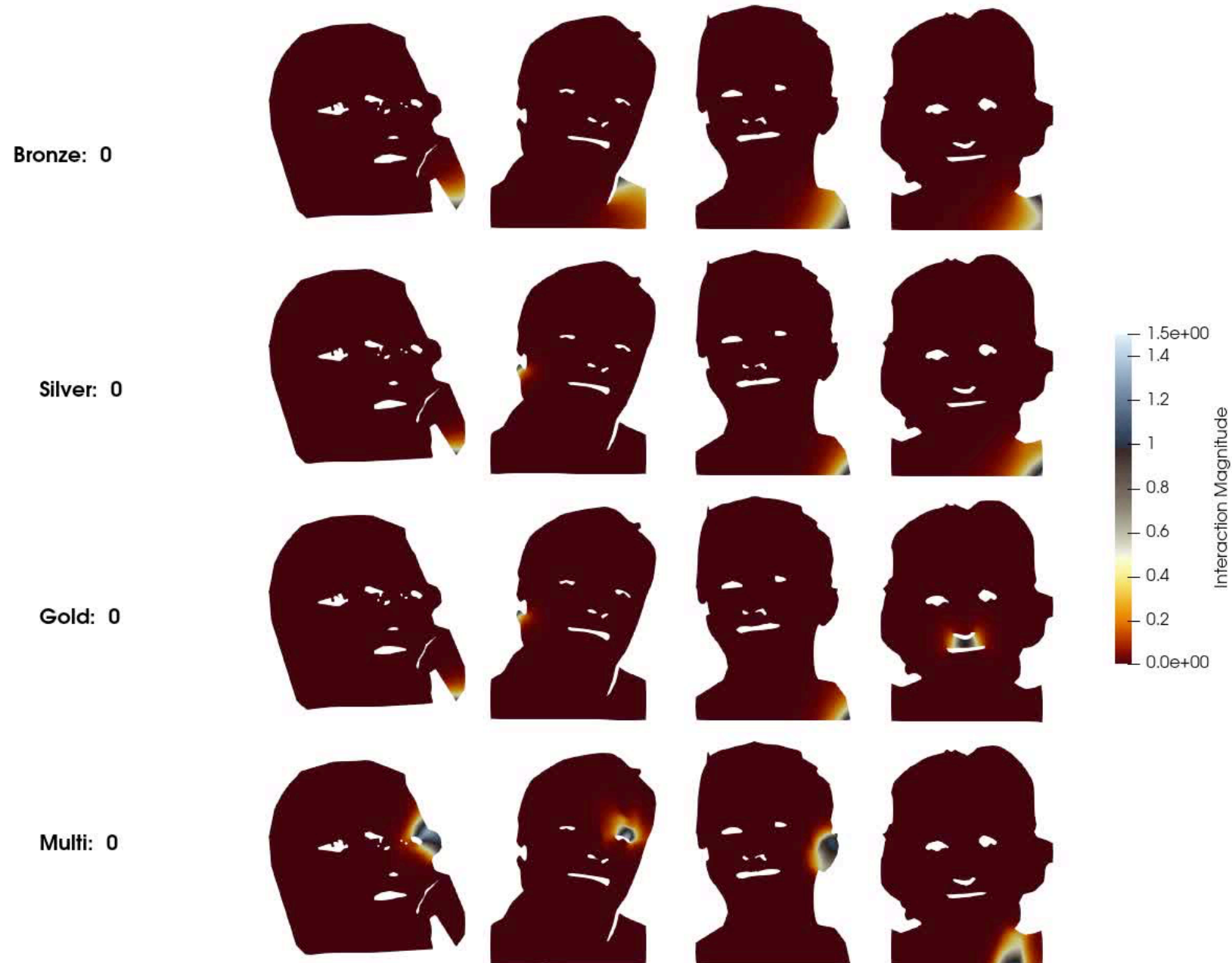
Gold: 200



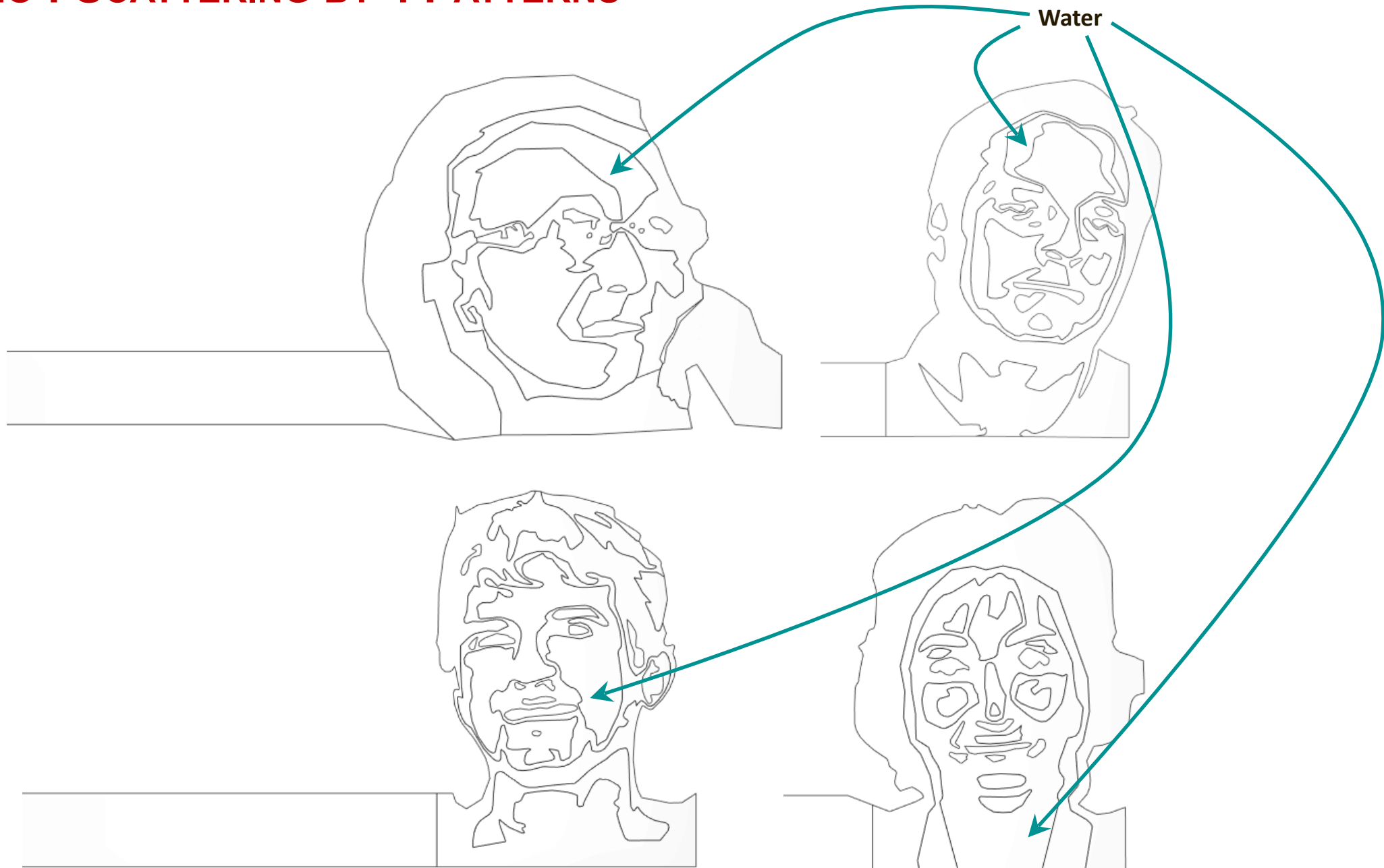
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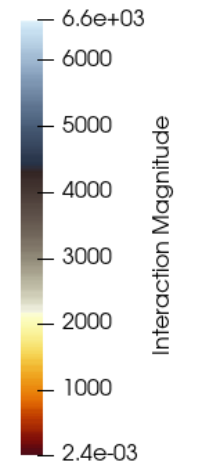


# DEMO : SCATTERING BY 4 PATTERNS



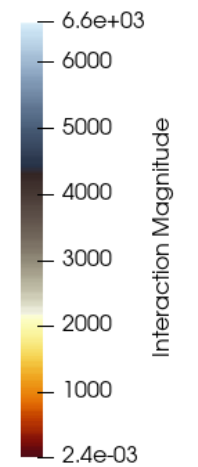
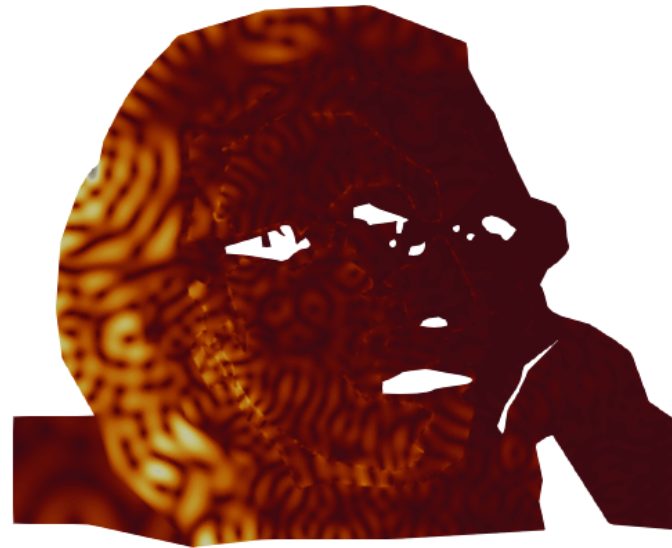


# DEMO : SCATTERING BY POETS' PATTERNS



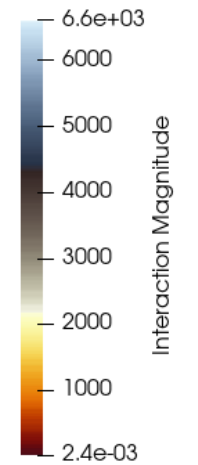
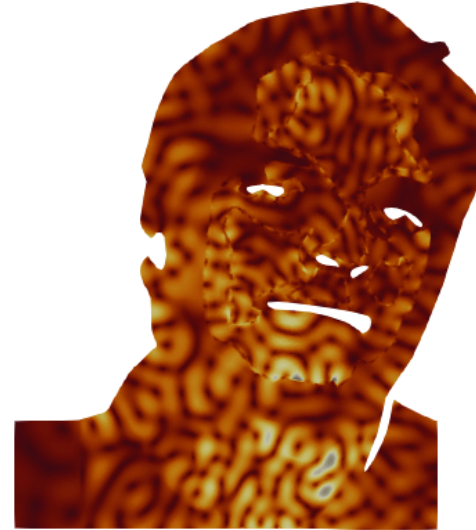
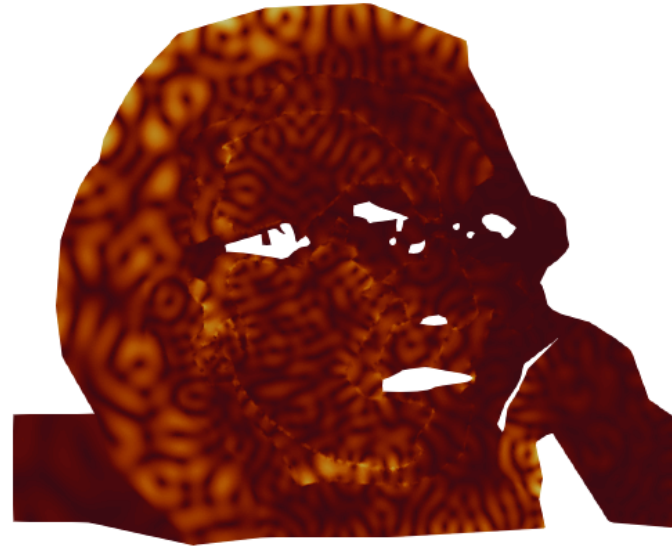
Time: 400.000

# DEMO : SCATTERING BY POETS' PATTERNS



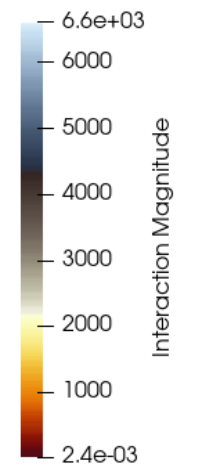
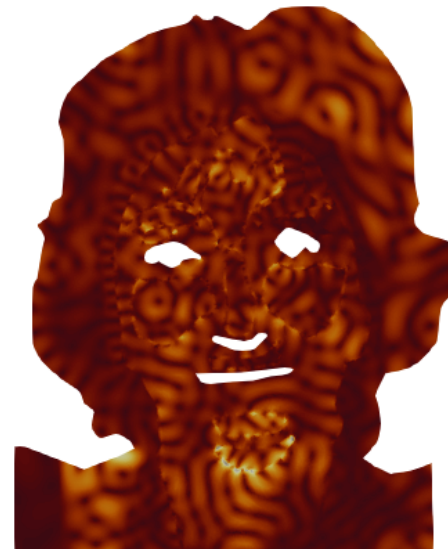
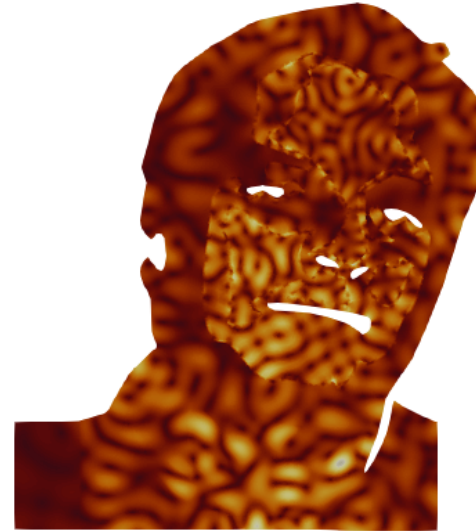
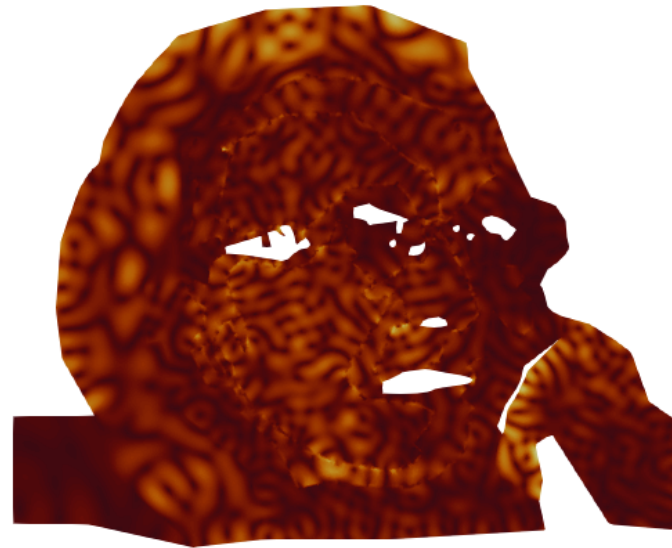
Time: 500.000

# DEMO : SCATTERING BY POETS' PATTERNS



Time: 600.000

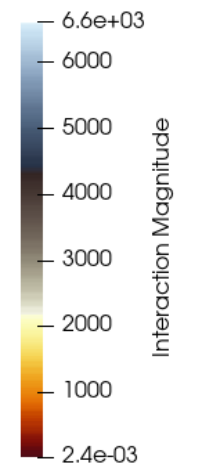
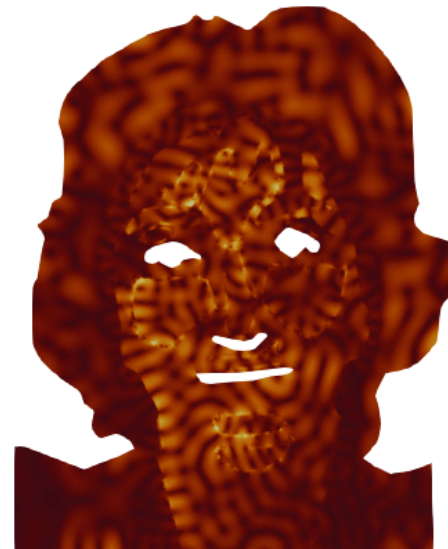
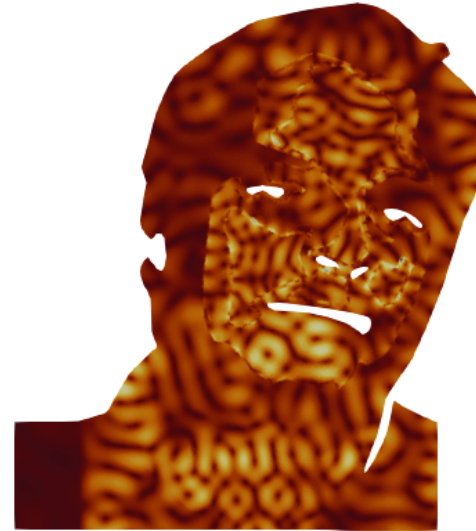
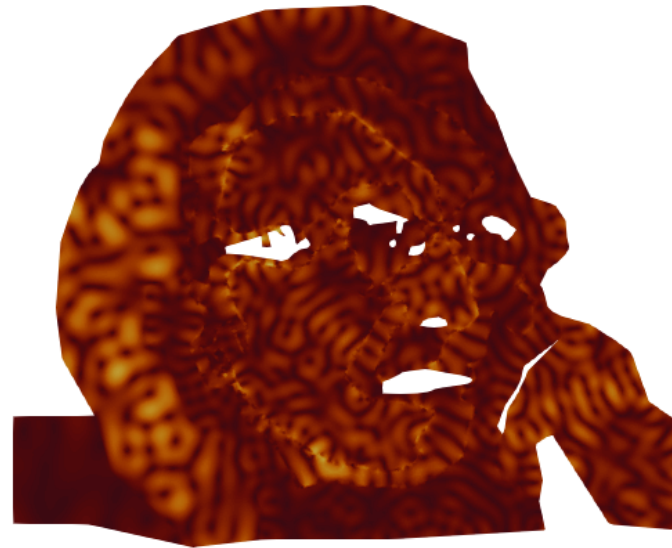
# DEMO : SCATTERING BY POETS' PATTERNS



Time: 700.000

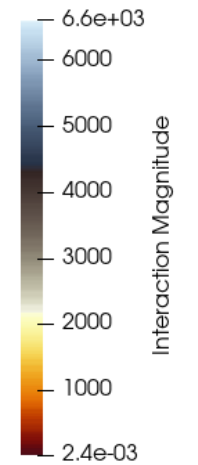
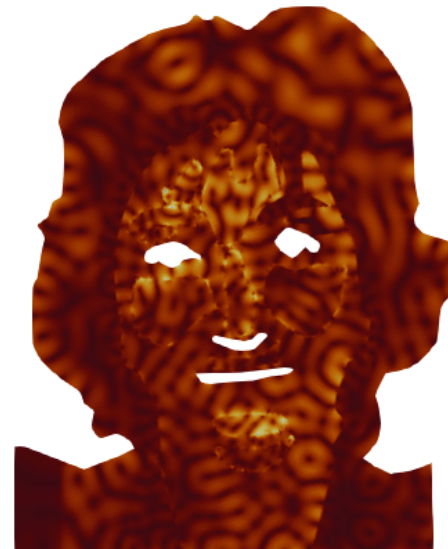


# DEMO : SCATTERING BY POETS' PATTERNS



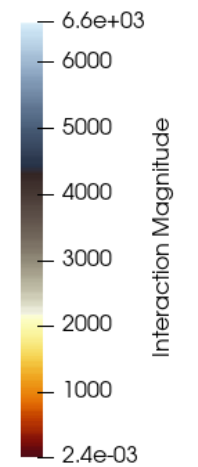
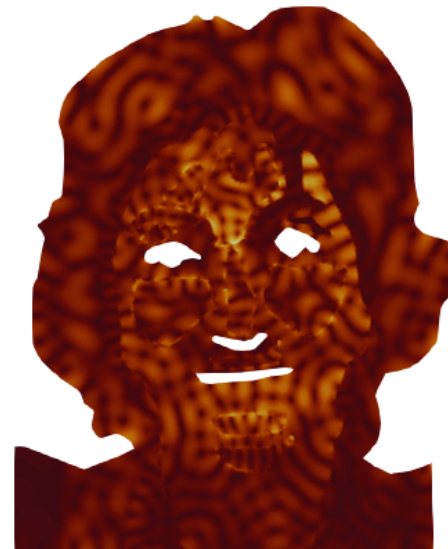
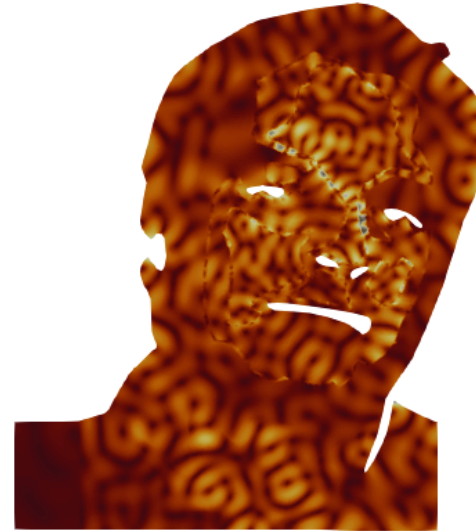
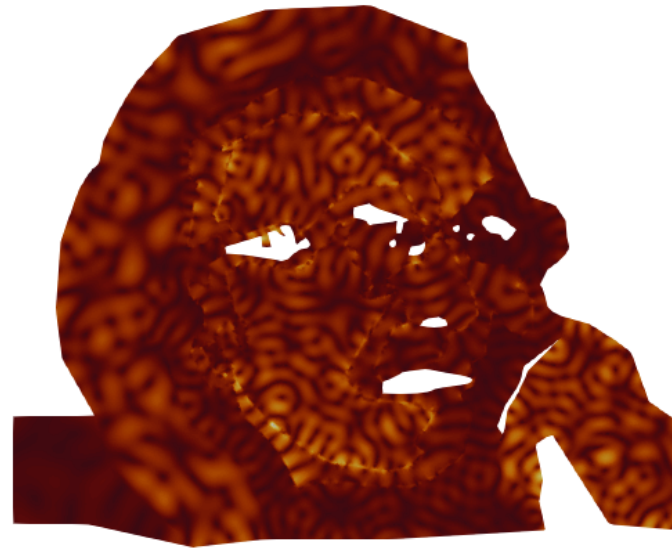
Time: 800.000

# DEMO : SCATTERING BY POETS' PATTERNS



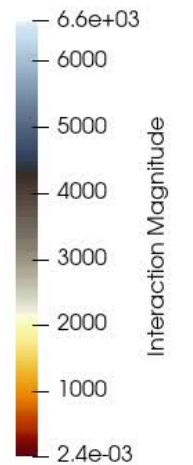
Time: 900.000

# DEMO : SCATTERING BY POETS' PATTERNS



Time: 1000.000

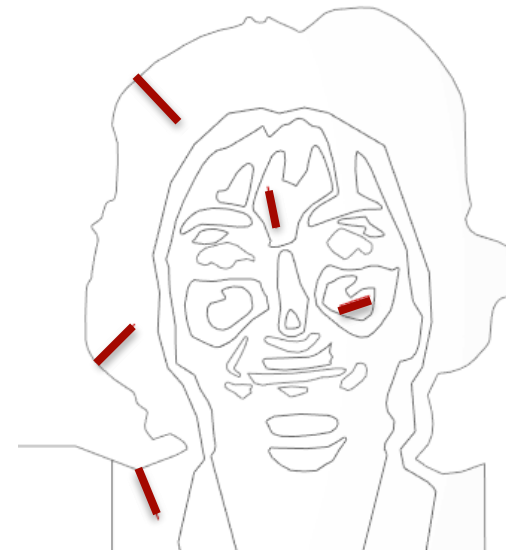
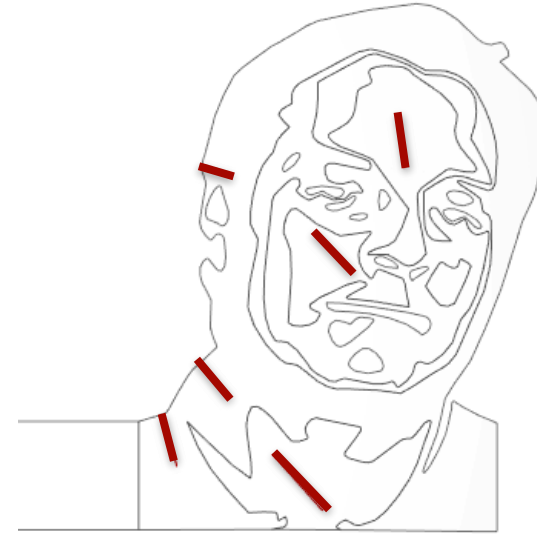
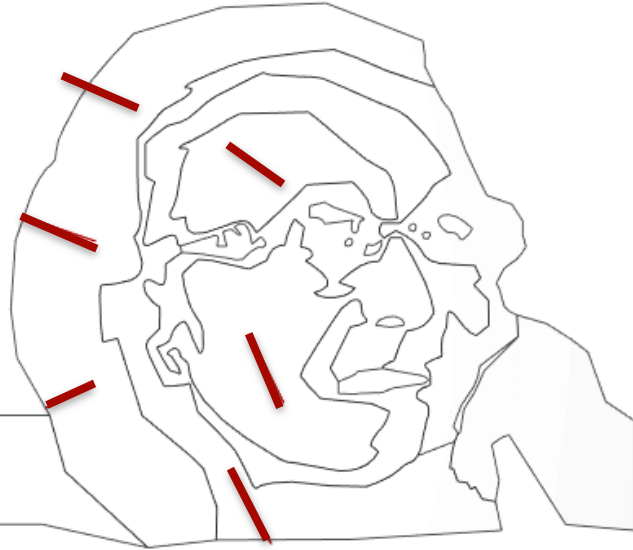
# DEMO : SCATTERING BY POETS' PATTERNS



Time: 0.000



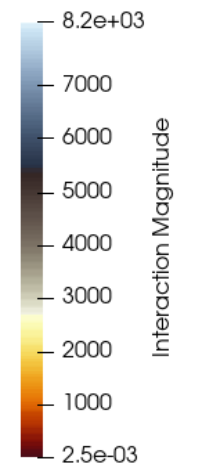
# DEMO : SCATTERING BY POETS' PATTERNS + CRACKS



# DEMO : SCATTERING BY POETS' PATTERNS + CRACKS

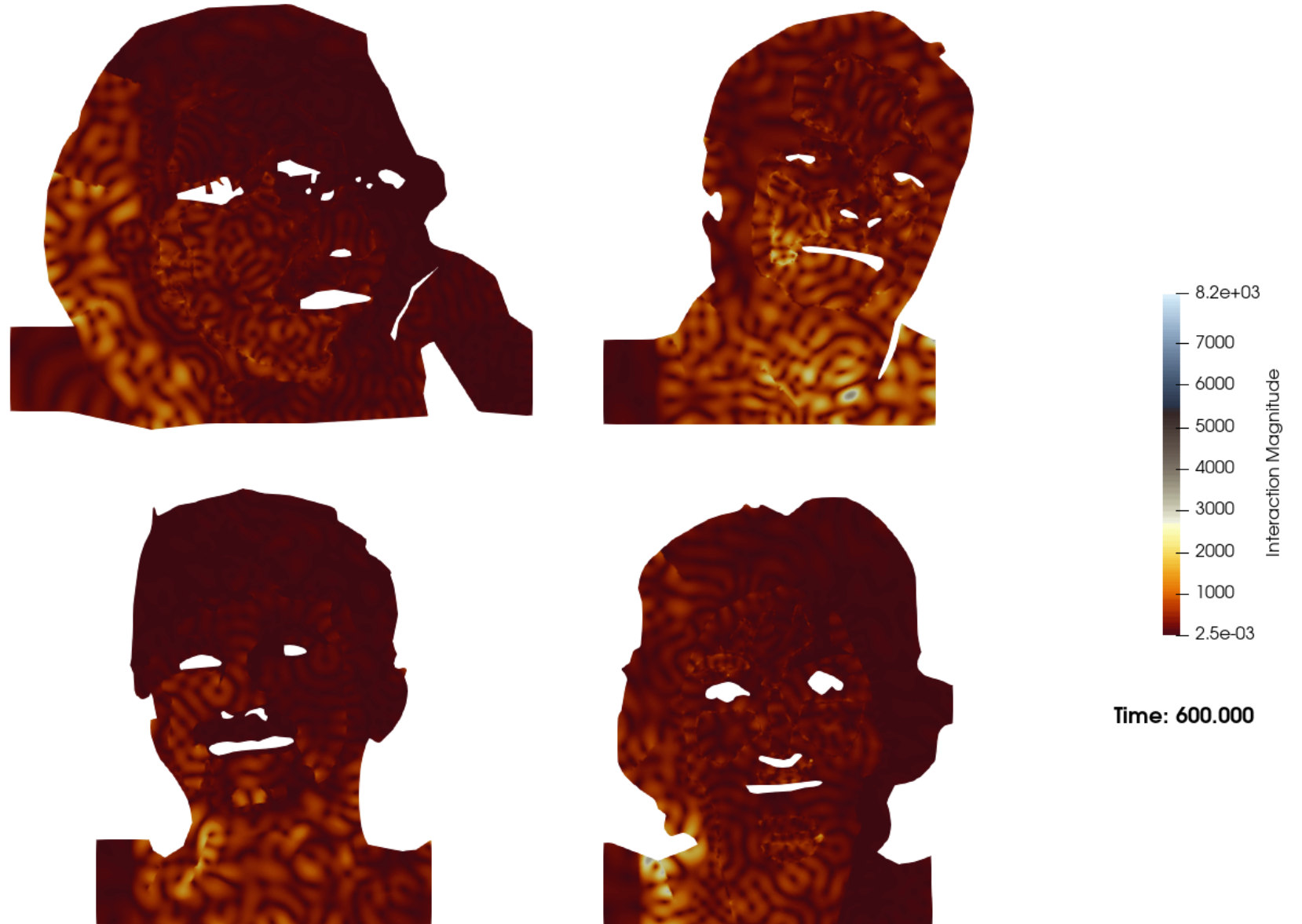


# DEMO : SCATTERING BY POETS' PATTERNS + CRACKS



Time: 500.000

# DEMO : SCATTERING BY POETS' PATTERNS + CRACKS





# DEMO : SCATTERING BY POETS' PATTERNS + CRACKS



# DEMO : SCATTERING BY POETS' PATTERNS + CRACKS



# DEMO : SCATTERING BY POETS' PATTERNS + CRACKS

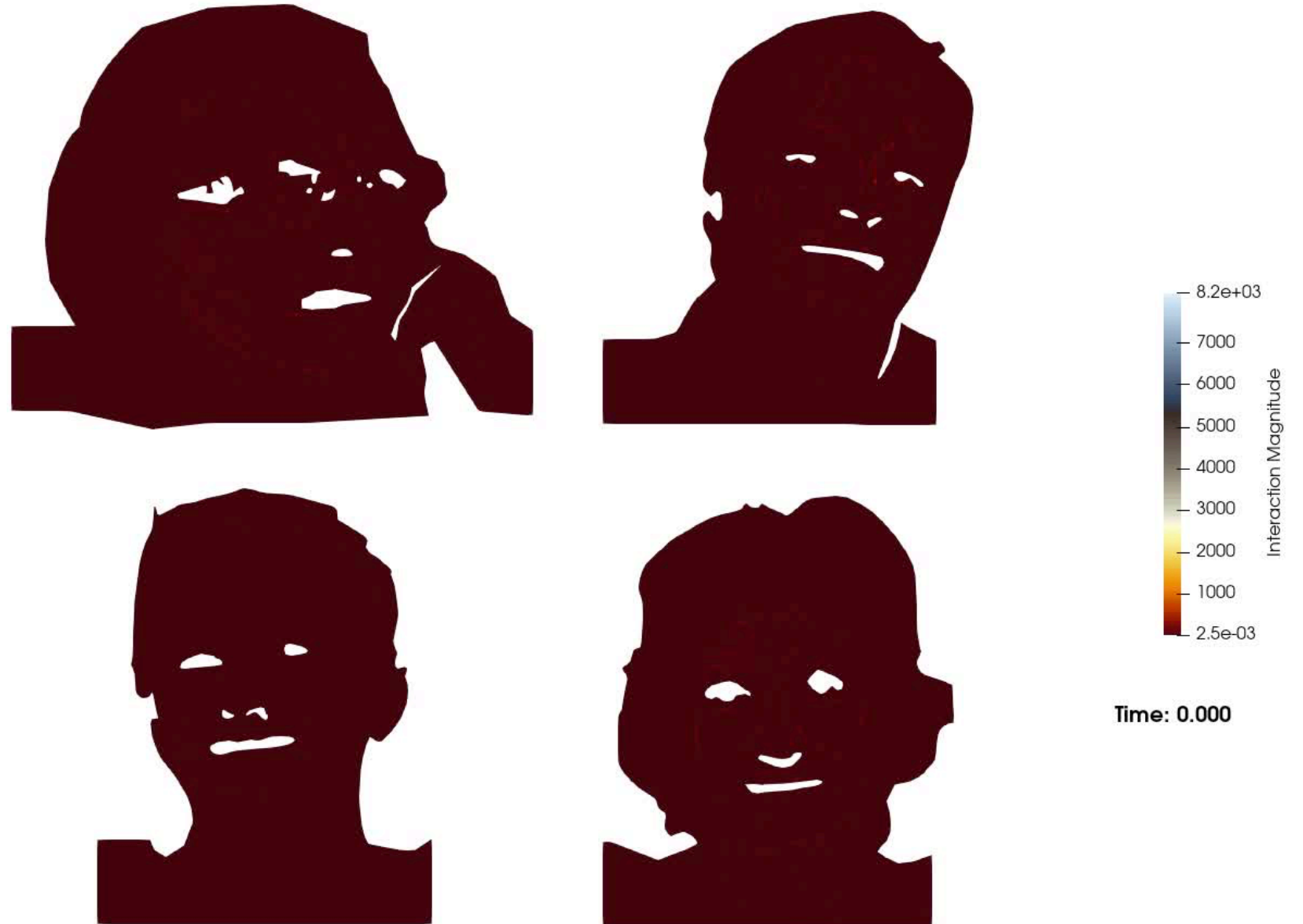


# DEMO : SCATTERING BY POETS' PATTERNS + CRACKS

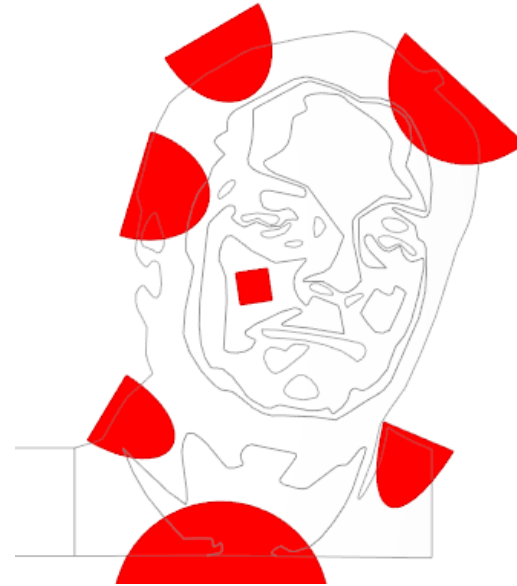
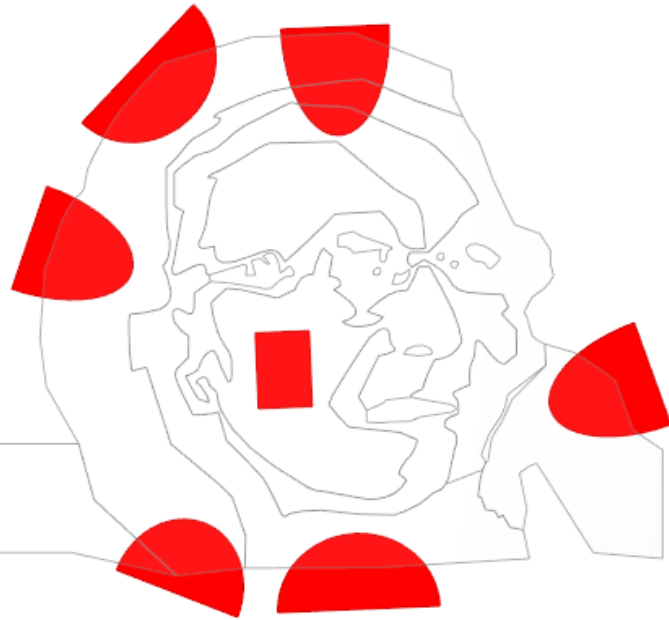




# DEMO : SCATTERING BY POETS' PATTERNS + CRACKS



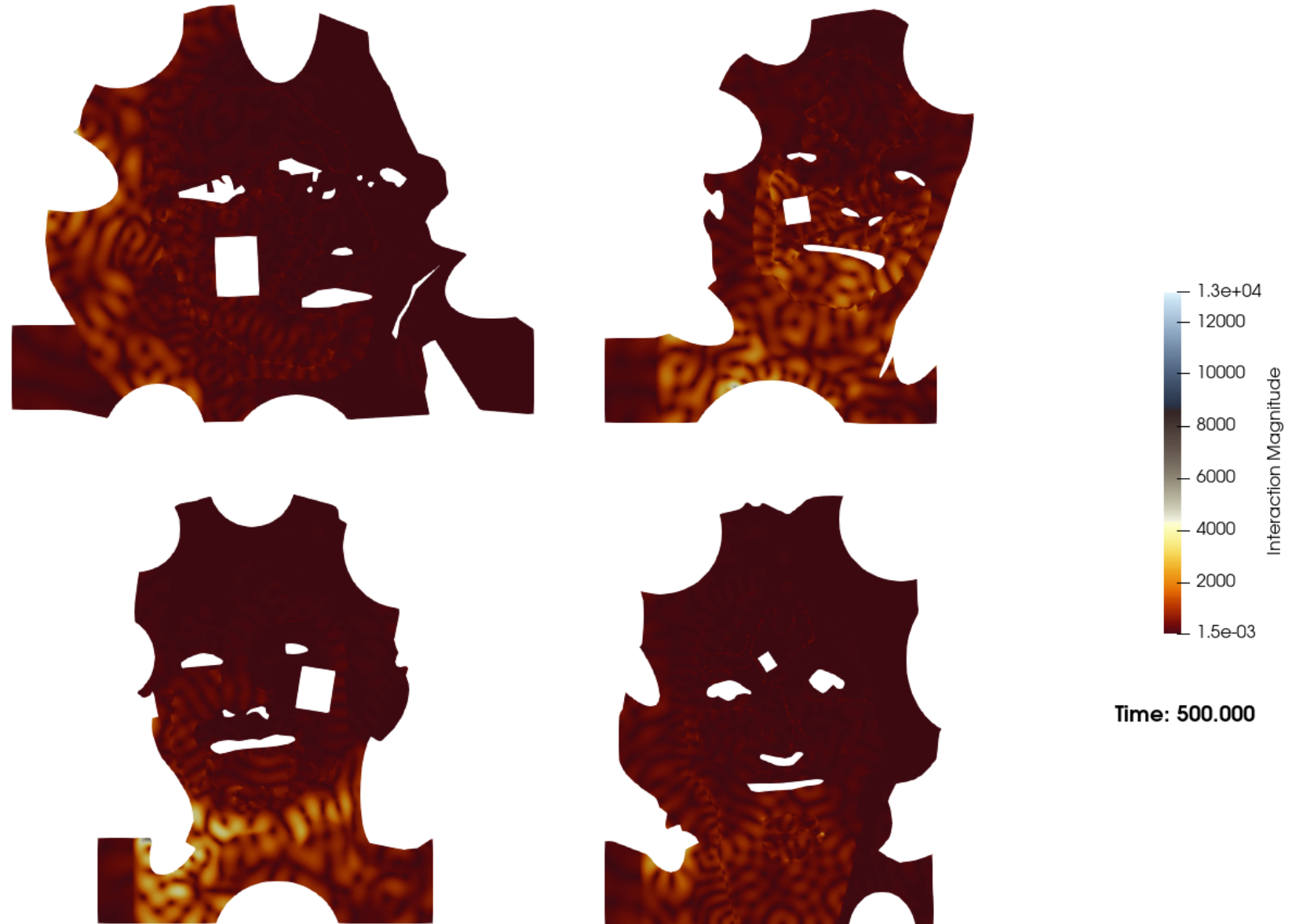
# DEMO : SCATTERING BY POETS' PATTERNS + HOLE(MIAM)



# DEMO : SCATTERING BY POETS' PATTERNS + HOLE(MIAM)

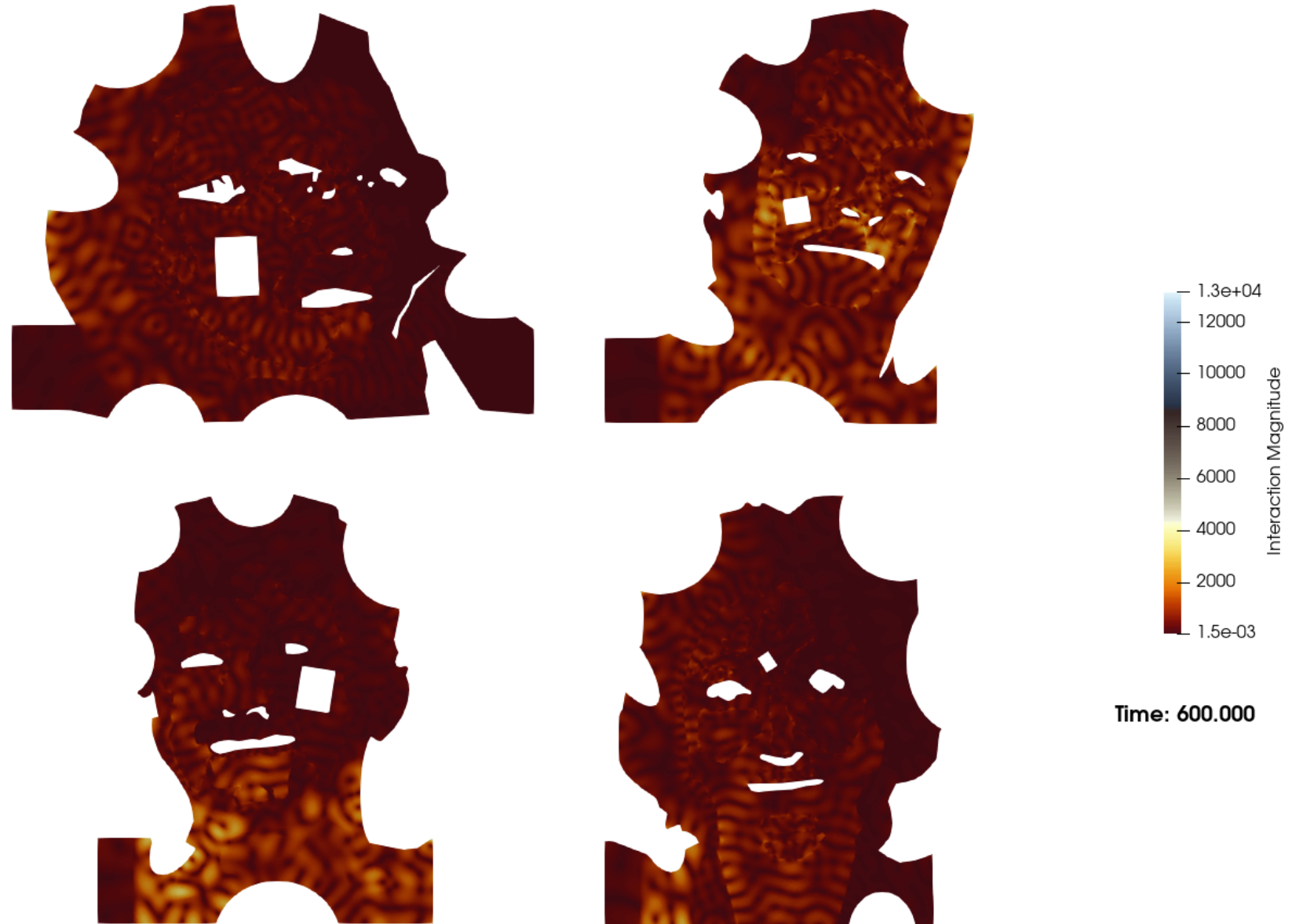


# DEMO : SCATTERING BY POETS' PATTERNS + HOLE(MIAM)

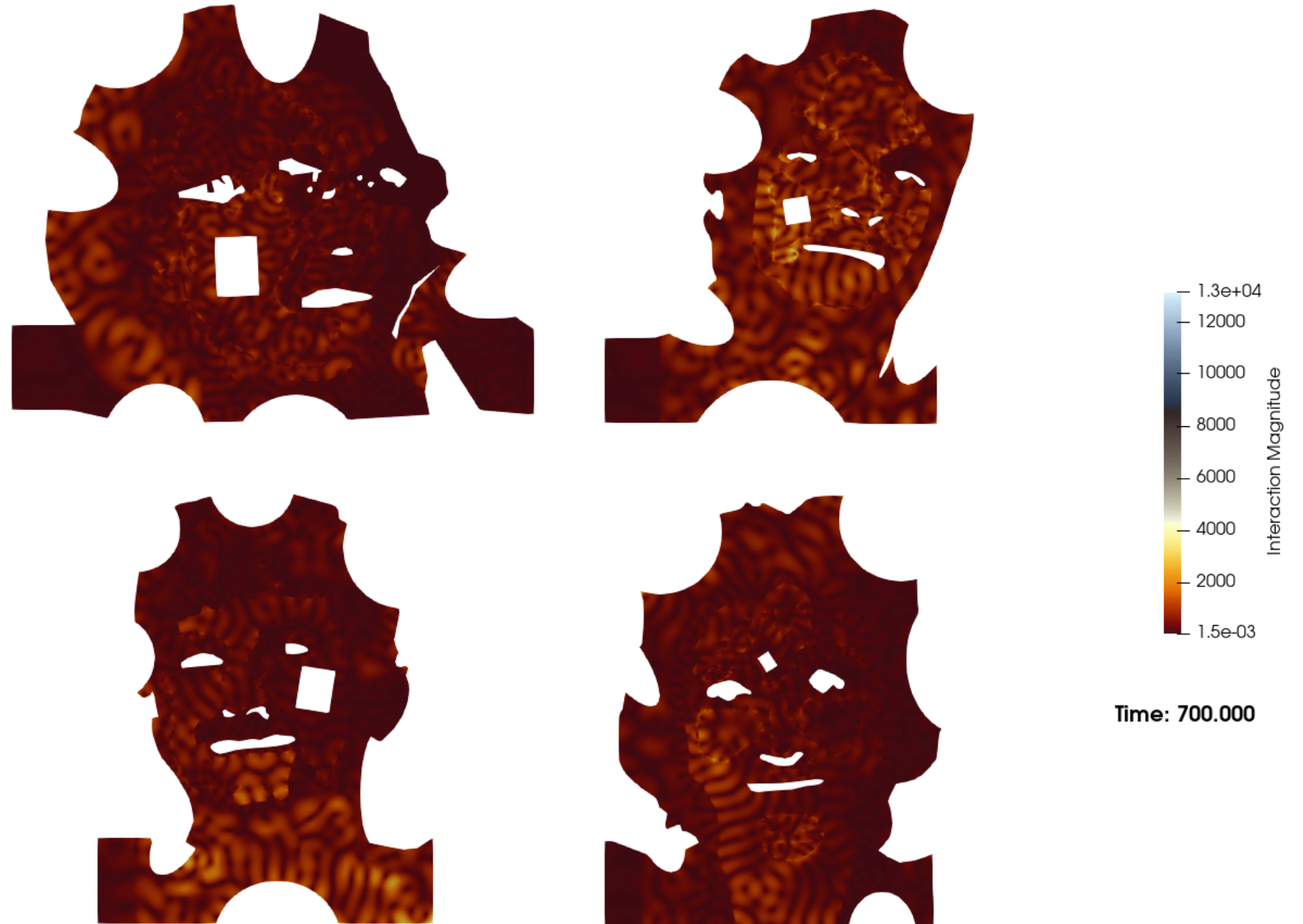




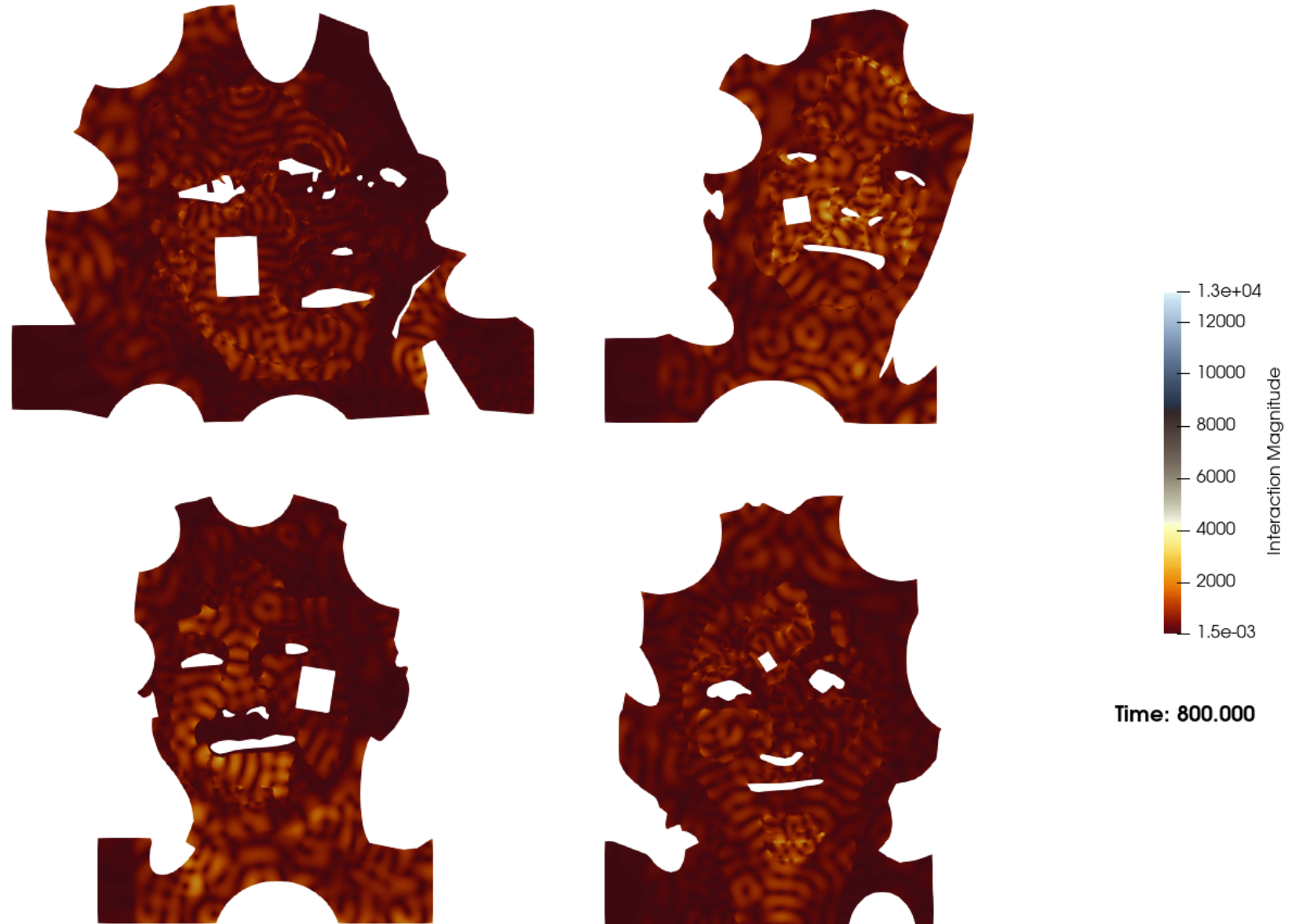
# DEMO : SCATTERING BY POETS' PATTERNS + HOLE(MIAM)



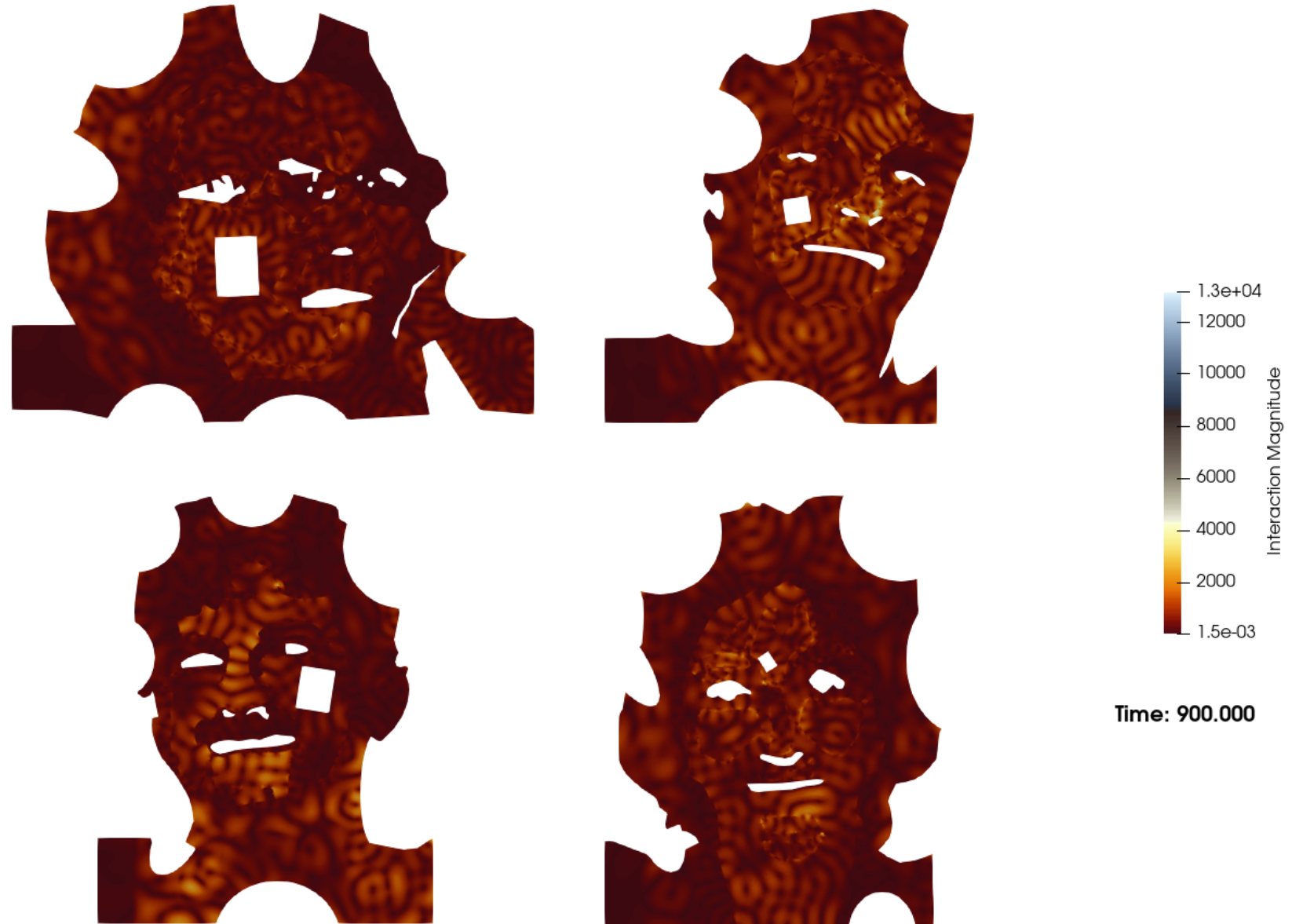
# DEMO : SCATTERING BY POETS' PATTERNS + HOLE(MIAM)



# DEMO : SCATTERING BY POETS' PATTERNS + HOLE(MIAM)

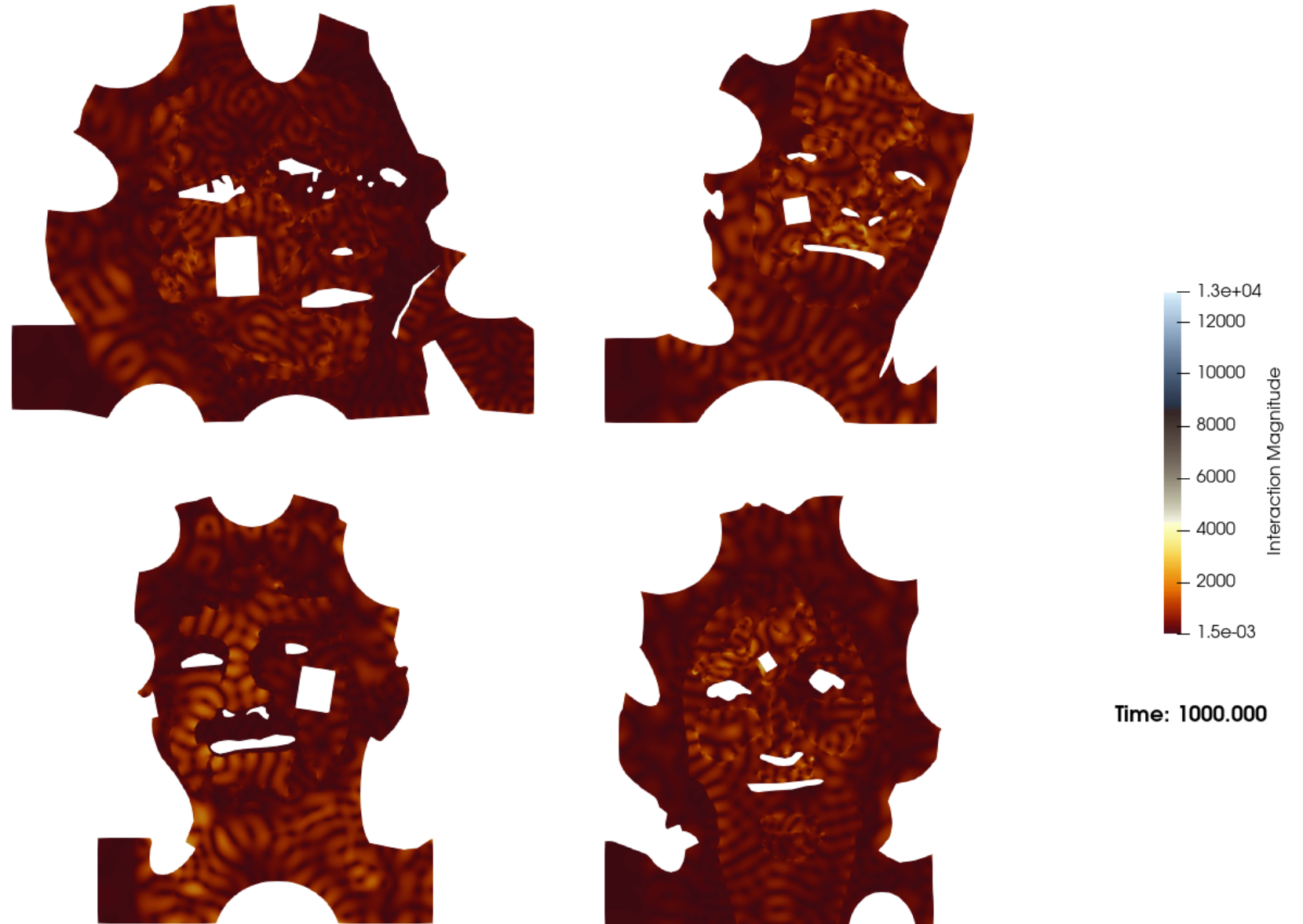


# DEMO : SCATTERING BY POETS' PATTERNS + HOLE(MIAM)

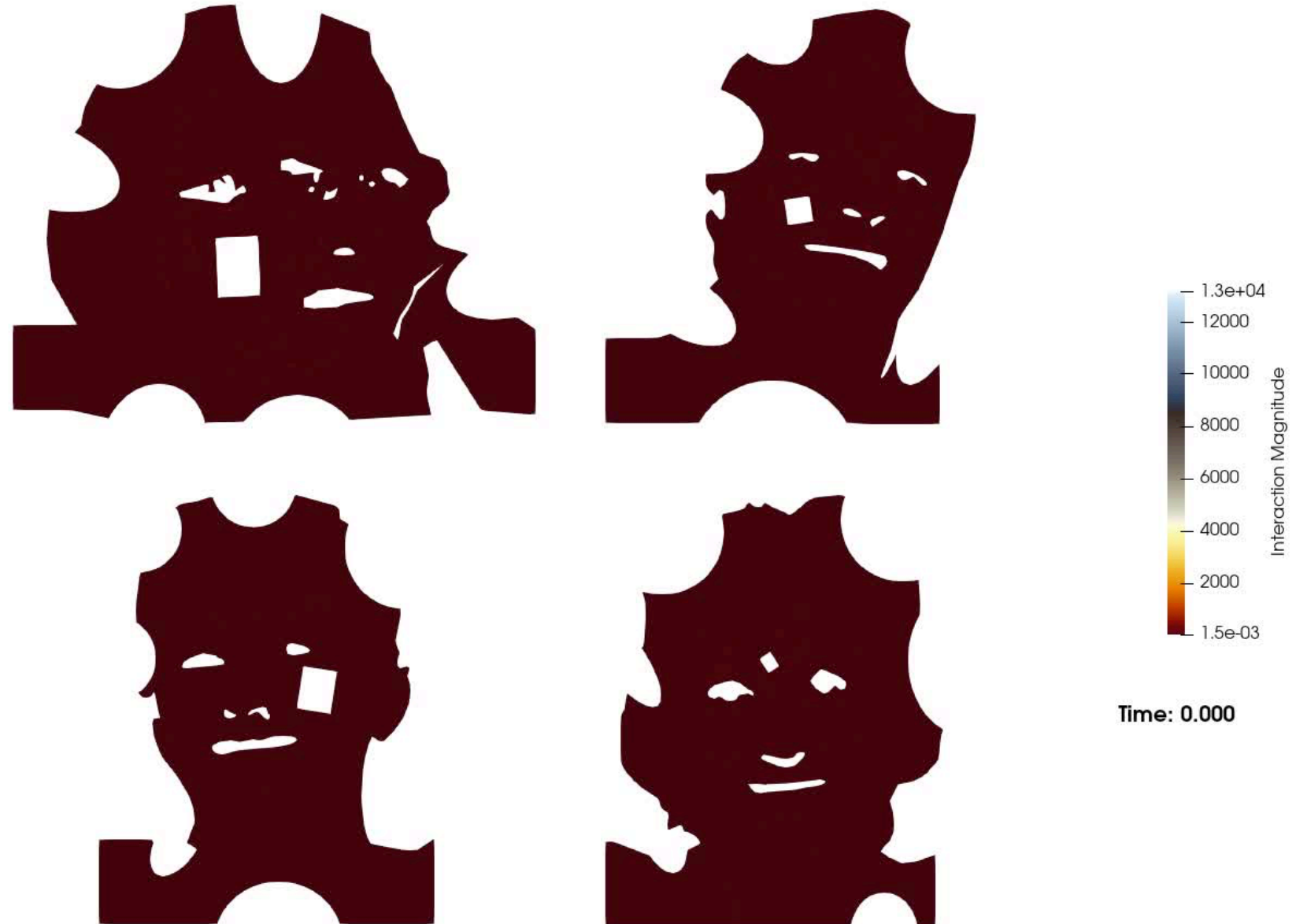




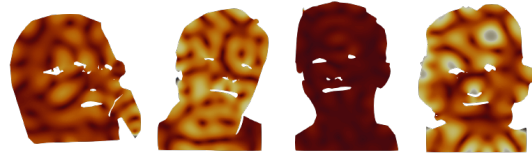
# DEMO : SCATTERING BY POETS' PATTERNS + HOLE(MIAM)



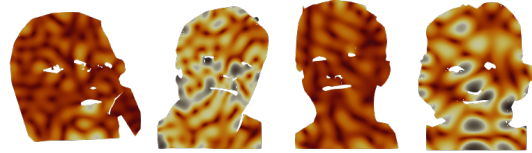
# DEMO : SCATTERING BY POETS' PATTERNS + HOLE(MIAM)



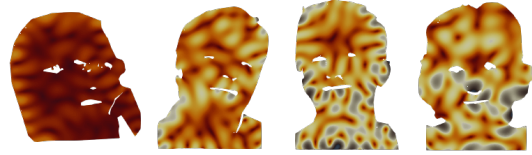
Bronze: 99



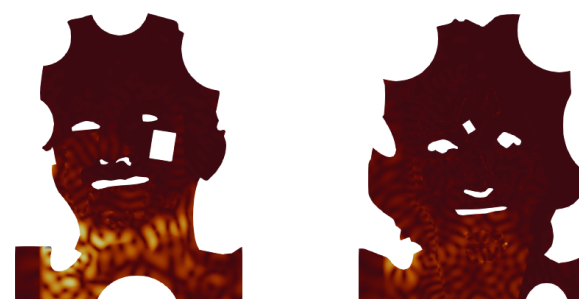
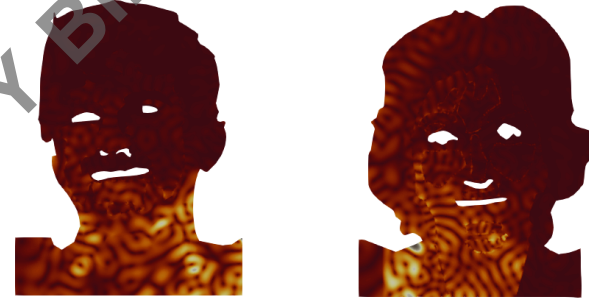
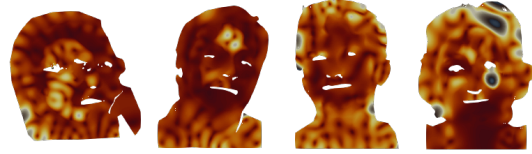
Silver: 99



Gold: 99



Multi: 99



THANKS FOR ALL & HAPPY BIRTHDAY



**POUR ANNE-SOPHIE**

**AMOND ALLOUKO**





# **OBJECTIF :**

**J'aimerais te remercier pour ce que tu as fait pour moi.  
T'honorer pour ces années et tes contributions pour la  
recherche française.**



# D'OÙ JE FAIS CES SLIDES

On a rien vu, ok ? 😊

Abidjan, Côte d'Ivoire



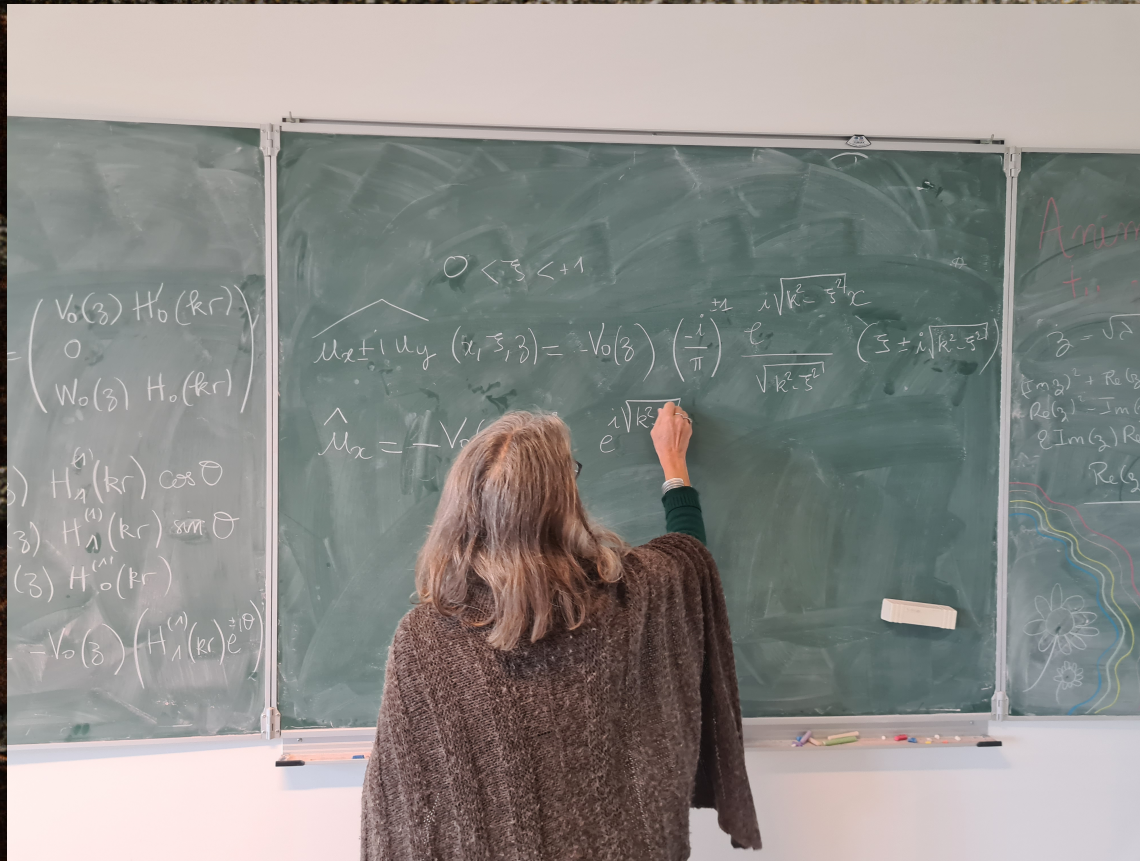


# CE QUE JE RETIENS DE TOI :

- GENTILLESSE, ATTENTIONNÉE, MATERNELLE
- RIGoureuse, MÊME DANS LES PETITES CHOSES
- POUR L'ÉNERGIE : ALORS LÀ, TU SAIS EN TRANSMETTRE 😊
- TRÈS PÉDAGOGUE, J'AI ÉNORMÉMENT APPRIS DE TOI



# J'ADORAIS TE VOIR PARTIR DANS DES DÉVELOPPEMENTS



**Pour à la fin, te demander de résumer.**

**Toujours patiente pour réexpliquer.**





**EN RÉSUMÉ, MERCI  
POUR TOUT. MA  
FIERTÉ A ÉTÉ DE TE  
RENDRE FIER**



**Je retourne pour une seconde  
bière, amusez vous !**